
**Economic Risk and Decision Analysis
for Oil and Gas Industry
CE81.9008**

**School of Engineering and Technology
Asian Institute of Technology**

January Semester

**Presented by
Dr. Thitisak Boonpramote**

Department of Mining and Petroleum Engineering, Chulalongkorn University

Simulation using @RISK

What is @RISK?

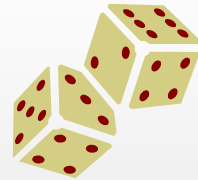
- @RISK is a modeling tool that allows you to incorporate (and quantify) uncertainty in your decision making
 - Similar software is Crystal Ball
 - Implements Monte Carlo simulation via an Excel Add-in
 - Leverages power of Excel to facilitate model construction, analysis and presentation of results
-

Why use @RISK?

- Statistical and uncertainty models can range from very simple to very complex
 - Models can quickly become too complex for manual calculations
 - Best explained with an illustration
-

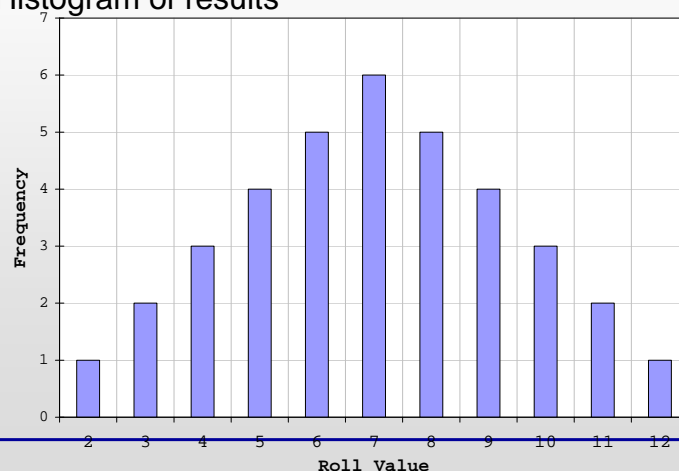
Rolling the Dice – A simple @RISK model

- Two six-sided dice, numbering 1 to 6
- Questions
 - What are the possible combinations of numbers that can occur on any roll?
 - What is the frequency of occurrence of each number?
- Both questions can be answered with simple manual calculations – don't need @RISK for this



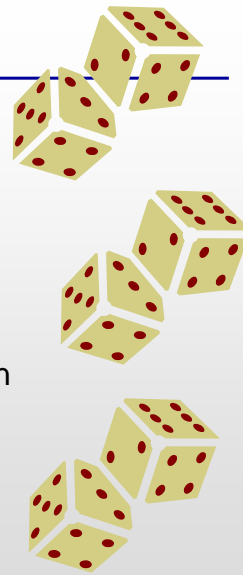
Outcomes of rolling two dice

- Range of values is 2 through 12
- Histogram of results



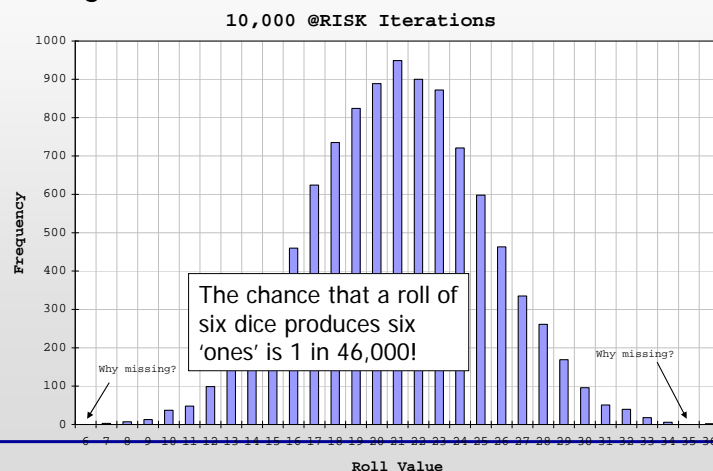
Let's Increase the Complexity

- Six dice, each with numbers 1 through 6
- Questions are the same
 - What are the possible combinations of numbers that can occur on any roll?
 - What is the frequency of occurrence of each number?
- No longer a simple, manual calculation
- We'll show how these models are set up in @RISK later



Outcomes of rolling six dice

- Range of values is 6 through 36
- Histogram of results



Extend Model Complexity

- Models are often very complex
 - Can involve many variables, not all of which are independent and/or linear in their behavior
 - Examples
 - Estimating fluids in place (gas PVT v Pres)
 - Decline curve analysis (decline curve parameters)
 - Reservoir modeling (porosity, permeability, thickness variations, vertical vs horizontal, lateral lengths, etc)
 - Economic analysis (costs, prices, drilling schedules, expectations for success, dry holes, etc)
-

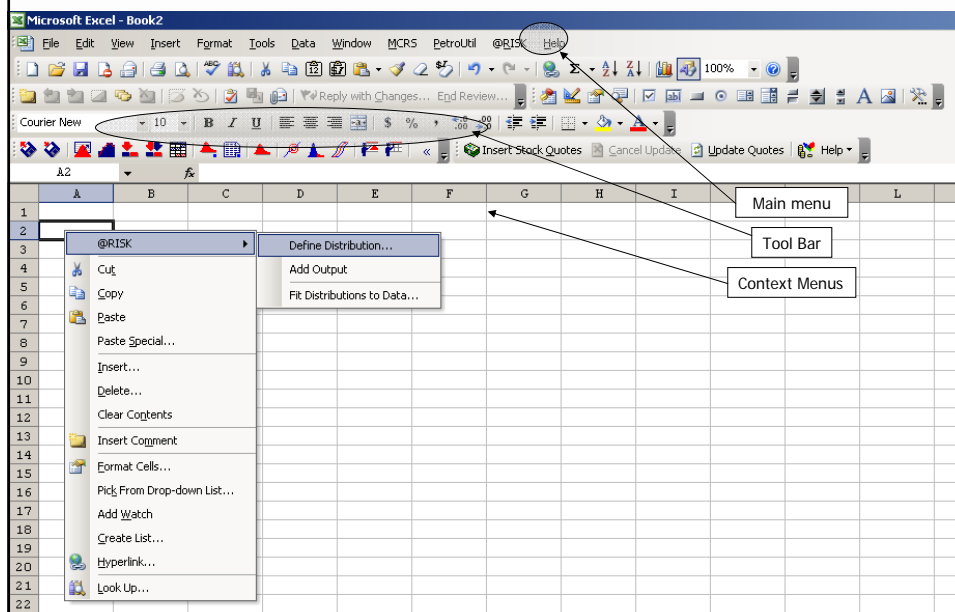
Getting Back to Why Use @RISK?

- When you want to take a *probabilistic* approach rather than a deterministic (or limited scenario) approach
 - When you want to understand how *uncertainty* in your inputs affects the outcome of your analysis
 - When you want to make decisions in the context of a *range* of possible outcomes (is this better?)
 - @RISK facilitates our ability to do all these things
-

Overview of Basic Features in @RISK

- **Primary functions** (what you'll do most often)
 - Inputs – getting data in using mathematical representations of distribution functions
 - Outputs – capturing, accessing, reviewing and graphing results
 - Settings – setting up the model iterations, sampling scheme, etc.
- **Secondary capabilities**
 - Calibrating (fitting) data to distribution functions
 - Correlation
 - Sensitivity analysis (tornado charts)
- **Integration with Excel** – powerful
 - Excel will be the most commonly used, day-to-day tool in your career
 - @RISK extends that into the probabilistic analysis/statistics realm

@RISK User Interface

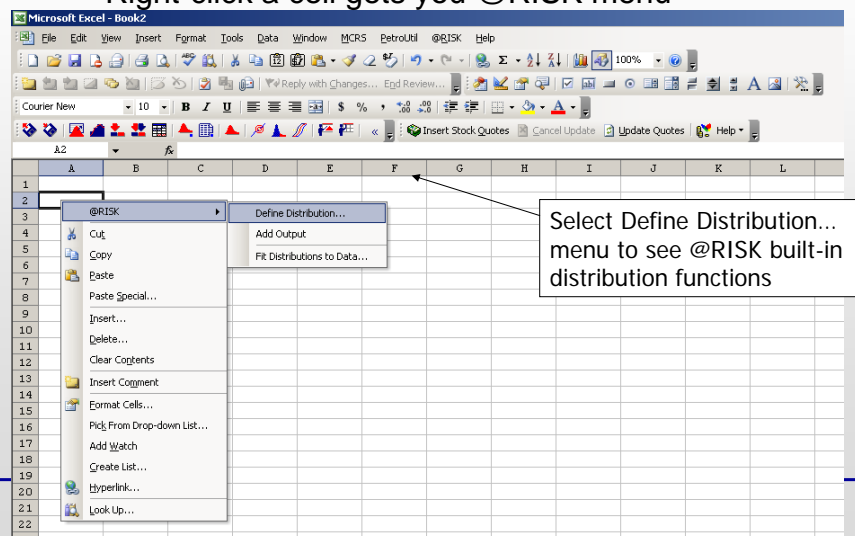


@RISK Input Functions

- Primary mechanism for data input is a collection of @RISK distribution functions
- Can be entered directly or use context menus to access them
- Can be used in a cell by themselves, or combined into any Excel cell formula

Accessing @RISK Distribution Functions

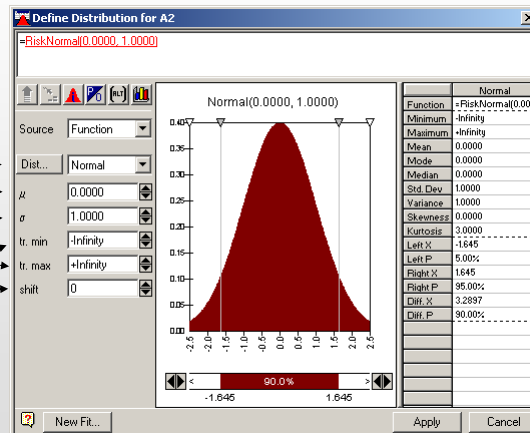
- Right-click a cell gets you @RISK menu



Accessing @RISK Distribution Functions

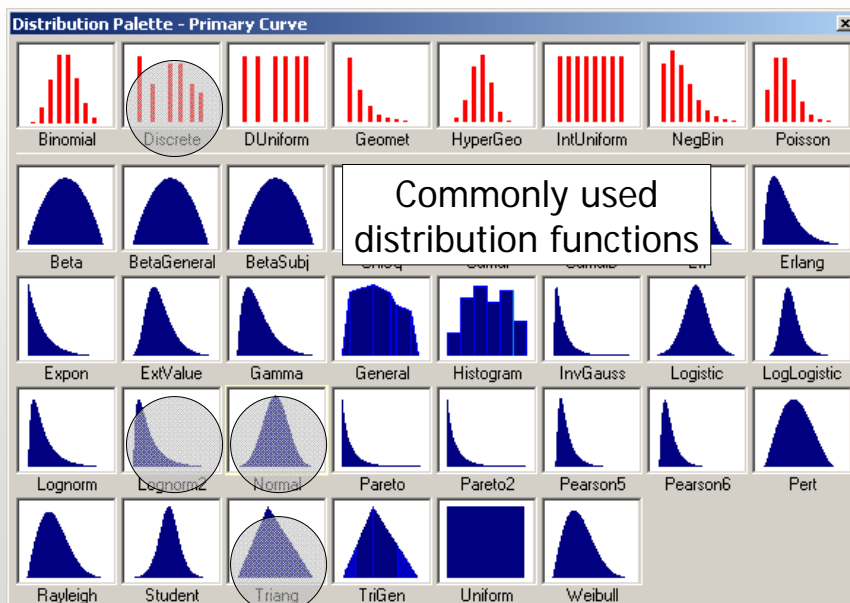
- @RISK Normal Distribution function

- User Inputs:
- Palette
- Mean*
- Std Dev*
- Boundaries
- Shift

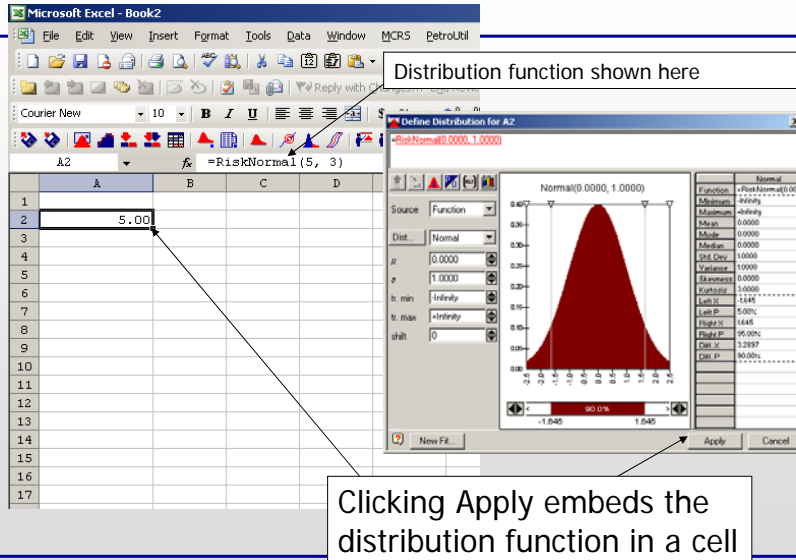


* - Most **distribution functions** are defined simply with a **mean** and a **standard deviation**

@RISK Distribution Functions Palette



@RISK Distribution Function in a Cell



@RISK Output Functions

- @RISK output function 'captures' any information in your spreadsheet model resulting from calculations in @RISK
- Use '=Riskoutput()+formula' syntax
- Can be a single cell reference or a formula that combines @RISK distribution values with other items in the spreadsheet

Example @RISK Model Showing Formulas

- Normal & log normal distributions
- Output is product of the two distributions

	A	B	C
1			
2	Net H	=RiskNormal(5, 3, RiskName(A2))	
3	Perm	=RiskLognorm(2.5, 2.5, RiskName(A3))	
4			
5	KH	=RiskOutput(A5)+B2*B3	
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			
16			

Example @RISK Model Showing Values

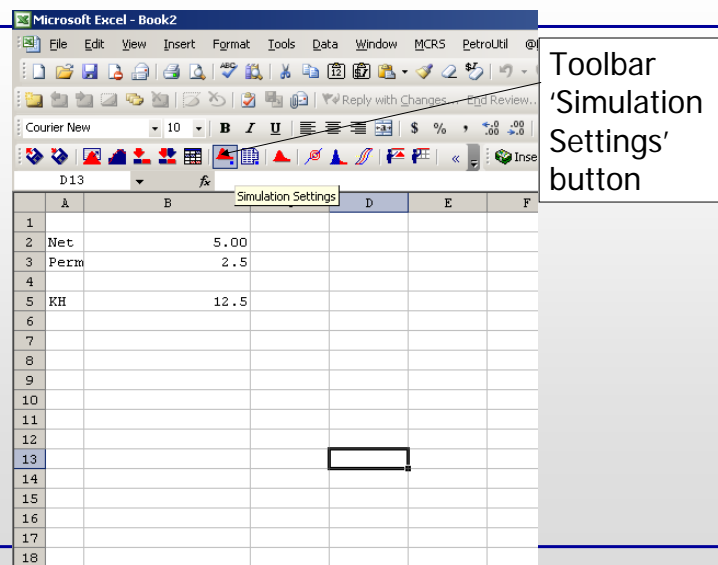
- Normal & log normal distributions
- Output is product of the two distributions

	A	B	C	D	E	F
1						
2	Net	5.00				
3	Perm	2.5				
4						
5	KH	12.5				
6						
7						
8						
9						
10						
11						
12						
13						
14						
15						
16						
17						

Running an @RISK Model

- What you need to know ahead of time
 - How many simulations?
 - How many iterations?
 - What type of sampling?
 - Running any macros with the model?
- Access settings via the main menu or the toolbar

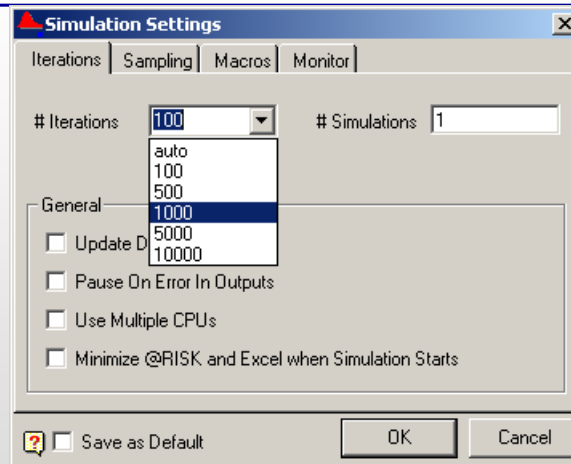
@RISK Model Settings



Toolbar 'Simulation Settings' button

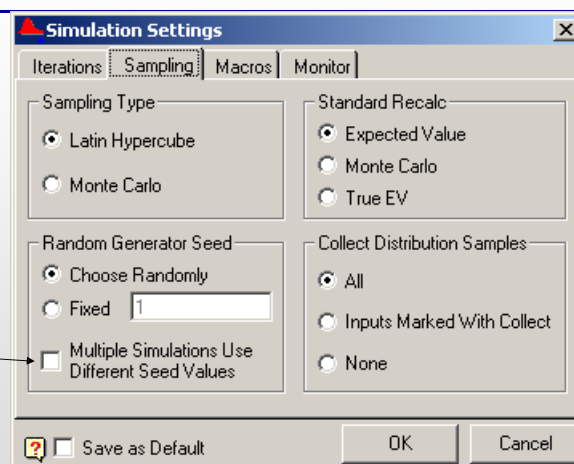
	A	B	D	E	F
1					
2	Net	5.00			
3	Perm	2.5			
4					
5	KH	12.5			
6					
7					
8					
9					
10					
11					
12					
13					
14					
15					
16					
17					
18					

@RISK Model Settings Dialog – Iterations Tab



@RISK Model Settings Dialog – Sampling Tab

Very important
consideration for
multiple
simulations



@RISK Model Settings Dialog – Macros Tab

The screenshot shows the 'Simulation Settings' dialog box with the 'Macros' tab selected. The dialog has four tabs: 'Iterations', 'Sampling', 'Macros', and 'Monitor'. The 'Macros' tab contains a section titled 'Run An Excel Macro' with four checkboxes and corresponding text input fields for 'Macro Name':

- ☐ Before Each Simulation
- ☐ Before Each Iteration's Recalc
- ☐ After Each Iteration's Recalc
- ☐ After Each Simulation

At the bottom of the dialog, there is a 'Save as Default' checkbox, an 'OK' button, and a 'Cancel' button.

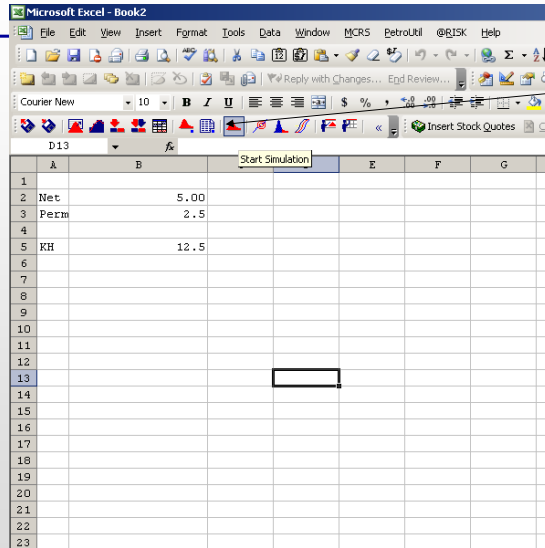
@RISK Model Settings Dialog – Monitor Tab

The screenshot shows the 'Simulation Settings' dialog box with the 'Monitor' tab selected. The dialog has four tabs: 'Iterations', 'Sampling', 'Macros', and 'Monitor'. The 'Monitor' tab contains a section titled '@RISK Results Window' with the following settings:

- 'Update Every' is set to '100' with a dropdown arrow, followed by the text 'Iterations'.
- ☐ Update Real Time
- ☐ Monitor Convergence

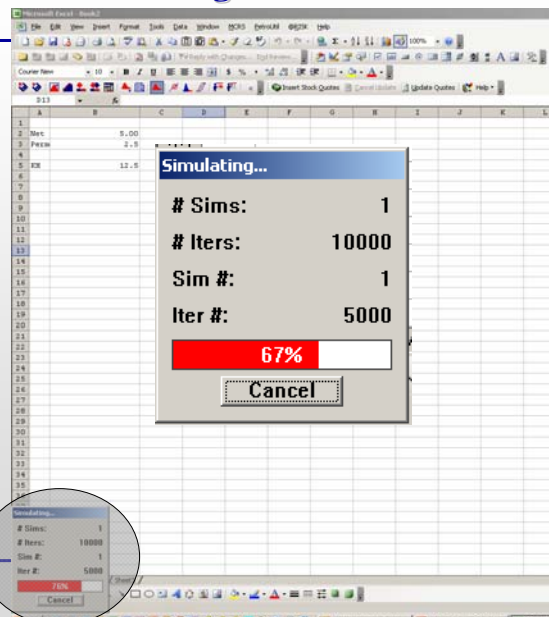
At the bottom of the dialog, there is a 'Save as Default' checkbox, an 'OK' button, and a 'Cancel' button.

@RISK Model Run Simulation

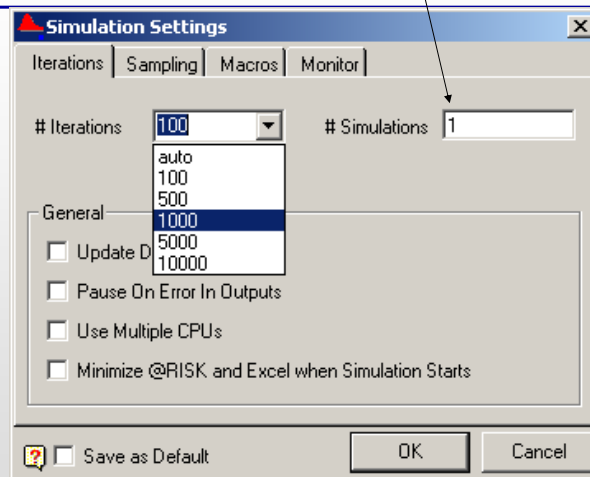


Toolbar
'Start
Simulation'
button

@RISK Model Running



Multiple Simulations – what's meant here?



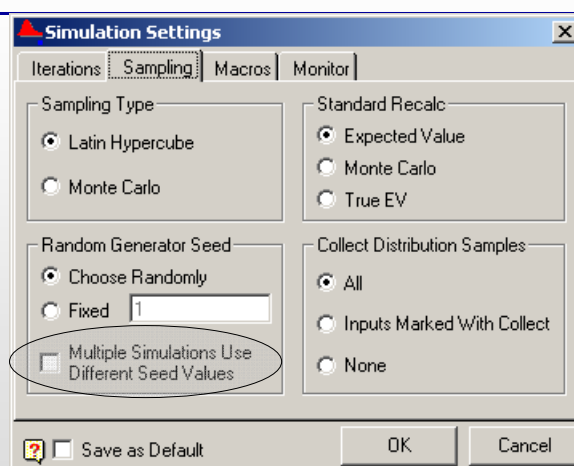
Multiple Simulations - Explained

- A single @RISK simulation might involve many iterations (hundreds or thousands), with each iteration sampling from input distribution functions
- Sometimes, you might want to vary some part of your model with multiple, discrete values and associate that with a full set of Monte Carlo iterations

Multiple Simulations - Examples

- You have set up a Monte Carlo economics model, and you want to run a Monte Carlo simulation for each of 5 different gas prices – that is 5 simulations
 - You have set up a horizontal well model, and you want to explore the performance of 3 separate lateral lengths using Monte Carlo simulation – that is 3 simulations
-

Multiple Simulations and the Fixed Seed



Multiple Simulations – Why a Fixed seed?

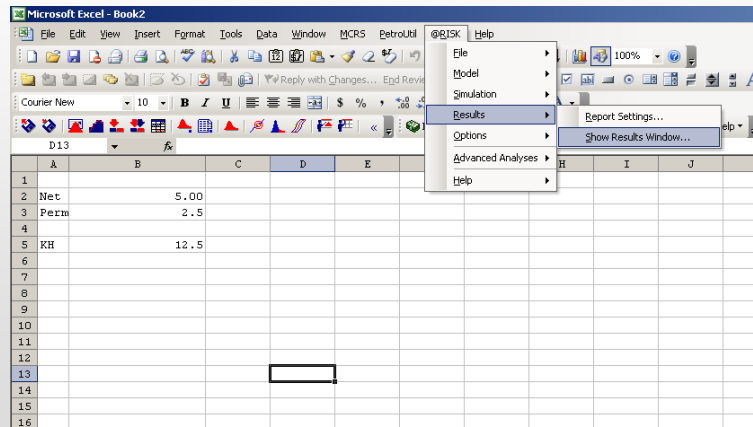
- If you are running multiple simulations, you might consider a fixed seed
 - With a fixed seed for all simulations, the same sampling sequence is used for all simulations
 - This keeps the values of sampled parameters the same across multiple simulations, ensuring consistency when running multiple simulations and comparing results
-

Getting Results from an @RISK Model

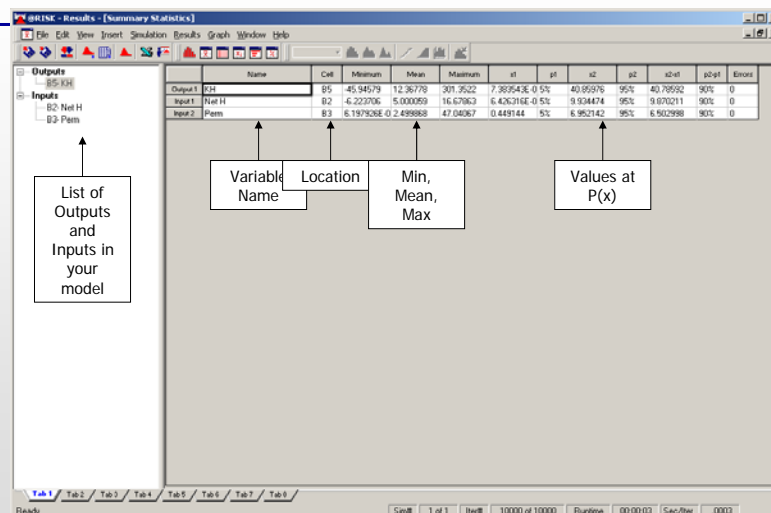
- Once all simulations and iterations are complete, you can
 - Check the descriptive statistics related to both your inputs and outputs
 - Show the results graphically
 - ‘Speak’ probabilistically
-

Getting Results from an @RISK Model

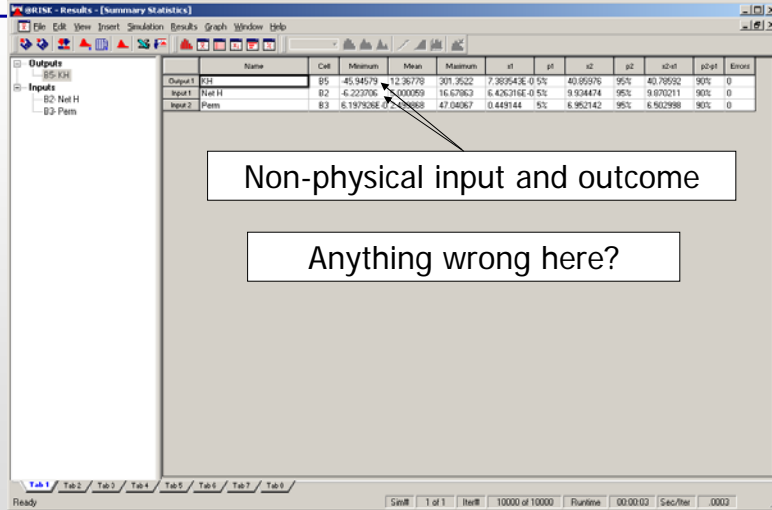
- Accessing the results window



@RISK Results Window



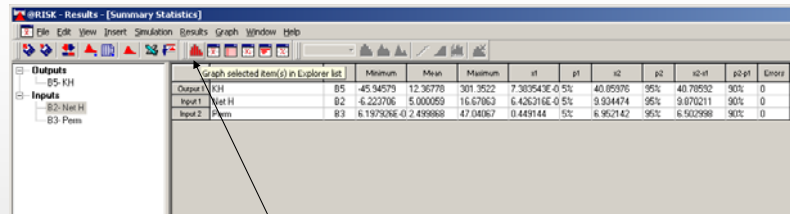
@RISK Results Window



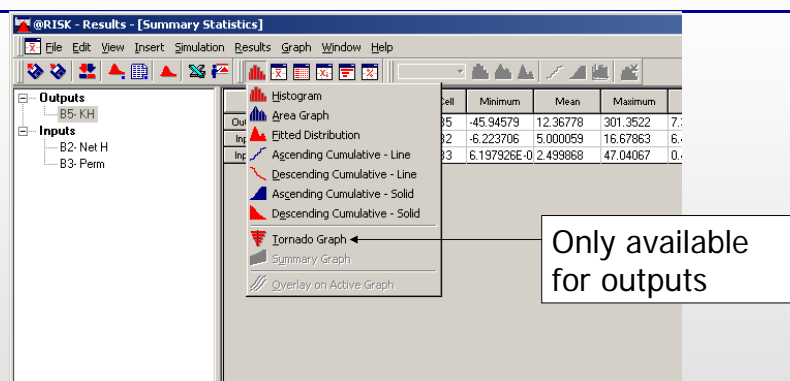
@RISK Results – Graphical Options

- Various options available for any input parameter or output variable
 - Histogram
 - CDFs
- For outputs
 - Tornado plots

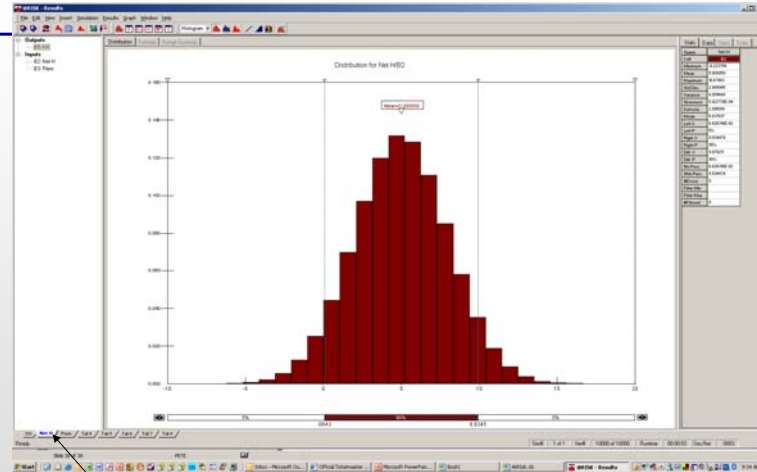
@RISK Results – Accessing Results Graphically



@RISK Results – Graph Selections

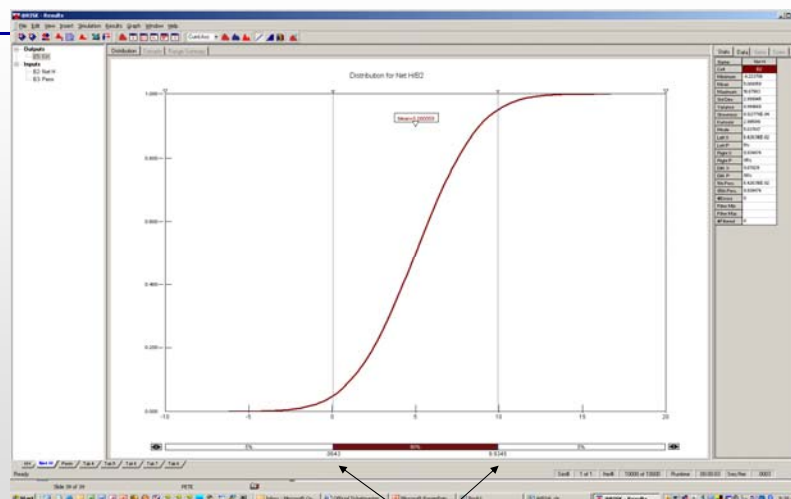


@RISK Results – Histogram



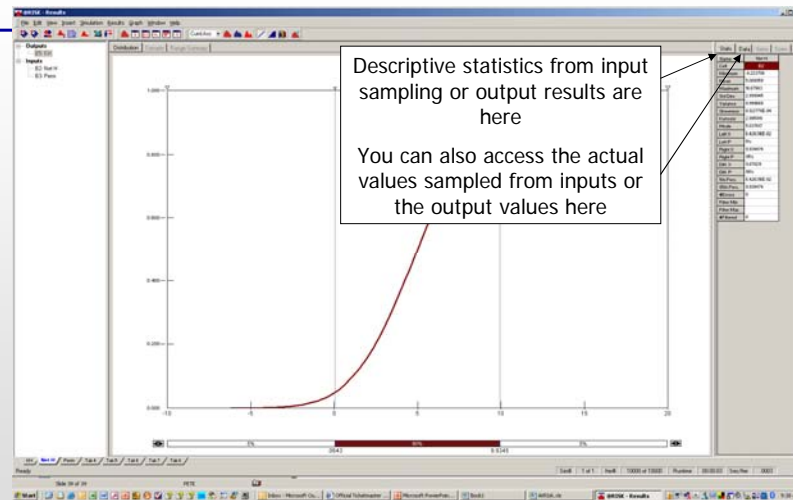
Tabs let you save different presentations of information

@RISK Results – CDF



Information about ranges here

@RISK Results – Stats and Data



@RISK Results – Stats and Data Closeup

STATS	
Stats	Data
Name	Net H
Cell	B2
Minimum	-6.223706
Mean	5.000059
Maximum	16.67863
Std Dev	2.999945
Variance	8.999668
Skewness	8.122778E-04
Kurtosis	2.996919
Mode	5.037617
Left X	6.426316E-02
Left P	5%
Right X	9.934474
Right P	95%
Diff. X	9.870211
Diff. P	90%
5th Perc.	6.426316E-02
95th Perc.	9.934474
#Errors	0
Filter Min	
Filter Max	
#Filtered	0

DATA	
Stats	Data
Name	Net H
Description	mal(5, 3, RiskNa
Iter#	Cell
1	4.44958
2	2.93671
3	2.60324
4	6.77080
5	5.02756
6	0.78939
7	4.12282
8	6.97593
9	3.47701
10	5.32403
11	3.04444
12	8.46586
13	3.26973
14	7.13687
15	5.27725
16	0.75995
17	7.49261

Let's Review @RISK Basic Features

- Model inputs via **distribution functions**
 - Used alone or combined in formulas with other information or inputs
 - '**RISKOUTPUT**' **function** used to capture desired results
 - Results viewed in @RISK results window – actual values or graphical presentation
-

@RISK More Advanced Features

- Calibration of functions to data (Pro version or higher)
 - Correlation of inputs
 - Sensitivity analysis (tornado charts)
-

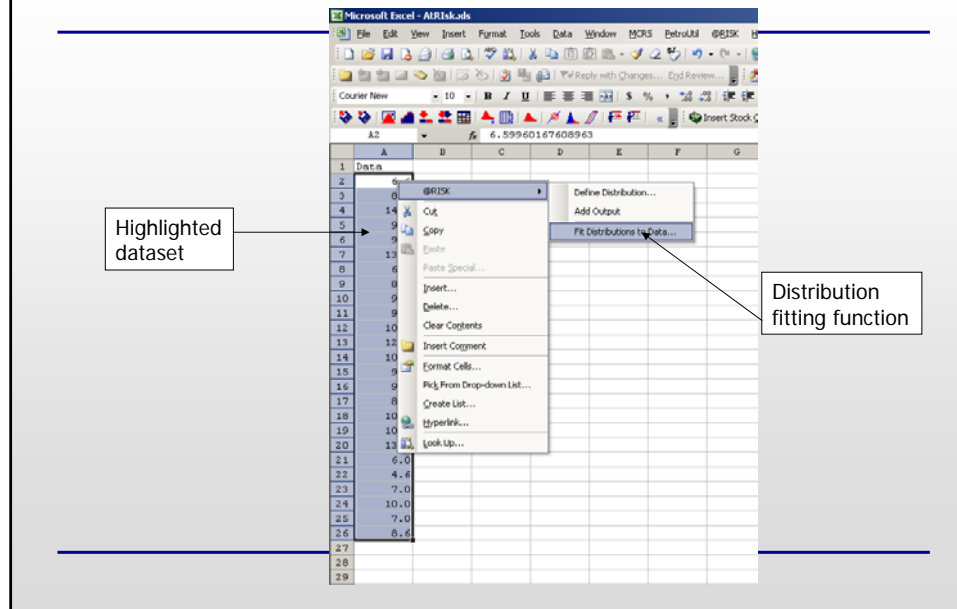
@RISK Calibration to Data

- Automatic curve fitting of distribution functions to actual data
 - Then, access to curve fits during model construction
 - Converts a discrete data set (with possibly a limited number of points) into a continuous distribution of values
-

@RISK Calibration to Data - Example

- Dataset has 25 data points
 - Highlight data
 - Use context menus to select “Fit Distributions to Data...”
 - @RISK automatically fits as many distributions as possible to the data and ranks them according to goodness of fit
-

@RISK Calibration to Data – Getting Started



@RISK Calibration to Data – Input Dialog

@RISK - Fit Excel Data

Fit Tab Name: Fit2

Excel Data Range: [AtRisk.xls]Sheet2!\$A\$2:\$A\$26

Type Of Data:

- ☒ Sampled Values
- ☐ Density Curve
- ☐ Cumulative Curve

Domain:

- ☒ Continuous
- ☐ Discrete (Integral Domain)

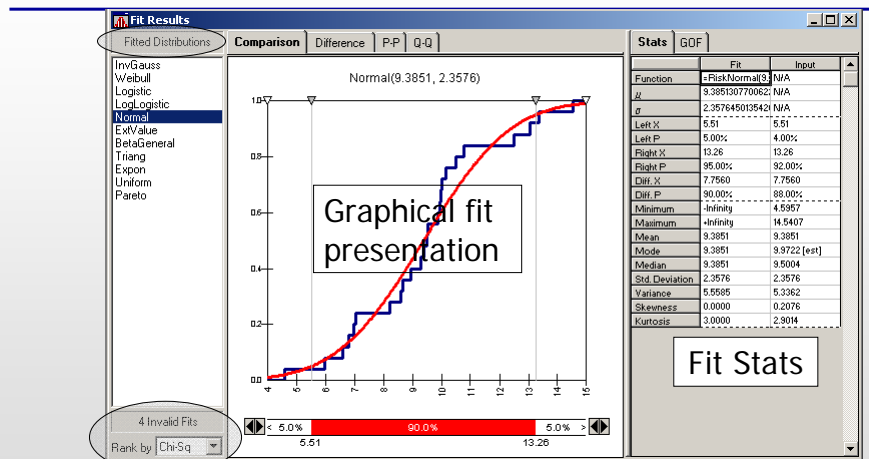
Filtering Options:

- ☒ No Filtering
- ☐ Filter Data Outside Range: Xmin: [] to Xmax: []
- ☐ Filter Data that Falls [1] Standard Deviations Beyond the Mean

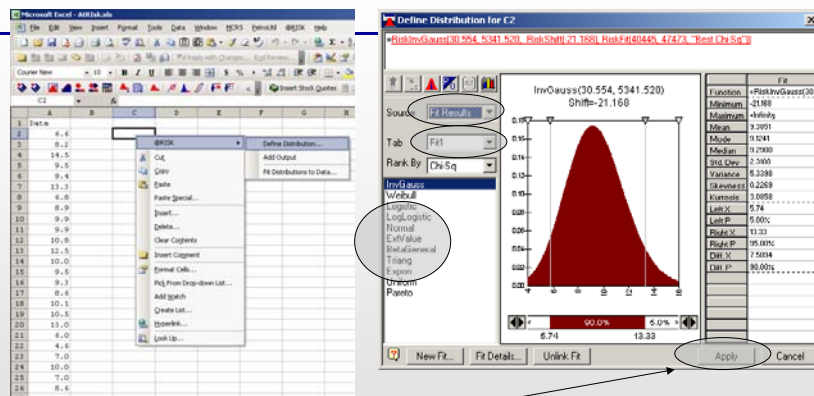
☐ Automatically Refit When Input Data Changes

OK Cancel

@RISK Calibration to Data – Fit Results



@RISK Calibration to Data – Using Fits



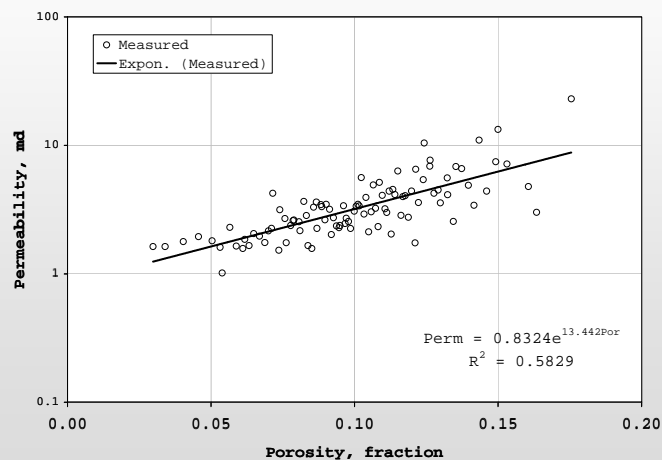
Clicking Apply embeds your fitted distribution curve into the Excel worksheet

@RISK Correlation Capability

- By default, the underlying assumption in @RISK is that INPUT parameters are sampled as completely independent events
- Each input is sampled independently of every other input
- However, there are times when input parameters are in fact correlated, and this needs to be taken into account in the model

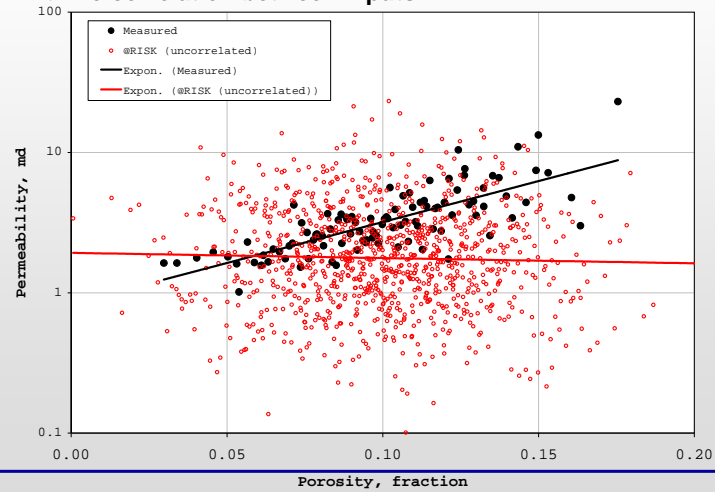
@RISK Correlation Capability - Example

- 100 samples of core permeability and porosity measurements – correlation is clear



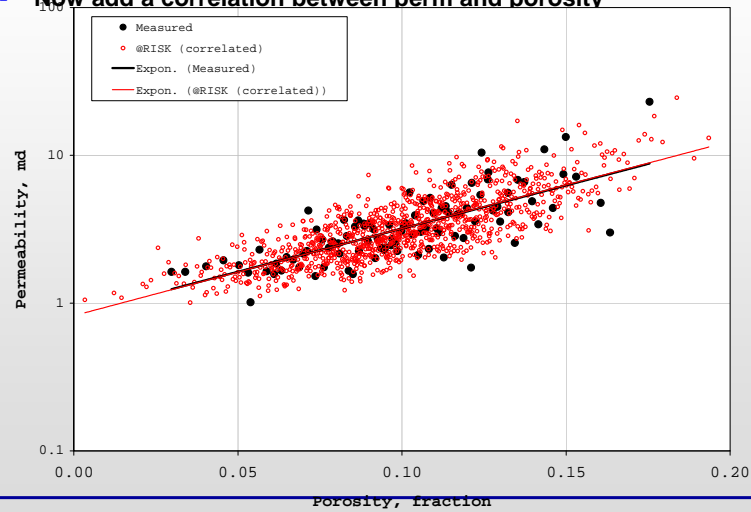
Model data using @RISK without correlation

- Fit porosity and perm data using @RISK, and then run a model with no correlation between inputs



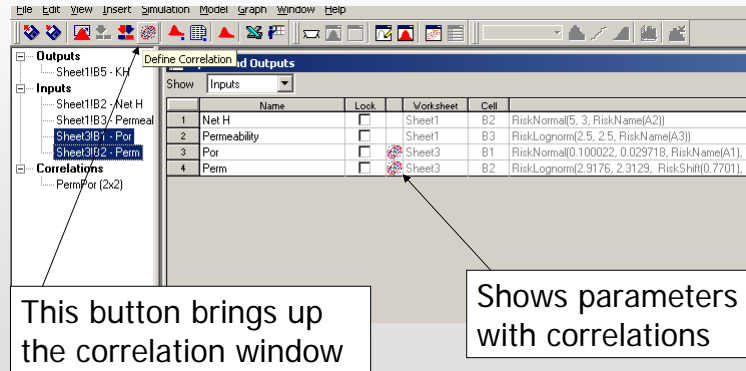
Model data using @RISK with correlation

- Now add a correlation between perm and porosity



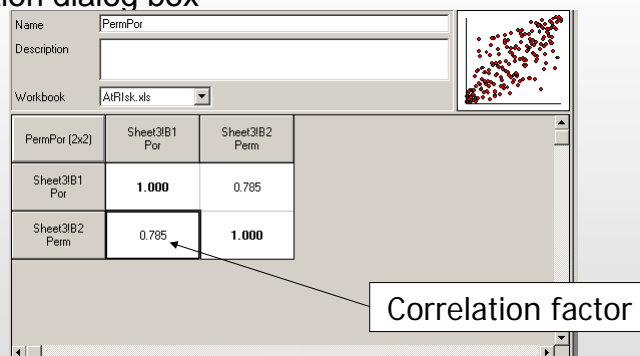
Using the @RISK Correlation Function

- Found in the @RISK model window



Using the @RISK Correlation Function

- Correlation dialog box



@RISK Sensitivity Analysis – Tornado Charts

- Evaluates the relative impact of any input parameter on any output variable
 - Automatically generated with each Monte Carlo simulation
 - Helpful to understand which input parameters most greatly affect outputs and how they affect outputs (directionally)
-

@RISK Sensitivity Analysis – Example

- Make a probabilistic gas in place estimate and understand the relative impact of each input

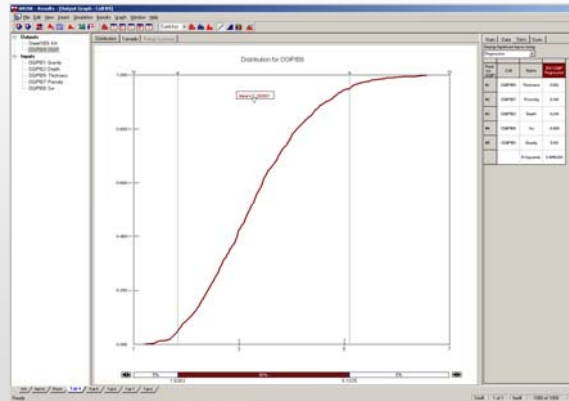
Parameter	Min	Most Likely	Max
Gravity (air=1)	0.63	0.65	0.66
Depth, ft	2,500	3,000	3,500
Thickness, ft	5	10	20
Porosity, %	10	15	17
Sw, %	20	25	30

Assumptions:

1) Pore pressure gradient= 0.433 psi/ft

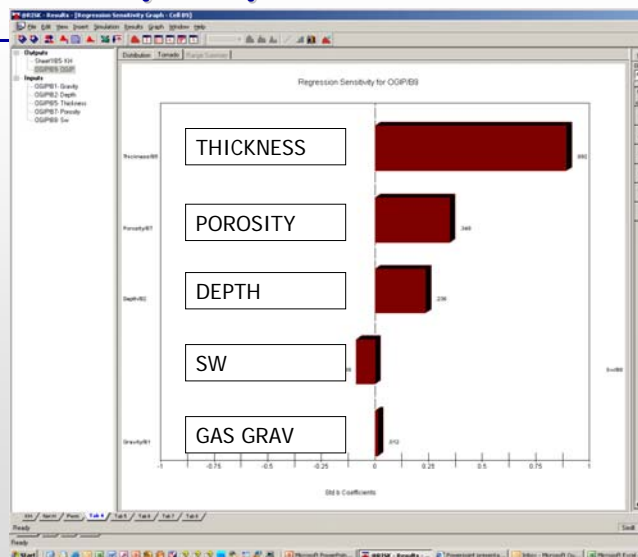
2) Temperature gradient= 1.0 deg F per 100 ft of depth + 75 deg

@RISK Sensitivity Analysis – OGIP CDF



- Avg OGIP= 3.29 Bscf/sec
- 90% of values fall between 1.8 and 5.1 Bscf/sec

@RISK Sensitivity Analysis – OGIP Tornado



Model Construction – Tips & Tricks

- Model construction can be very flexible
 - Because of integration with Excel, there is almost no limit to what you can do
 - This is also a reason to be cautious!
-

Model Construction – Tips & Tricks

- Test, test and test your inputs
 - look for and eliminate physically unrealistic values
 - Compare your inputs to available or analogous data as a check
 - Check for correlations
 - Cross-plot inputs against inputs looking for possible correlations between input parameters that need to be included in the model
-

Model Construction – Tips & Tricks

- Use the simplest, most common distribution function(s) possible for your model's inputs
 - Triangular
 - Normal
 - Log normal
 - If you have fitted distribution functions, always check the fitted results against your raw data – particularly, beware of fitted results in the area outside the range of your input data
-

Model Construction – Tips & Tricks

- During model development and testing, limit the iterations to a few (10?) to speed up your testing phase
 - Do you need to reproduce results in the future?
 - Why is this important?
 - How? use a fixed seed for consistent testing and results
 - Not always necessary
-

Model Construction – Discrete Events

- Examples of discrete or random events
 - Infrequent, but possible, dry holes
 - Not encountering a particular zone in a multi-zone completion
 - Wellbore mechanical failures
 - Usually an ‘either or’ situation
 - Often handled with a simple ‘0 or 1’ type of model
-

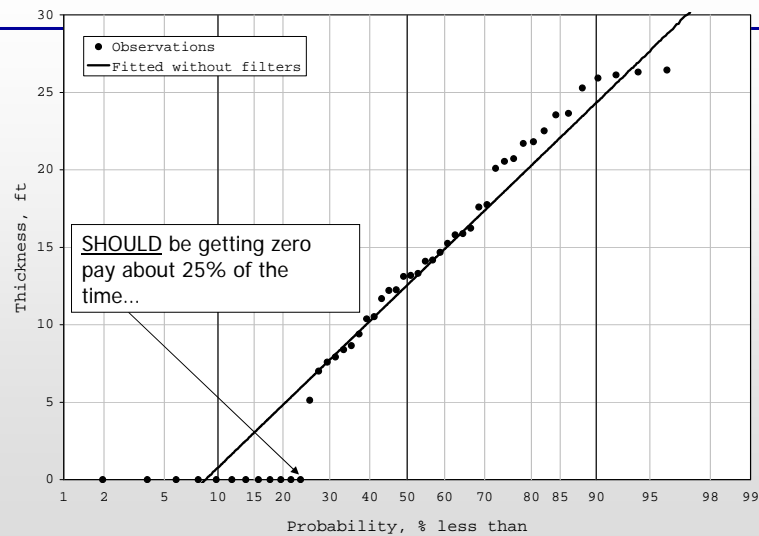
Discrete events example

- Distribution of net pay
 - 50 data points
 - 12 values are zero because pay was not encountered
 - Leaves 38 non-zero pay values
 - You want to fit a distribution function to all this data, including the non-zero entries
 - The difficulty is the non-smooth nature of the data due to the zero-pay values (introduces sort of a discontinuity)
-

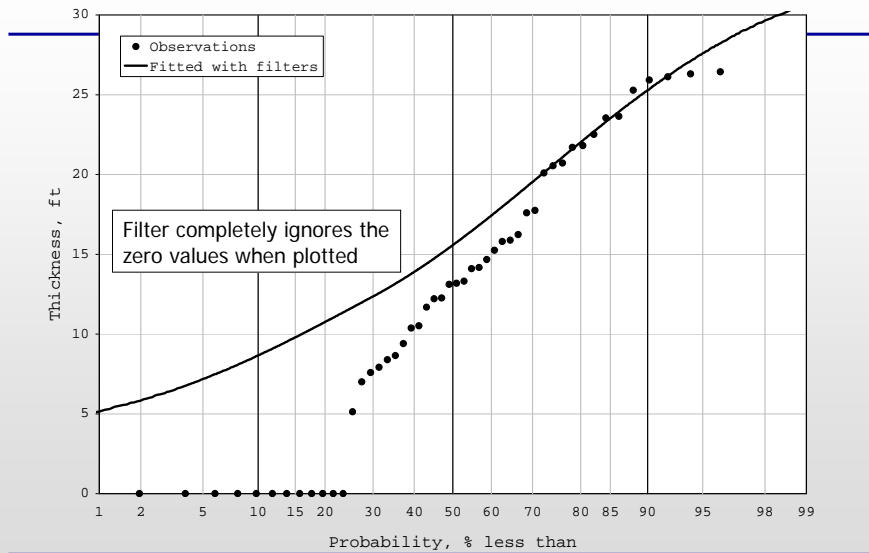
Discrete events example – Options for Handling

- Ignore it – not likely, but we'll show it anyway!
- Could use @RISK built-in data filtering during the fitting process – but that leaves out the probability of getting no pay
- Could split into two distributions
 - One to match the non-zero data
 - One to represent the probability of encountering zero pay
 - Final net pay is combination of two distribution functions

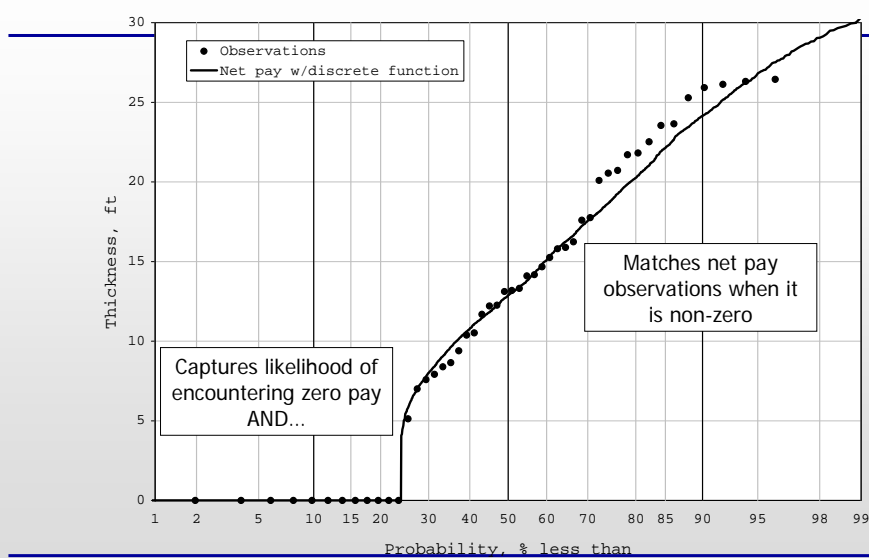
Discrete events example – Ignore it?



Discrete events example – Filter it?



Discrete events example – Split it



Discrete events example – @RISK model

- Our original dataset had 12 out of 50 values equal to zero
 - Use **RiskDiscrete** function to model frequency of occurrence
 - =RiskDiscrete({0,1}, {12,38})**
 - Note that it only takes on one of two values: 0 or 1
 - The 12 and 38 establish the frequency with which each value occurs, regardless of the number of iterations run in the simulation
- For non-zero pay, use @RISK distribution fitting on non-zero data only
- Final net pay is product of discrete function and non-zero distribution

	A	B
1	NonZero?	=RiskDiscrete({0,1}, {12,38}, RiskName("PayPresent"))
2	Pay	=RiskTriang(3.6224, 12.256, 33.113, RiskName("NonZeroPay"))
3	Final Pay	=RiskOutput("FinalPay") + B2 * B1
4		

Examples Using @RISK from Mian

- See Mian, pages 355-366 for details on using @RISK for this **reserves simulation example**
- See Mian, Example 6-3, pages 366-369 for details on using @RISK for **NPV example**
- See Mian, pages 370-373, for details on **modeling dependency** in @RISK
- See Mian, pages 373-375, for information on **combining @RISK and PRECISIONTREE**

Your assignment

- Download the paper on Risk Analysis pp.14-23 under the topic “**Decision Tree vs. Monte Carlo Simulation**” and “**When does correlation matter?**”.
 - Construct the decision tree (using PrecisionTree program) and building simulation model (using @RISK) as suggested in the examples.
 - Select one example for your presentation either **the reserve example** or the alternative mud systems.
 - Find out and explain what is the different between the two methods from your case.
-