

### Econometrics: Homework 5

1) Suppose the true relationship is  $Y = \beta_2 Z$ . However, we cannot measure  $Z$ . We can only measure  $X = Z + w$ .  $w$  is a measurement error and  $E[w] = 0$ . We want to estimate  $\beta_2$  with  $b_2 = \frac{Y_1}{X_1}$ .  $(Y_1, X_1)$  is a sample of  $X$  and  $Y$ . Is  $b_2$  biased?

2) Suppose the true relationship is  $Q = \beta_2 X$ . However, we cannot measure  $Q$ . We can only measure  $Y = Q + w$ .  $w$  is a measurement error and  $E[w] = 0$ . We want to estimate  $\beta_2$  with  $b_2 = \frac{Y_1}{X_1}$ .  $(Y_1, X_1)$  is a sample of  $X$  and  $Y$ . Is  $b_2$  biased?

3) In a certain industry, firms relate their stocks of finished goods,  $Y$ , to their expected annual sales,  $X_e$ , according to a linear relationship

$$Y = \beta_1 + \beta_2 X_e$$

Actual sales,  $X$ , differ from expected sales by a random quantity  $u$ , that is distributed with mean 0 and constant variance:

$$X = X_e + u$$

$u$  is distributed independently of  $X_e$ . An investigator has data on  $Y$  and  $X$  (but not on  $X_e$ ) for a cross-section of firms in the industry. Describe the problems that would be encountered if a least square estimator were used to estimate  $\beta_2$ .

4) You want to estimate the model

$$Y = a + b \cdot X1 + c \cdot X2.$$

Use the data set to produce the following results:

- Graphs of scatter plot between  $Y$ - $X1$  and  $Y$ - $X2$ . Is there the heteroscedasticity exists in the data? Why?
- Do the Park Test. Is there the heteroscedasticity exists in the data? Why?
- Do the White Test. Is there the heteroscedasticity exists in the data? Why?
- Estimate the model by applying White Heteroskedasticity Consistent Coefficient Covariance.