Rheology
and
Polymer Characterization

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http://pioneer.netserv.chula.ac.th/~sanongn1/course.html

Fundamentals:

- Why Rheology ?
- Fundamental Rheology Concepts and Parameters
- Fundamental Rheometry Concepts
- Viscosity, Viscoelasticiy and the Storage Modulus
- The Linear Viscoelastic Region (LVR)

AGENDA

- Why Rheology ?
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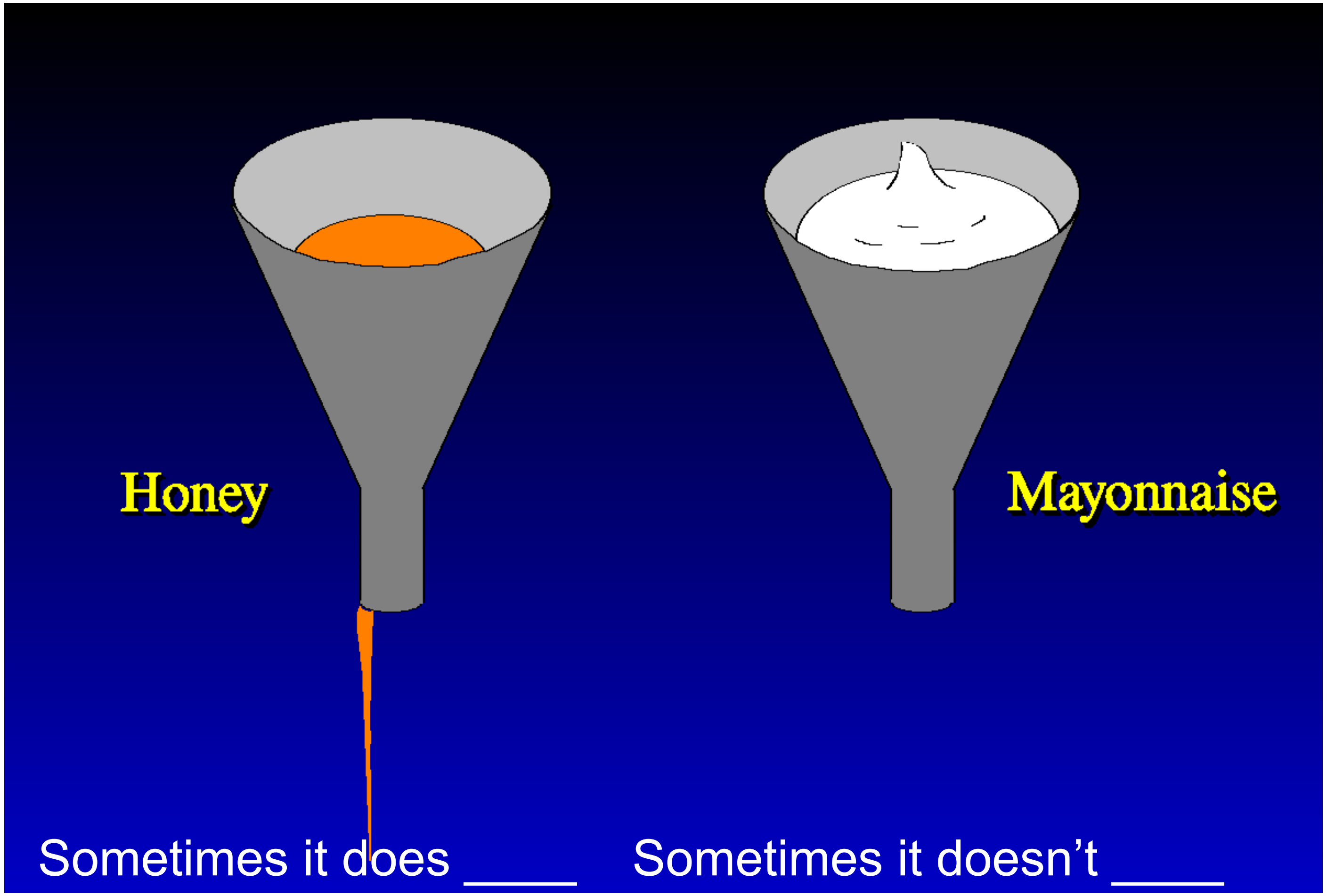
A Rheological Paradox



BECAUSE …

If a material is pumped, sprayed, extended, extruded, molded, coated, mixed, chewed, swallowed, rubbed, transported, stored, heated, cooled, aged …

RHEOLOGY is important ….!!

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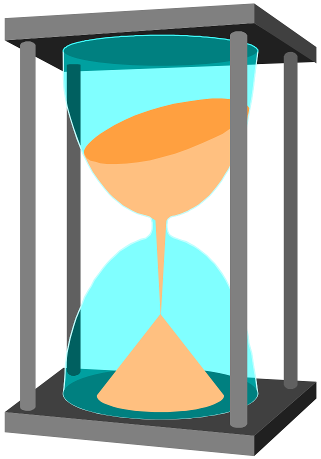
“παντα ρει” *(everything flows ...)*

- *Heraclito de Samos (500 A.C.)*



Time Scale in Rheology

Deborah Number $\mathbf{De = \lambda / t_{exp}}$

Judges 5:5

Definition of Rheology

Rheology is the science of

_______?_______ and _______?_______

of matter under controlled testing conditions .

- *flow*
- *deformation*

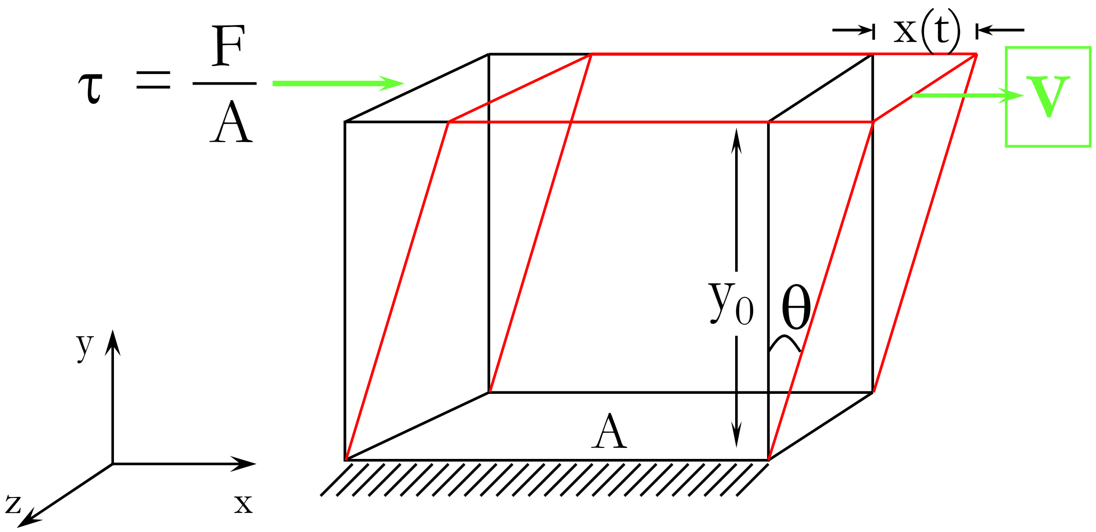
Definition of Rheology

Rheology is the science of *deformation* and *flow* of matter under controlled testing conditions .

- *Flow is a special case of deformation*
- *Deformation is a special case of flow*

Simple Shear Deformation and Shear Flow

Shear Deformation



$$\text{Strain, } \gamma = \frac{x(t)}{y_0}$$

$$\text{Strain Rate, } \dot{\gamma} = \frac{\mathbf{V}}{y_0} = \frac{1}{y_0}\frac{\mathbf{d}\, x(t)}{\mathbf{d\,t}}$$

$$\textbf{Viscosity, } \eta = \frac{\tau}{\dot{\gamma}}$$

$$\dot{\gamma} = \frac{\Delta\gamma}{\Delta t}$$

$$\textbf{Shear Modulus, } \mathbf{G} = \frac{\tau}{\gamma}$$

Range of Rheological Material Behavior

- Rheology: The study of deformation and flow of matter *at specified conditions*.

<u>Range of material behavior</u>

Solid Like ---------- *Liquid Like*

(Ideal Solid ------------- Ideal Fluid)

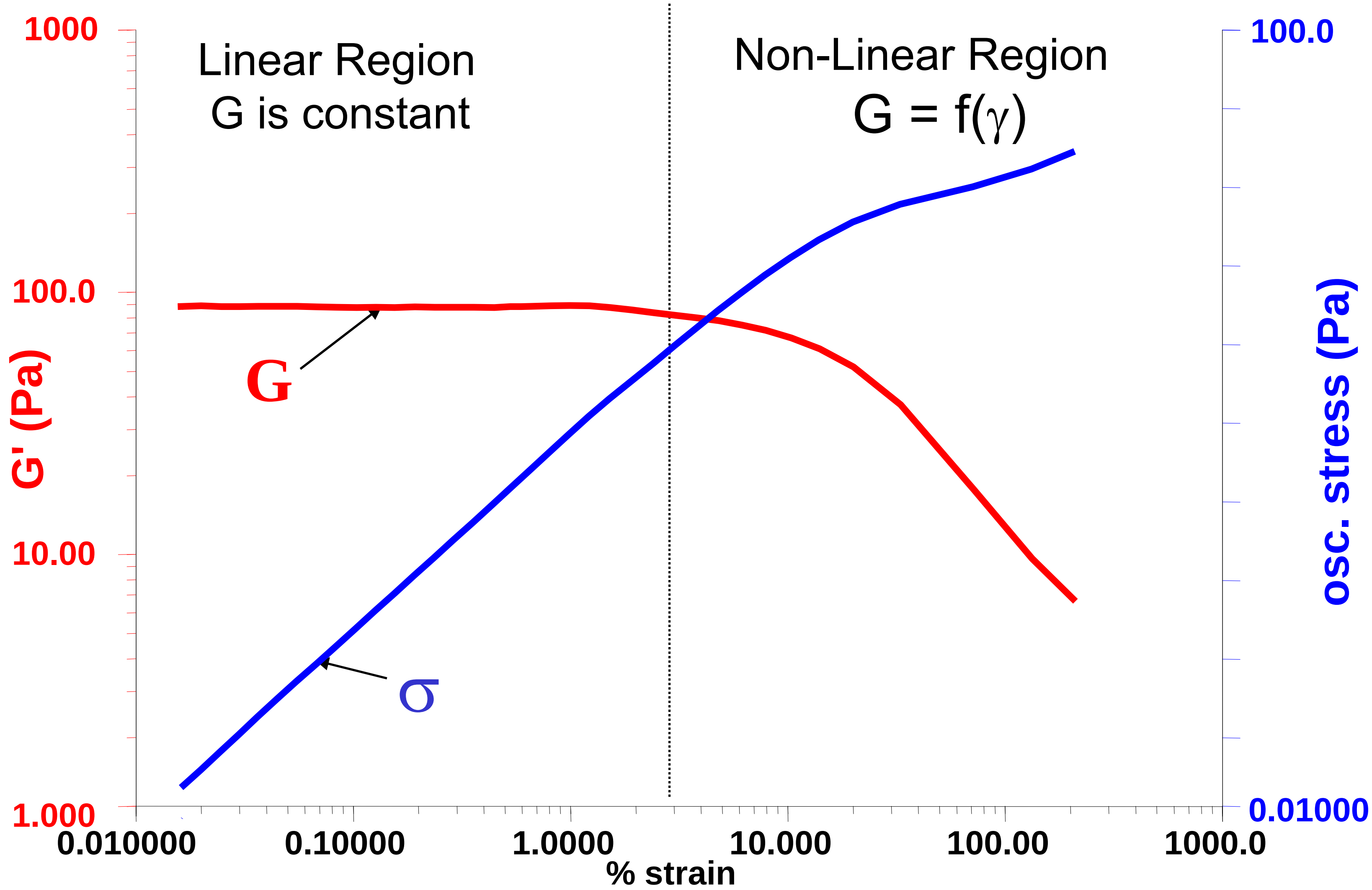
Classical Extremes

Classical Extremes: Elasticity

- 1678: Robert Hooke develops his "True Theory of Elasticity"
  - "The power of any spring is in the same proportion with the tension thereof."
  - Hooke's Law: $\tau = G\,\gamma$ or (Stress = G x Strain)

where G is the RIGIDITY MODULUS

Linear and Non-Linear Stress-Strain
Behavior of Solids



Classical Extremes: Viscosity

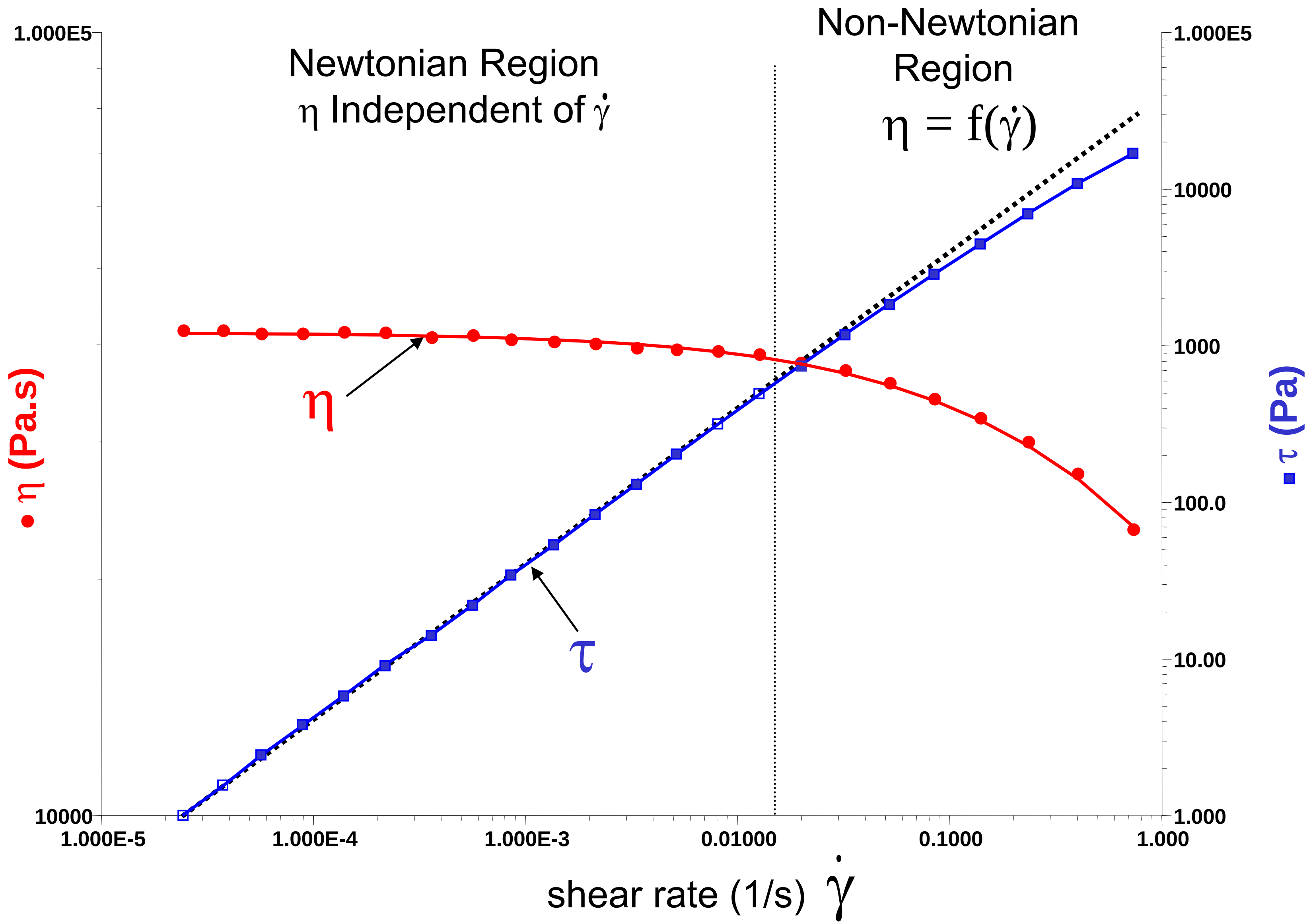
- 1687: Isaac Newton addresses liquids and steady simple shearing flow in his "*Principia*"

  - "The resistance which arises from the lack of slipperiness of the parts of the liquid, other things being equal, is proportional to the velocity with which the parts of the liquid are separated from one another."

  - Newton's Law: $\tau = \eta\dot{\gamma}$

where η is the Coefficient of Viscosity

Newtonian and Non-Newtonian Behavior of Fluids



PARAMETERS for Rheological Properties

Classical Extremes

Ideal Solid	-- [External Force] --	Ideal Fluid
STEEL		**WATER**
Strong Structure		**Weak Structure**
Rigidity		**Fluidity**
Deformation		***Flow***
Retains/recovers form		**Losses form**
Stores Energy		**Dissipates Energy**
(Purely Elastic – R. Hooke, 1678)	*[Energy]*	*(Purely Viscous – I. Newton, 1687)*
ELASTICITY		**VISCOSITY**
Storage Modulus		**Loss Modulus**

REAL Behavior

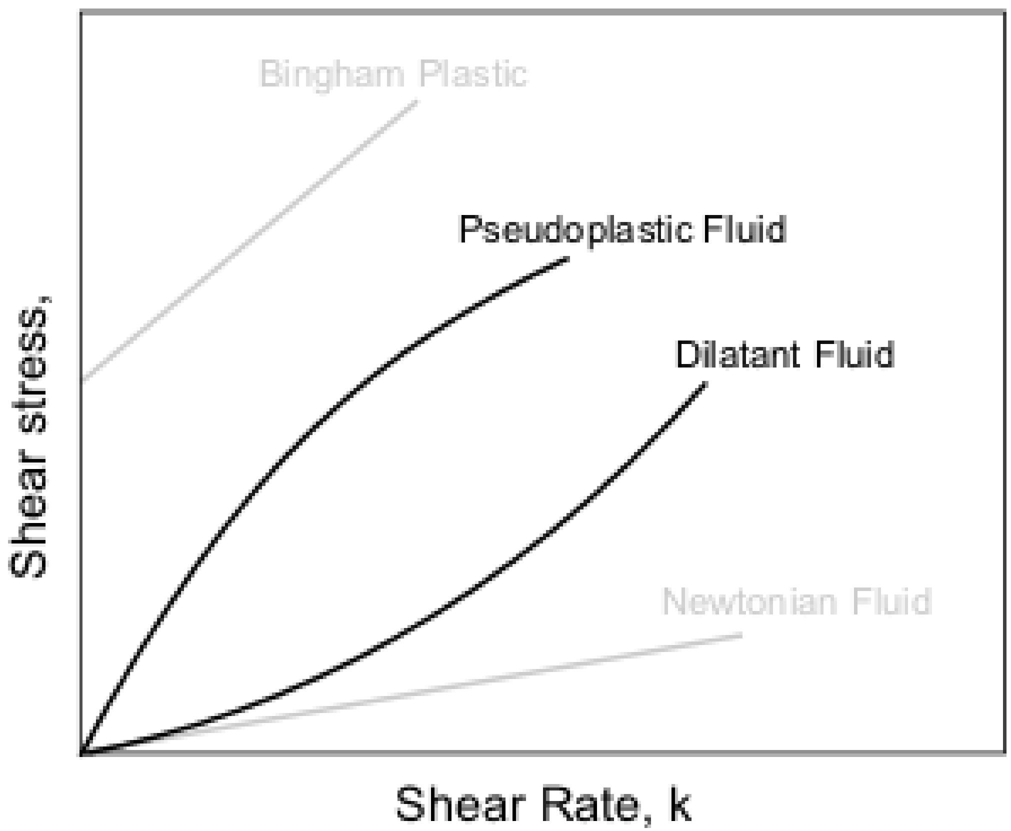
Apparent Solid	*[Energy + time]*	*Apparent Fluid*

- viscoelastic materials -

Types of non-Newtonian fluids

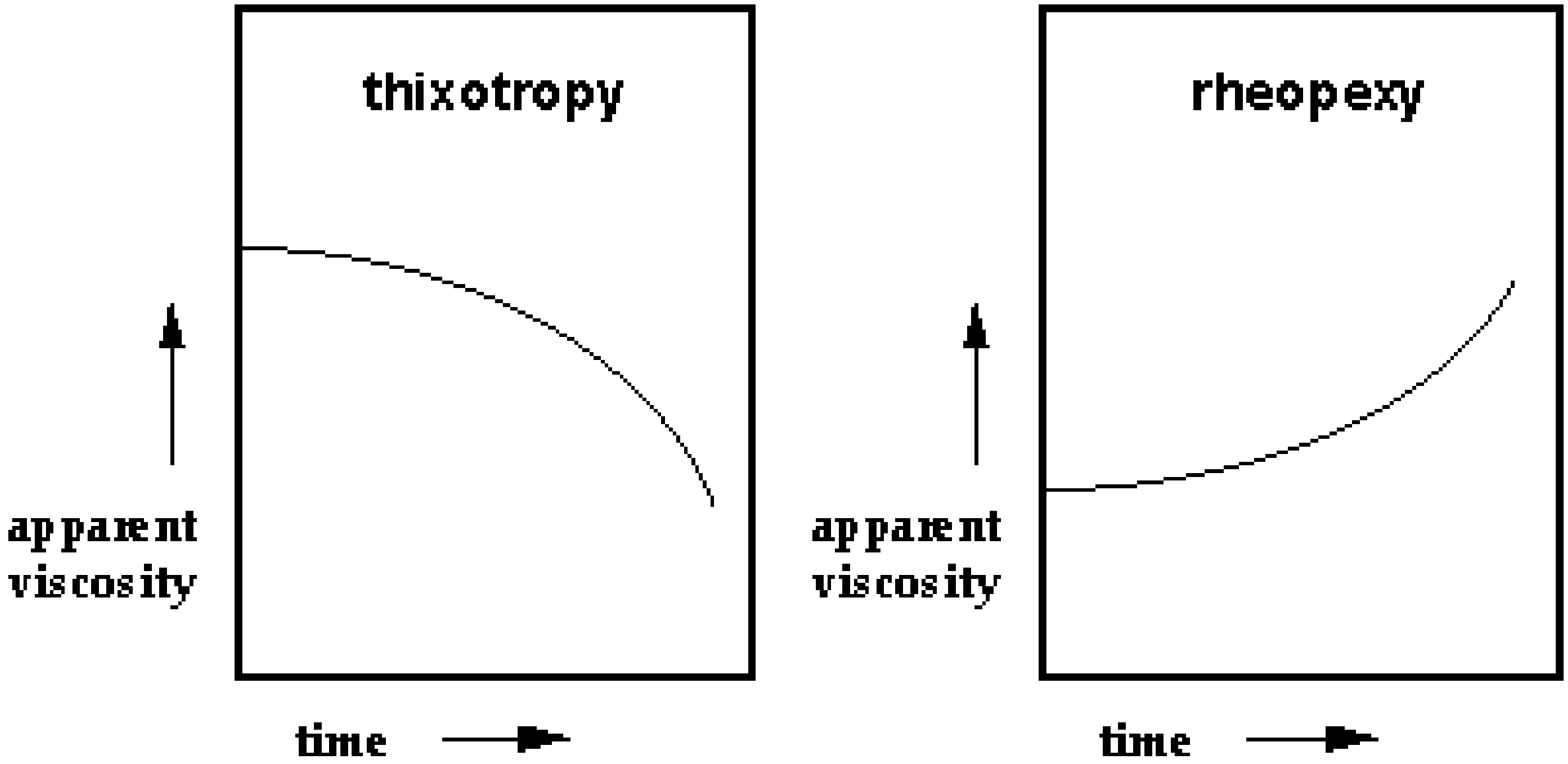
- Deformation rate dependent viscosity
- Yield Stress (plasticity)
- Elasticity
- Thixotropy
- Transient behaviour

Stress-strain rate curve



Dilatancy (shear thickening)
Plastic and Pseudoplastic (shear thinning)

apparent viscosity as a function of time



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Viscometer vs. Rheometer

- **Viscometer:** instrument that measures the viscosity of a fluid over a limited shear rate range

- **Rheometer**: instrument that measures:
  - *Viscosity over a wide range of shear rates, and…*
  - *Viscoelasticity of fluids, semi-solids and solids*

Frame of Reference…

- Recognize that a rheometer is a highly sensitive device used to quantify viscoelastic properties of the ***molecular structure*** of materials.

- A rheometer can not always mimic the conditions of a process, application or use.

- Rheometers determine apparent properties under a wide range of testing conditions.

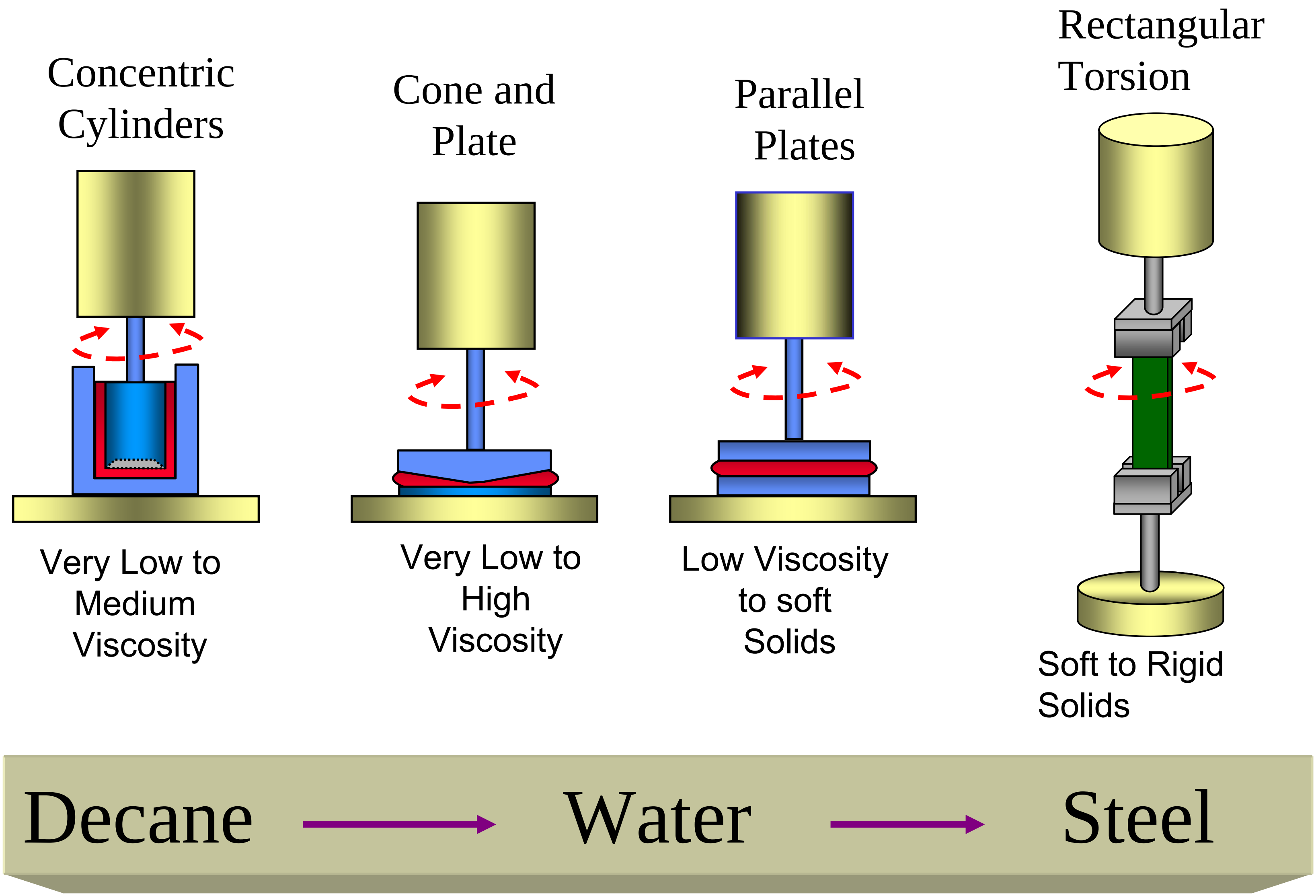
  - *The apparent behavior can be used as a “finger print” or “benchmark” of the material.*

Constitutive Relations

$$\frac{Stress}{Strain} = Modulus$$

$$\frac{Stress}{Shear\ rate} = \text{Viscosity}$$

Measuring Systems - Geometries



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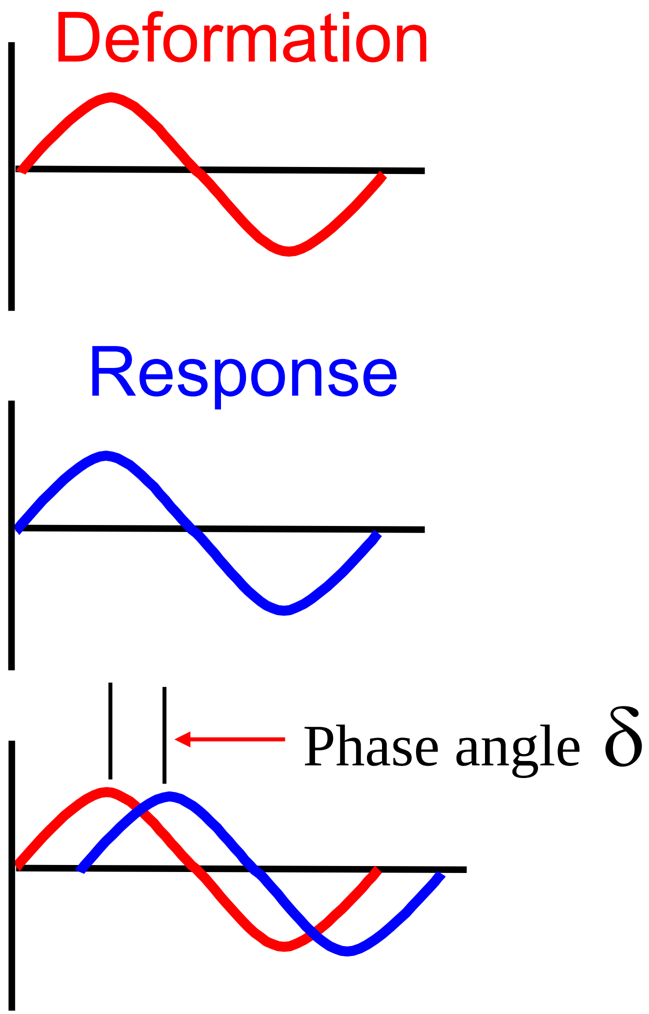
Dynamic Testing

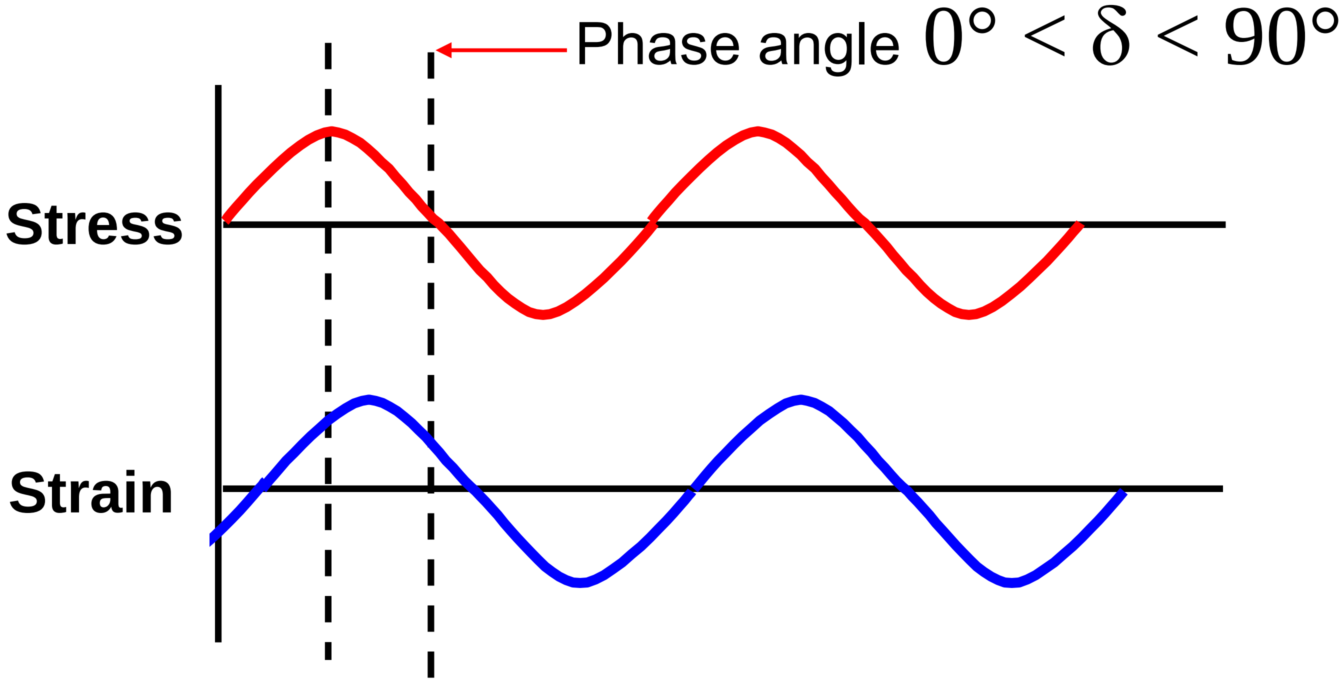
- An oscillatory (sinusoidal) deformation (stress or strain) is applied to a sample.

- The material response (strain or stress) is measured.

- The phase angle δ, or phase shift, between the deformation and response is measured.



Dynamic Viscoelastic Material Response



Viscoelastic Parameters

The Complex Modulus: Measure of materials overall resistance to deformation.

$$G^* = Stress^*/Strain$$

$$G^* = G' + iG''$$

The Elastic (Storage) Modulus: Measure of elasticity of material. The ability of the material to store energy.

$$G' = (stress^*/strain)\cos\Theta$$

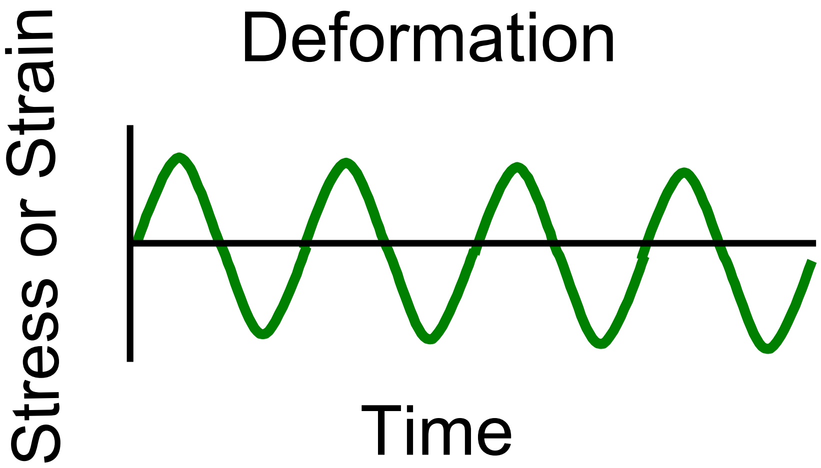
The Viscous (loss) Modulus: The ability of the material to dissipate energy. Energy lost as heat.

$$G'' = (stress^*/strain)\sin\Theta$$

Tan Delta: Measure of material damping - such as vibration or sound damping.

$$\text{Tan } \sigma = G''/G'$$

Dynamic Time Sweep (Time Ramp)



- The material response is monitored at a constant frequency, amplitude and temperature.

- <u>USES</u>
  - Time dependent Thixotropy
  - Cure Studies
  - Stability against thermal degradation
  - Solvent evaporation/drying

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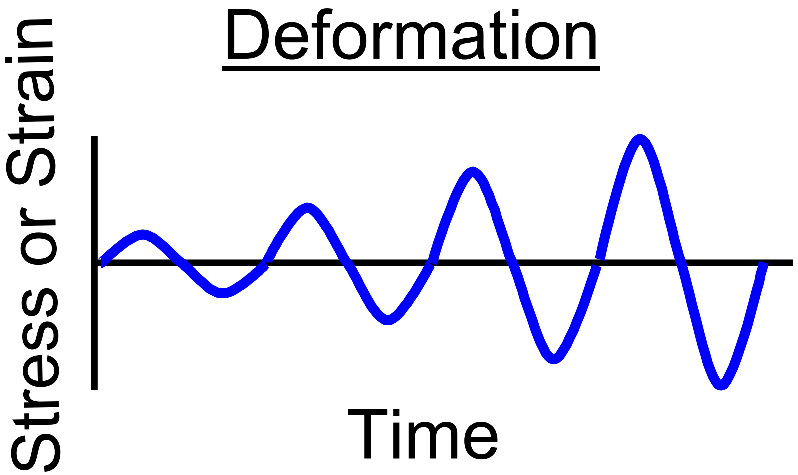
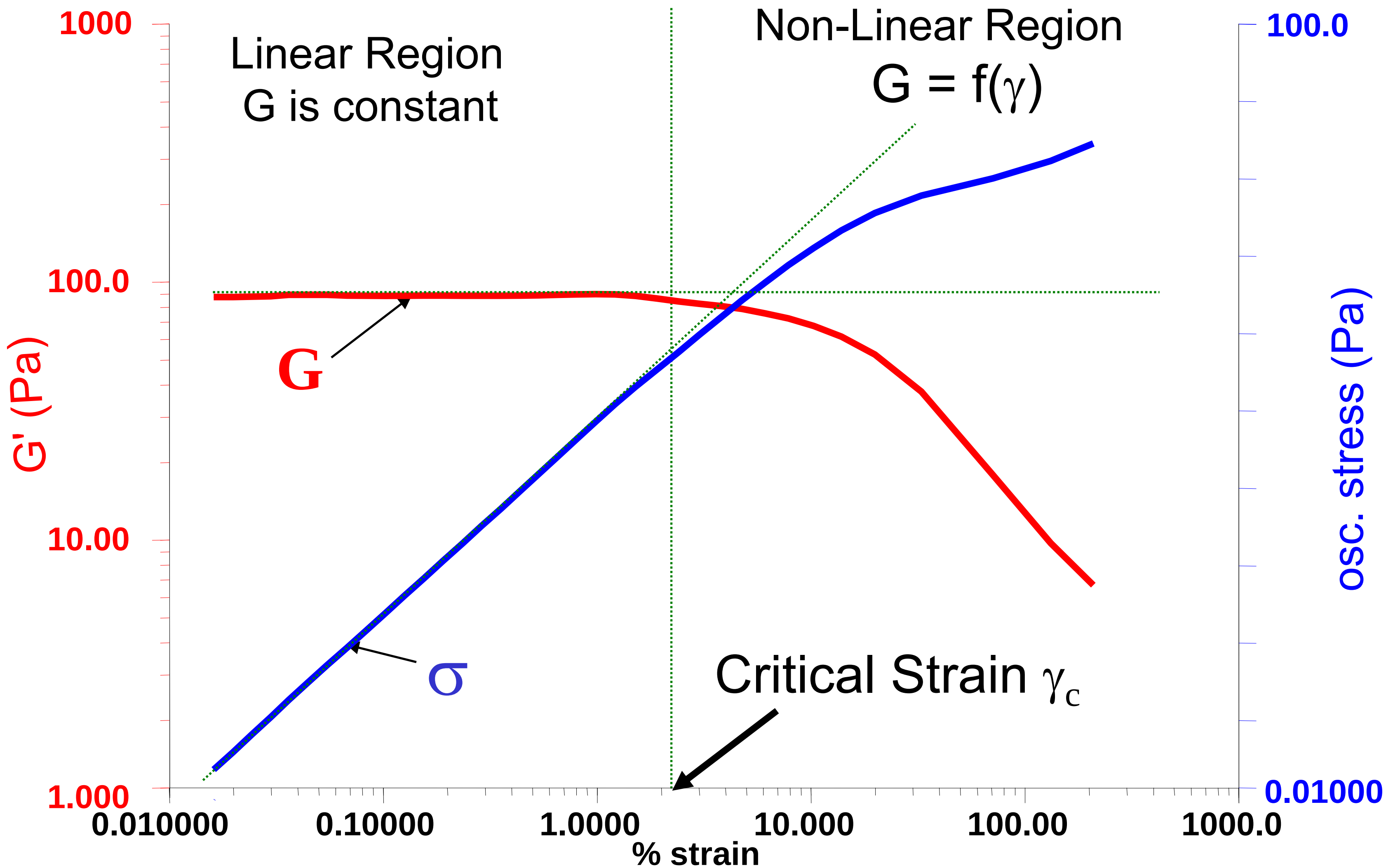
Dynamic Stress or Strain Sweep (Torque Ramp)



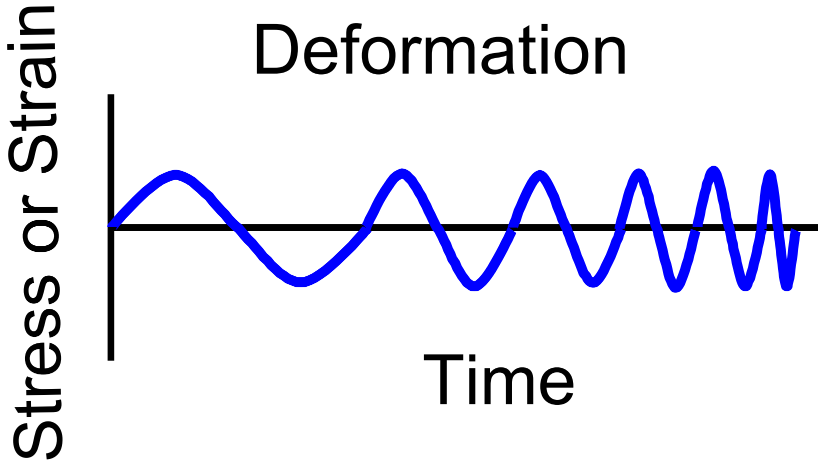
- The material response to increasing deformation amplitude (stress or strain) is monitored at a constant frequency and temperature.

- USES
  - Identify Linear Viscoelastic Region
  - Strength of dispersion structure - settling stability
  - Resilience

Dynamic Strain Sweep: Material Response



Frequency Sweep

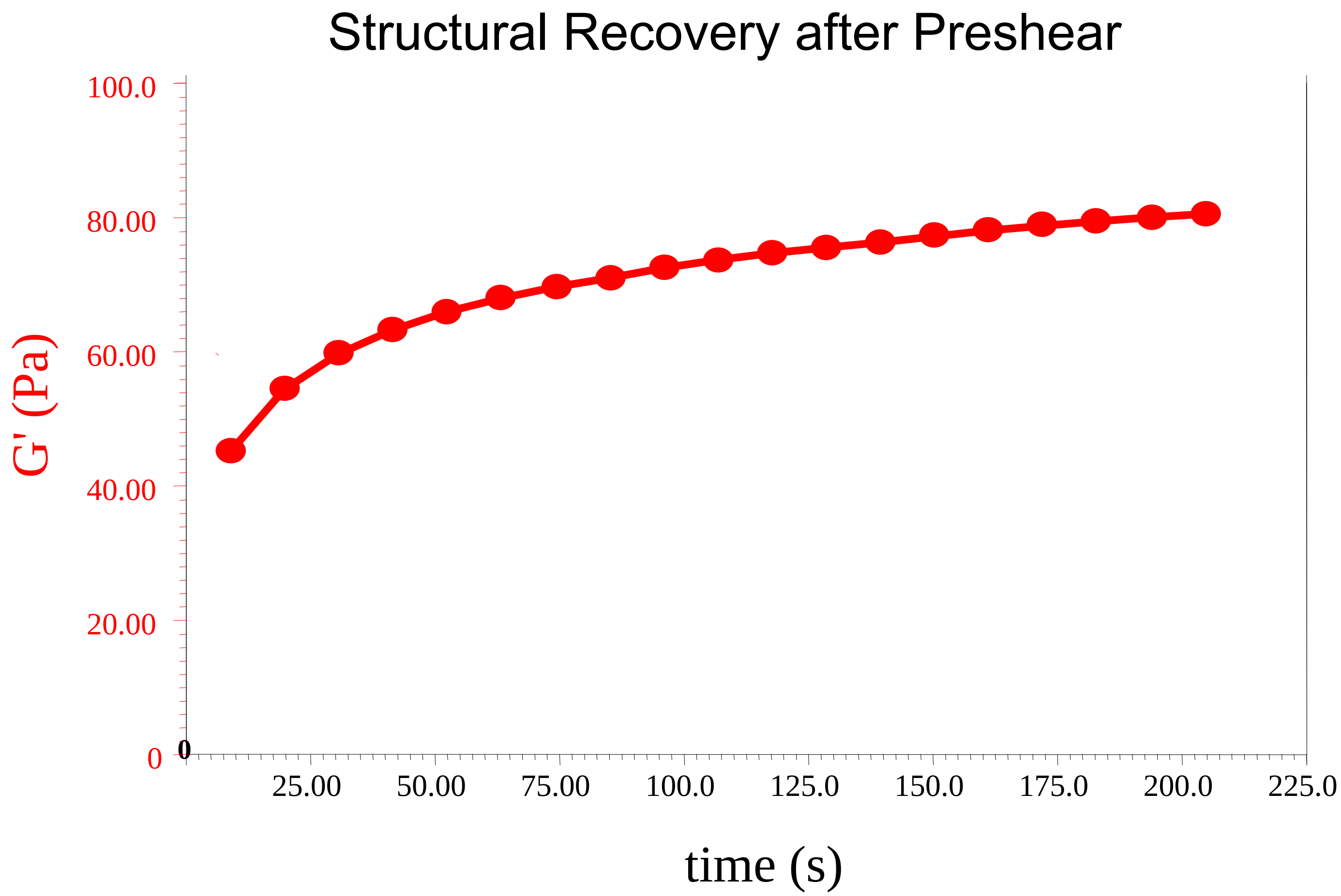


- The material response to increasing frequency (rate of deformation) is monitored at a constant amplitude (stress or strain) and temperature.

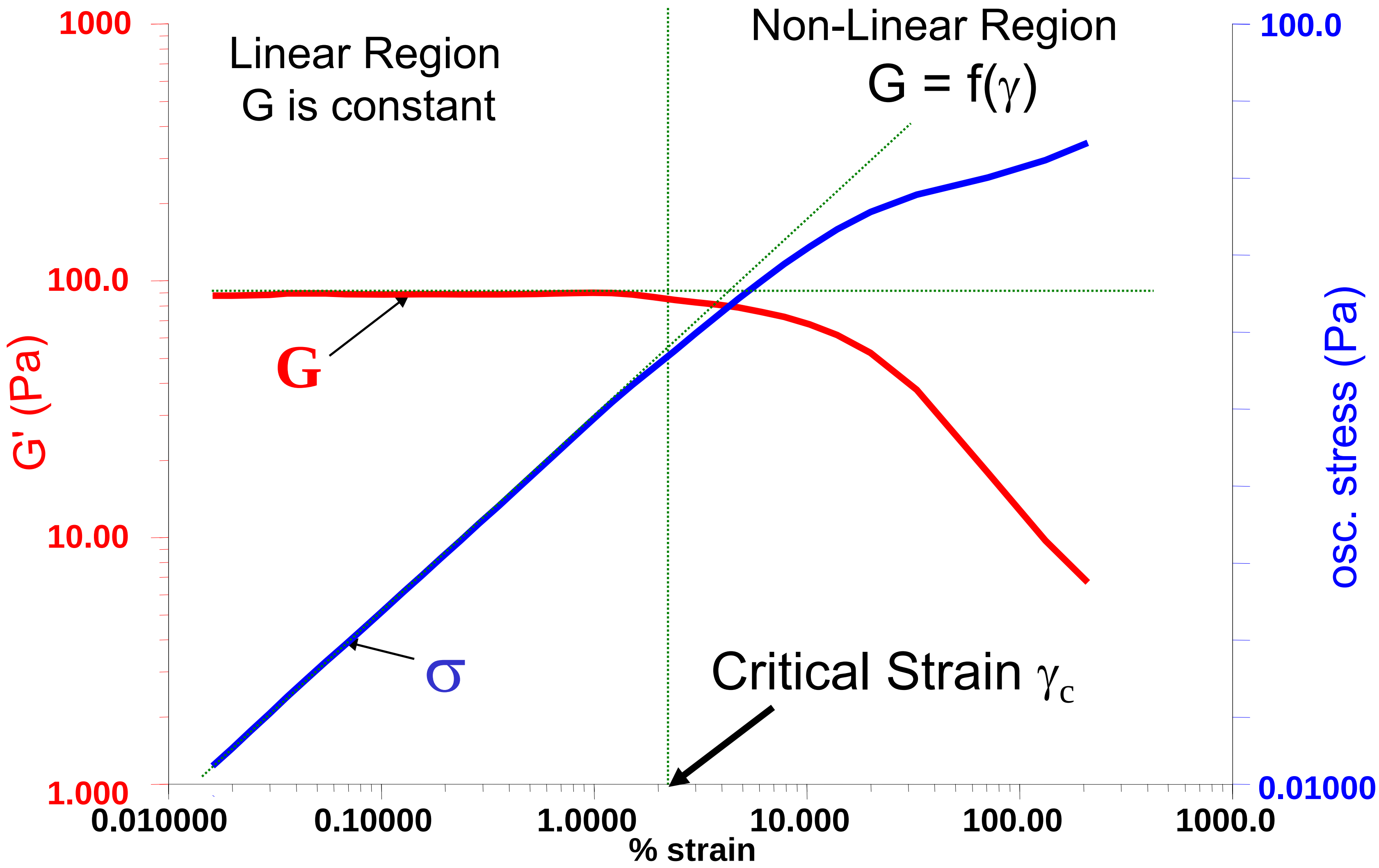
- <u>USES</u>

➢ Viscosity Information - Zero Shear η, shear thinning
➢ Elasticity (reversible deformation) in materials
➢ MW & MWD differences Polymer Melts and Polymer solutions.
➢ Finding Yield in gelled dispersions
➢ High and Low Rate (short and long time) modulus properties.
➢ Extend time or frequency range with TTS

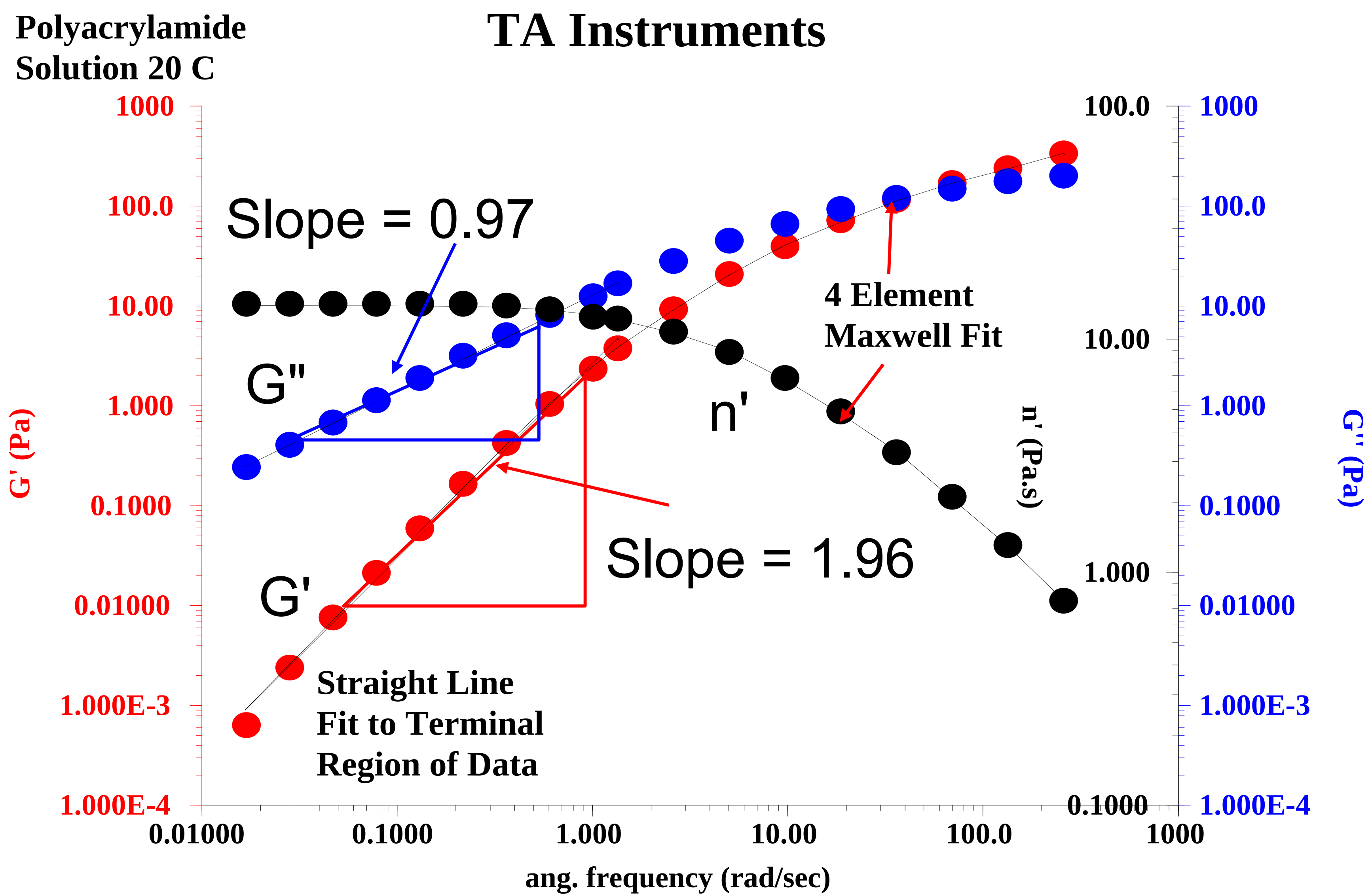
Time Sweep on Latex



Dynamic Strain Sweep: Material Response



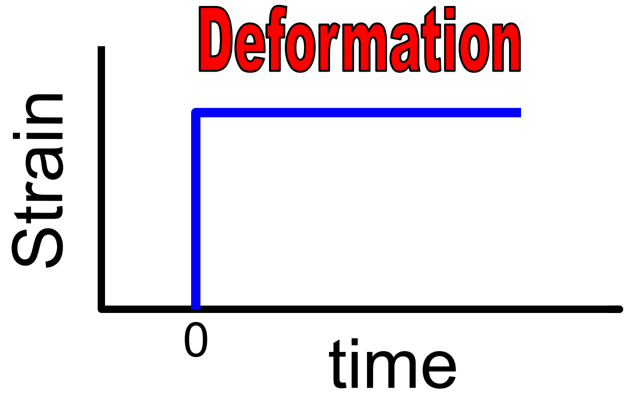
Oscillation Model Fitting for Classic Polymer Data [Polyacrylamide Soln.]



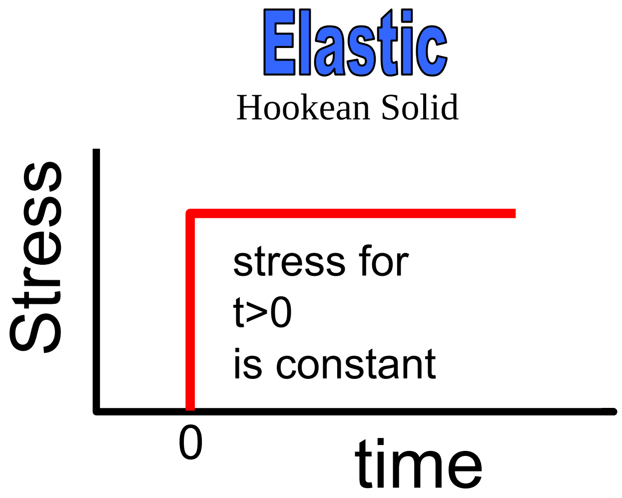
Defining Shear Rate Ranges

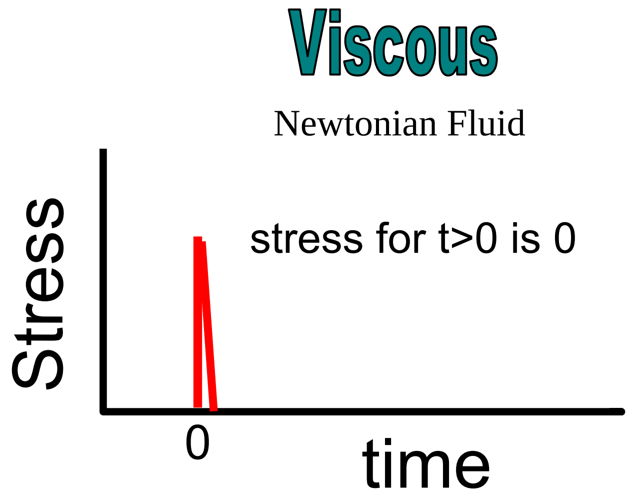
Situation	**Shear Rate Range**	**Examples**
Sedimentation of fine powders in liquids	10^{-6} to 10^{-3}	Medicines, Paints, Salad Dressing
Leveling due to surface tension	10^{-2} to 10^{-1}	Paints, Printing inks
Draining off surfaces under gravity	10^{-1} to 10^{1}	Toilet bleaches, paints, coatings
Extruders	10^{0} to 10^{2}	Polymers, foods
Chewing and Swallowing	**10^{1} to 10^{2}**	**Foods**
Dip coating	10^{1} to 10^{2}	Confectionery, paints
Mixing and stirring	**10^{1} to 10^{3}**	**Liquids manufacturing**
Pipe Flow	**10^{0} to 10^{3}**	**Pumping liquids, blood flow**
Brushing	10^{3} to 10^{4}	Painting
Rubbing	**10^{4} to 10^{5}**	**Skin creams, lotions**
High-speed coating	10^{4} to 10^{6}	Paper manufacture
Spraying	10^{5} to 10^{6}	Atomization, spray drying
Lubrication	10^{3} to 10^{7}	Bearings, engines

Stress Relaxation Experiment



Response of Classical Extremes





Stress Relaxation Experiment (cont'd)

Response of **Viscoelastic** Material

Stress decreases with time starting at some high value and decreasing to zero.

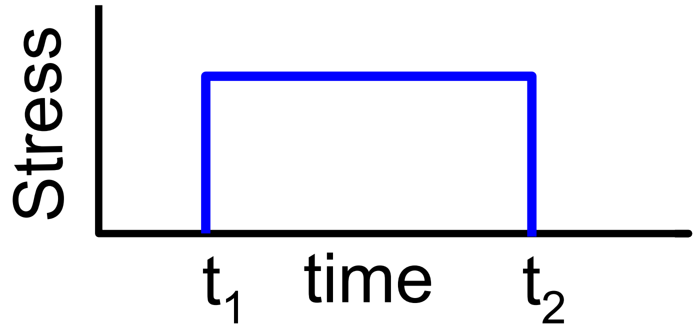
- For small deformations (strains within the linear region) the ratio of stress to strain is a function of time only.

- This function is a material property known as the STRESS RELAXATION MODULUS, G(t)

$$G(t) = s(t)/\gamma$$

Creep Recovery Experiment

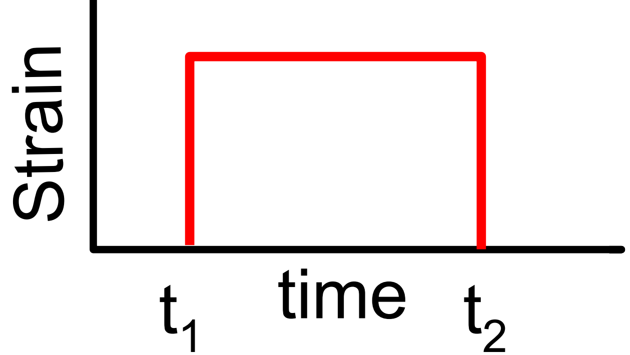
Deformation



Response of Classical Extremes

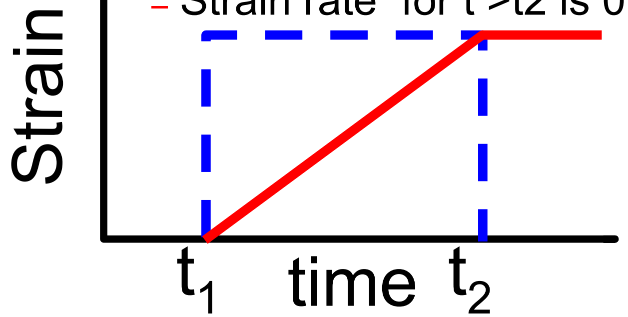
Elastic

- Stain for t>t1 is constant
- Strain for t >t2 is 0

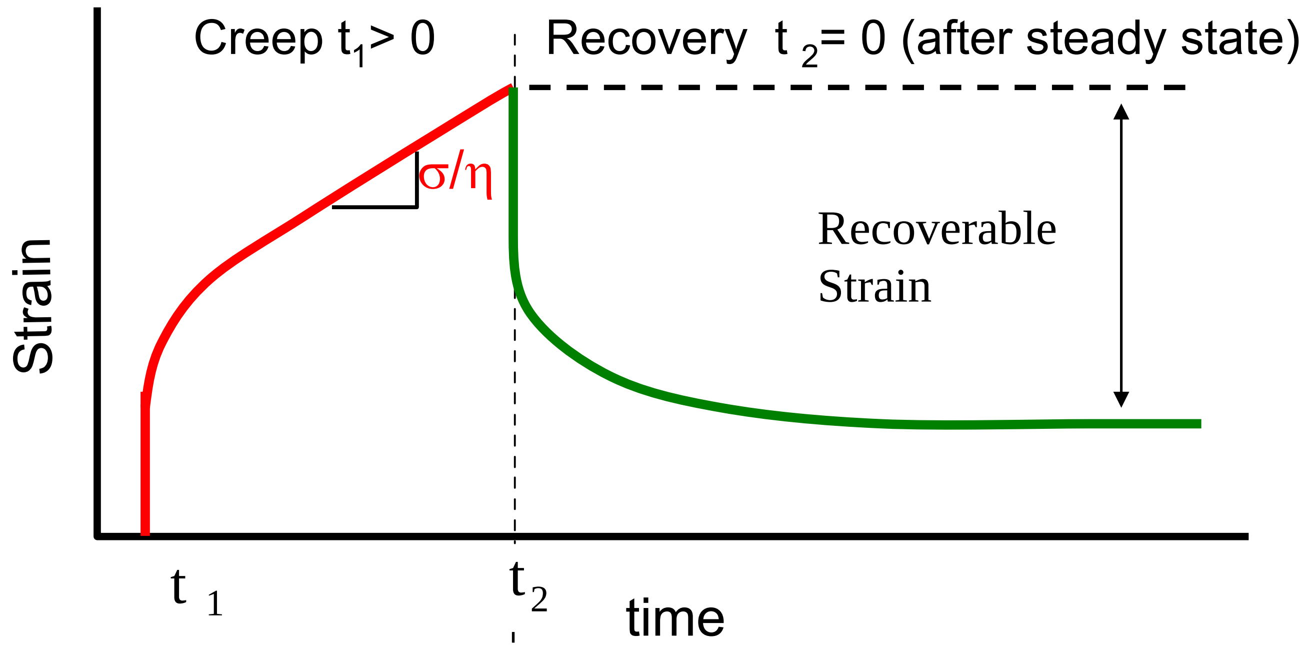


Viscous

- Stain rate for t>t1 is constant
- Strain for t>t1 increase with time
- Strain rate for t >t2 is 0



Creep Recovery Experiment: Response of Viscoelastic Material

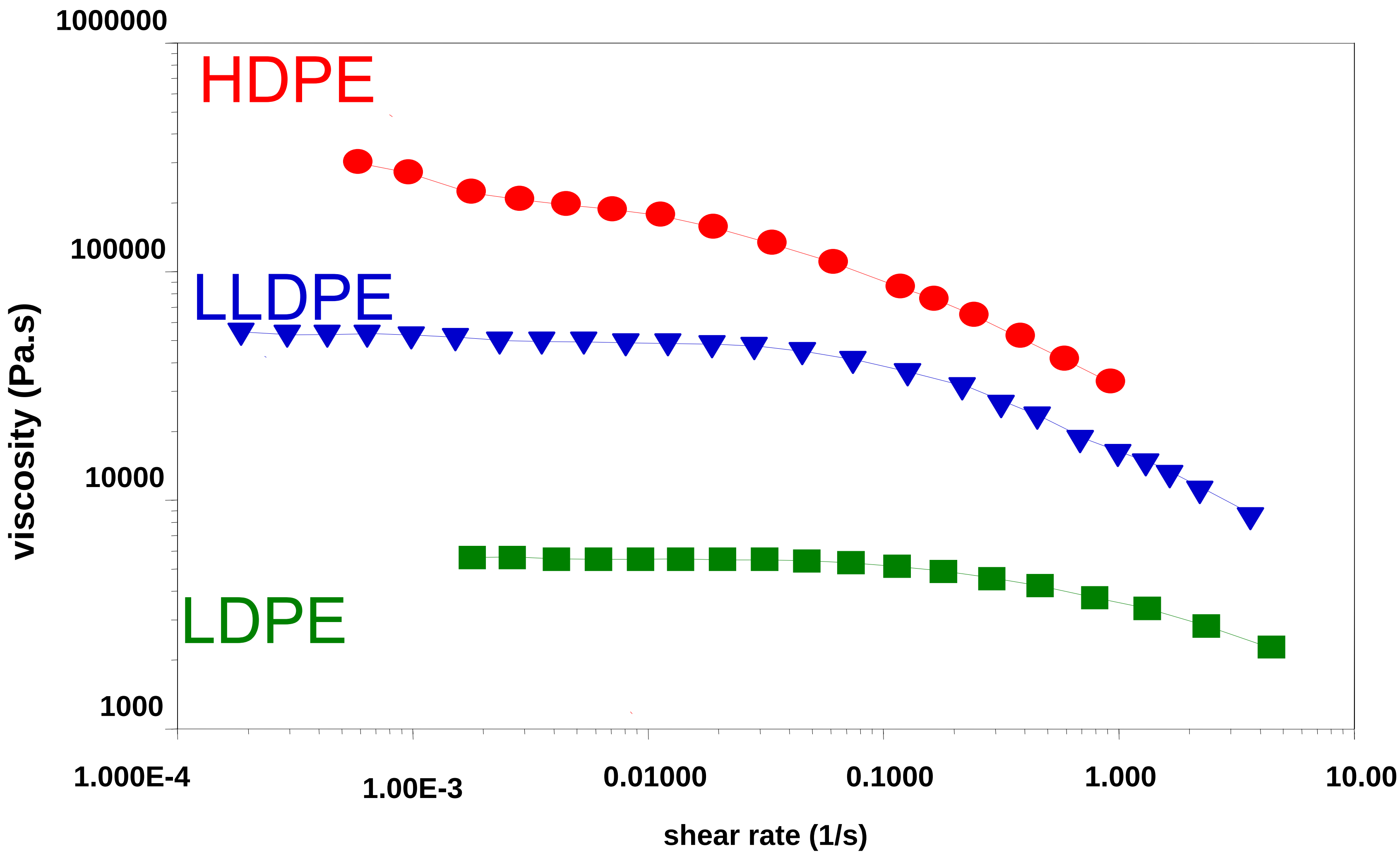


Strain rate decreases with time in the creep zone, until finally reaching a steady state.

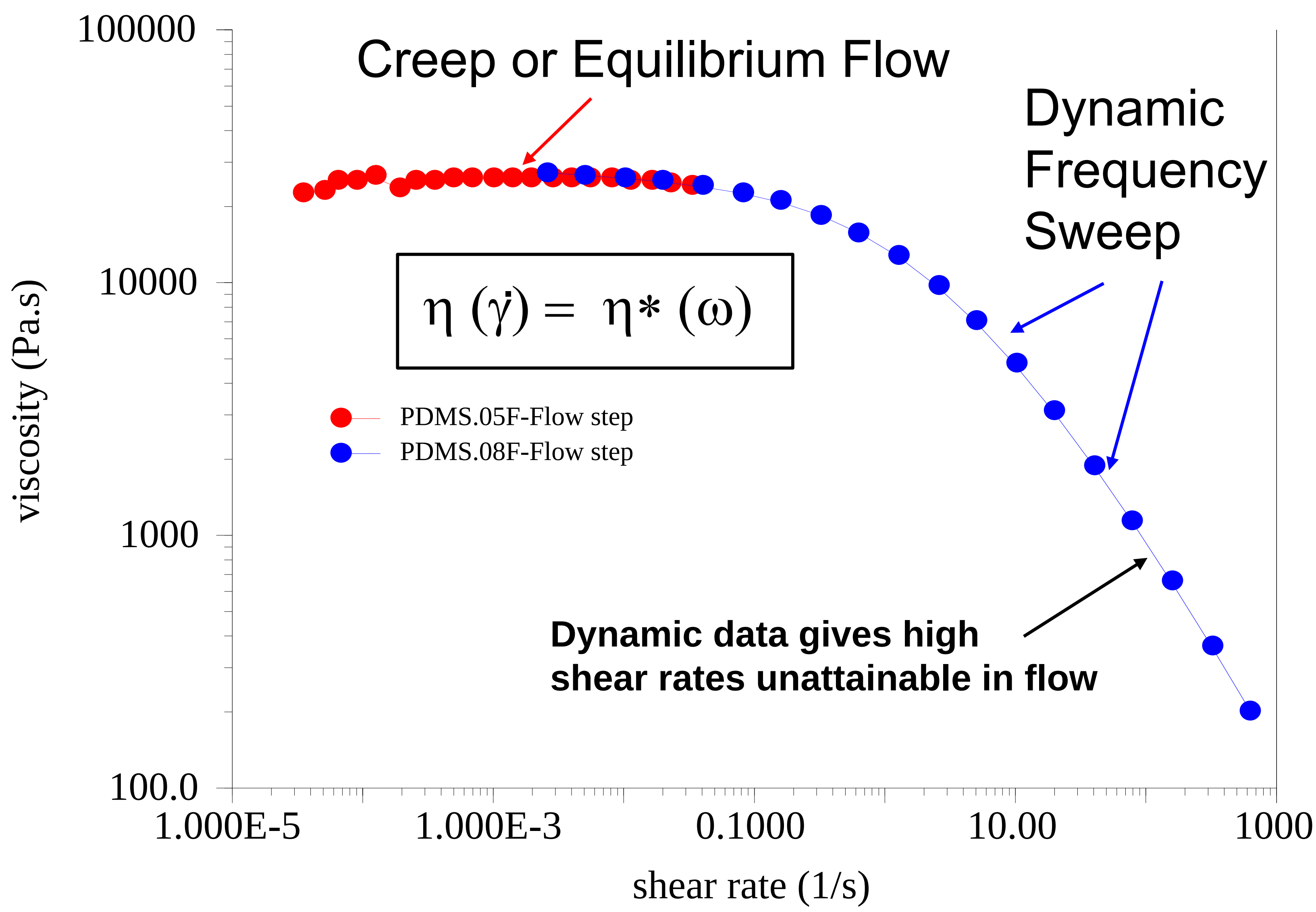
In the recovery zone, the viscoelastic fluid recoils, eventually reaching a equilibrium at some small total strain relative to the strain at unloading.

Reference: Mark, J., et.al., Physical Properties of Polymers, American Chemical Society, 1984, p. 102.

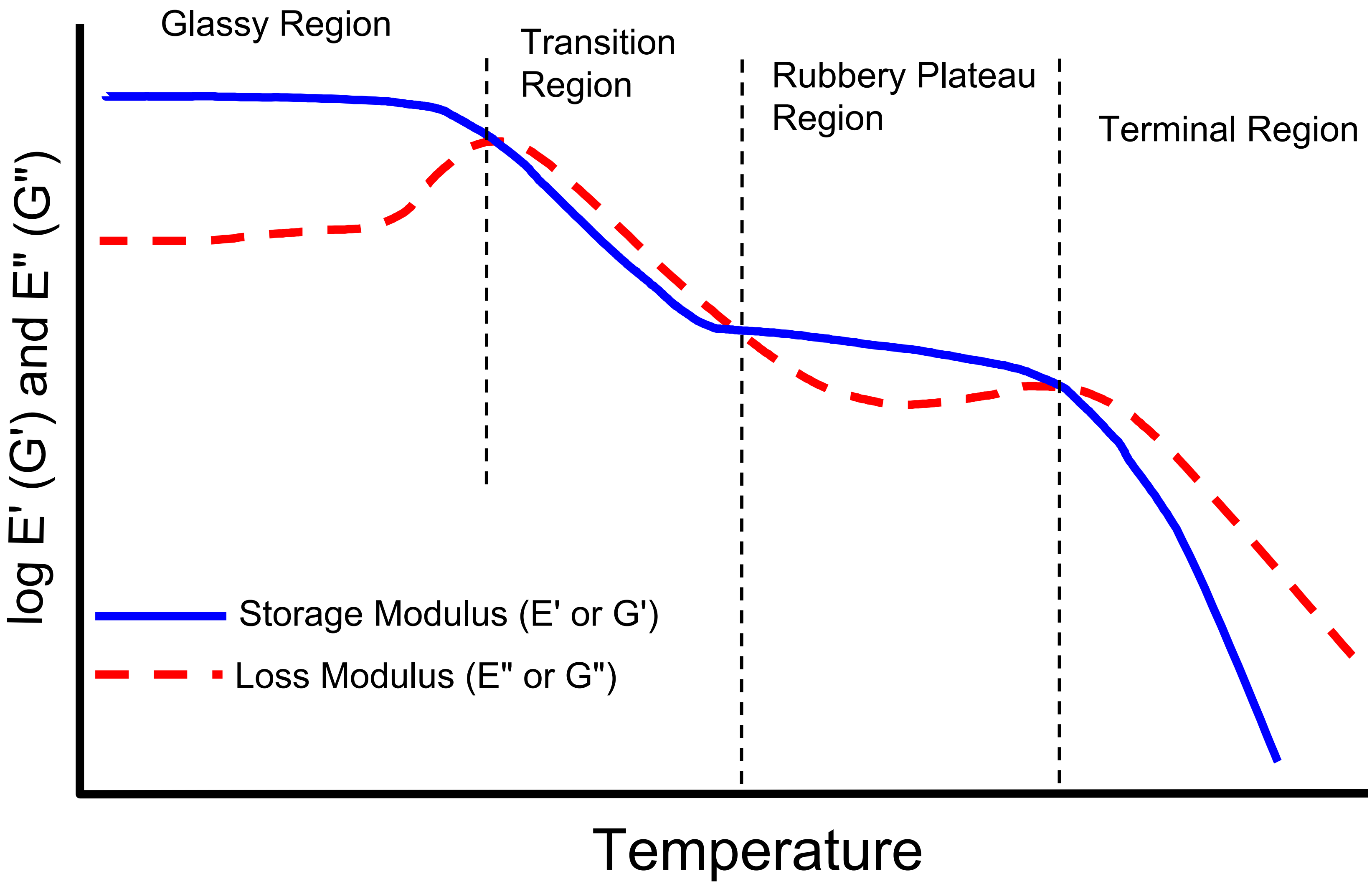
Polyethylene Rheology @ 150 C



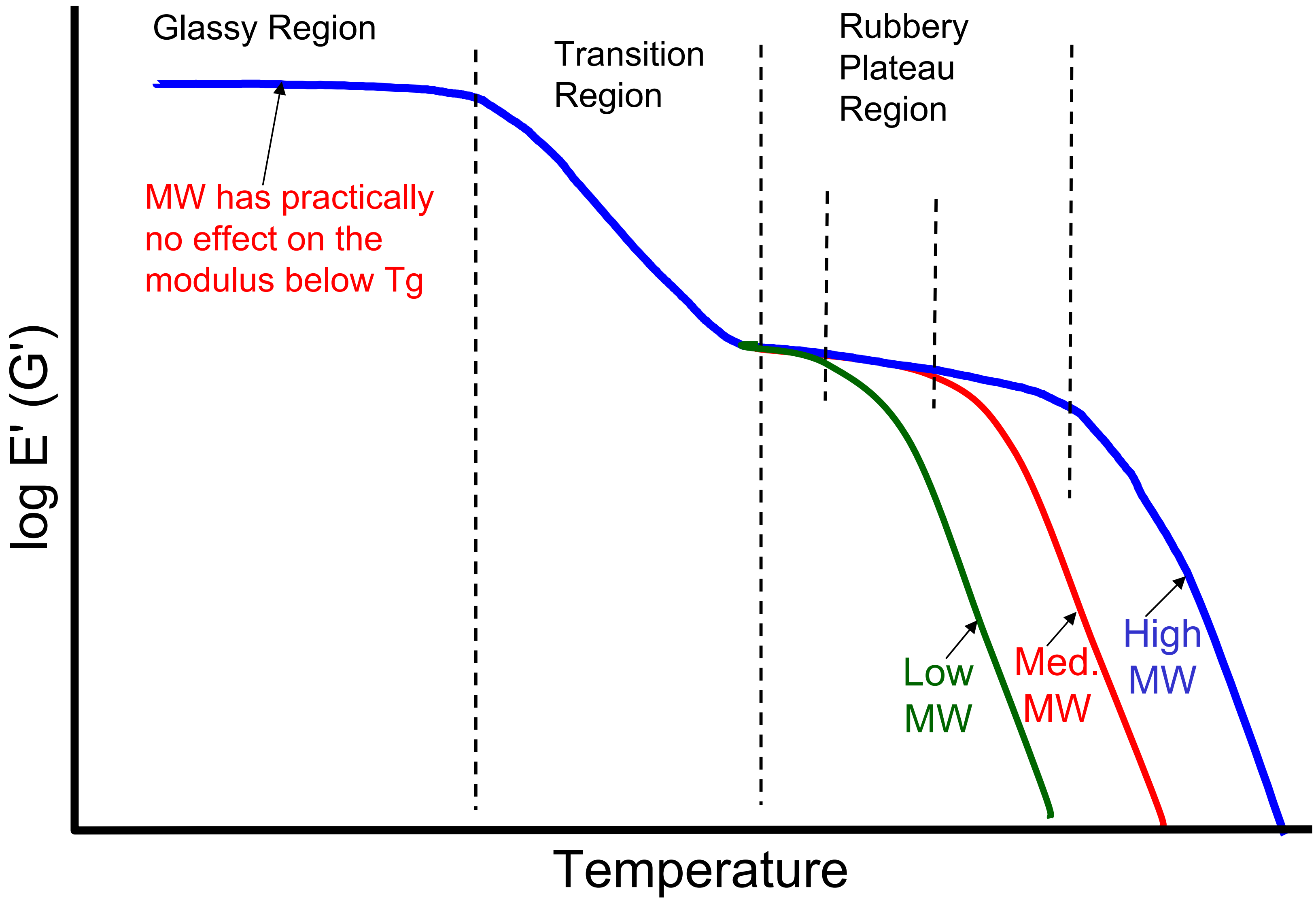
Polydimethylsiloxane - Cox-Merz Data



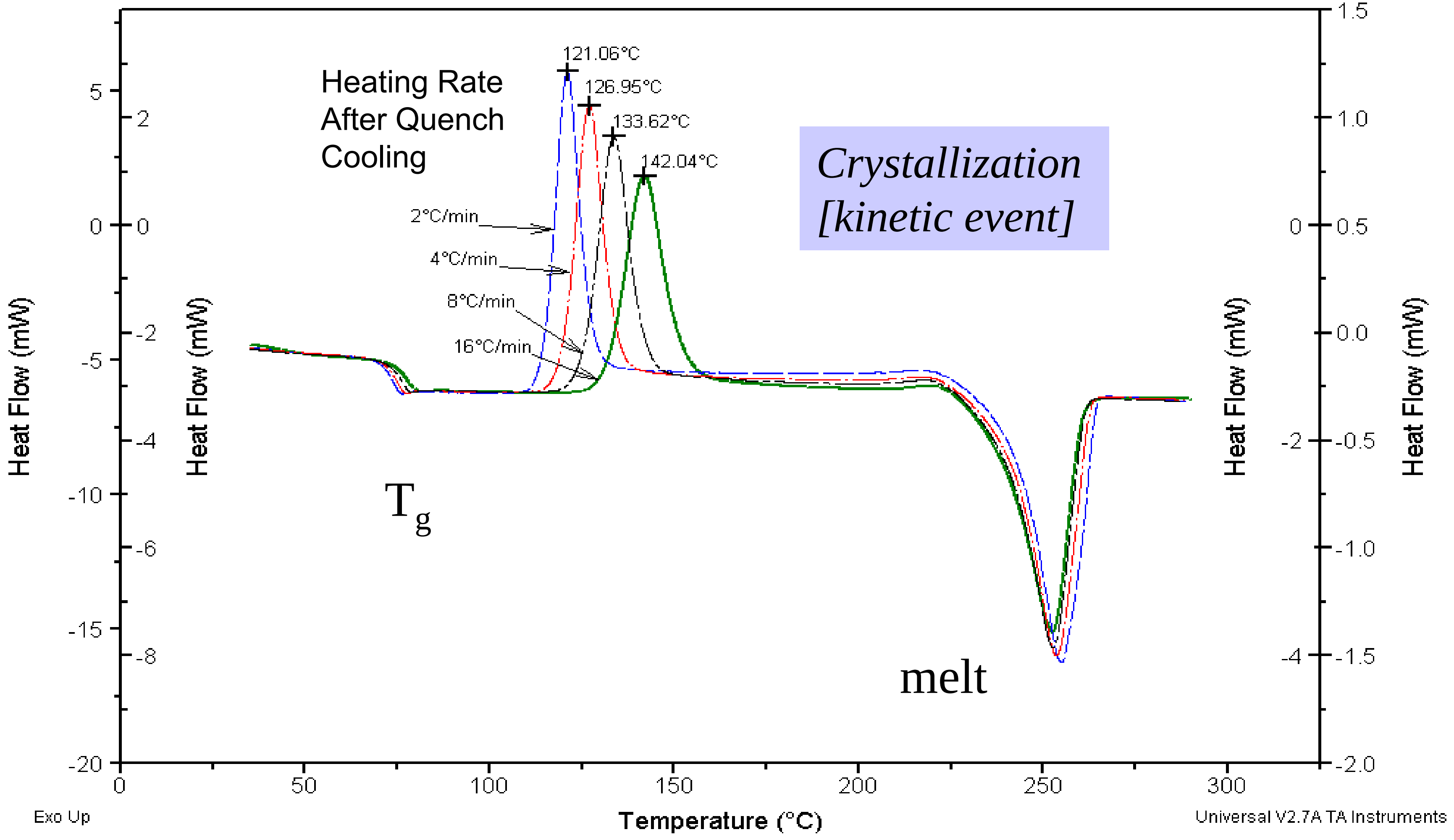
Dynamic Temperature Ramp or Step and Hold: Material Response



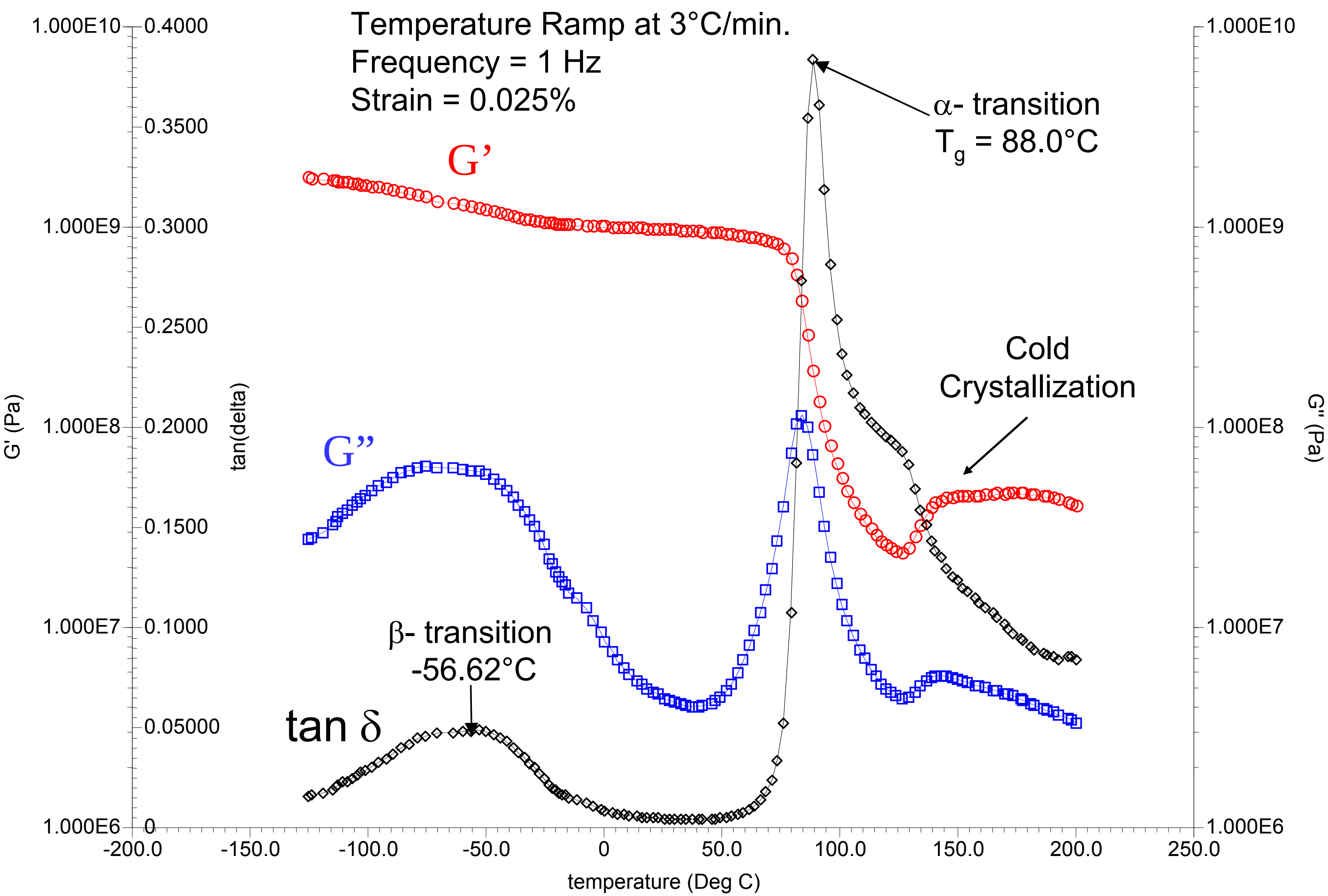
Molecular Structure - Effect of Molecular Weight



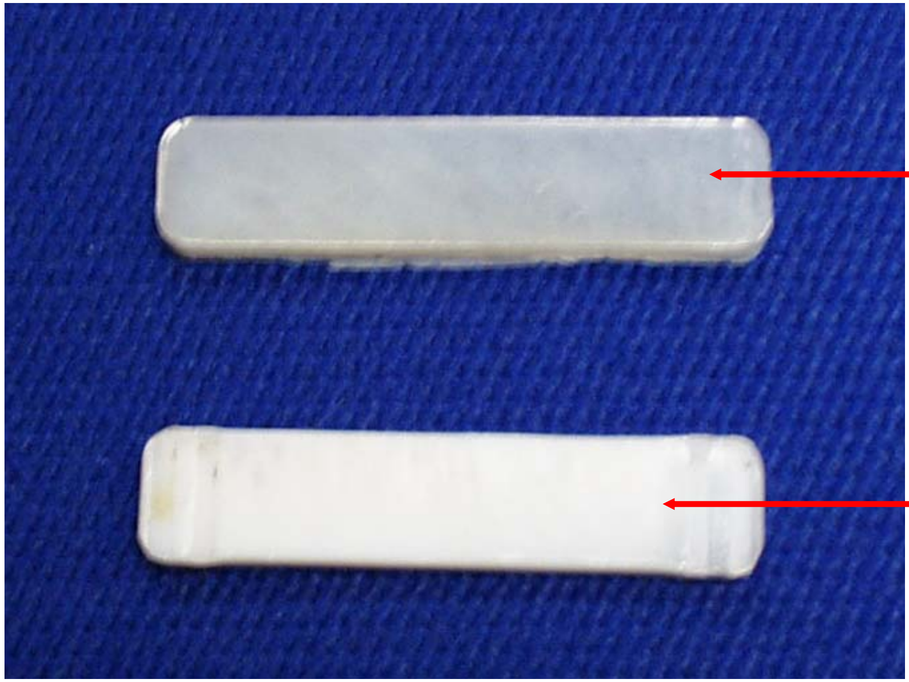
Effect of Heating Rate on Temperature of Cold Crystallization in PET



PET Bottle Resin – Cold Crystallization



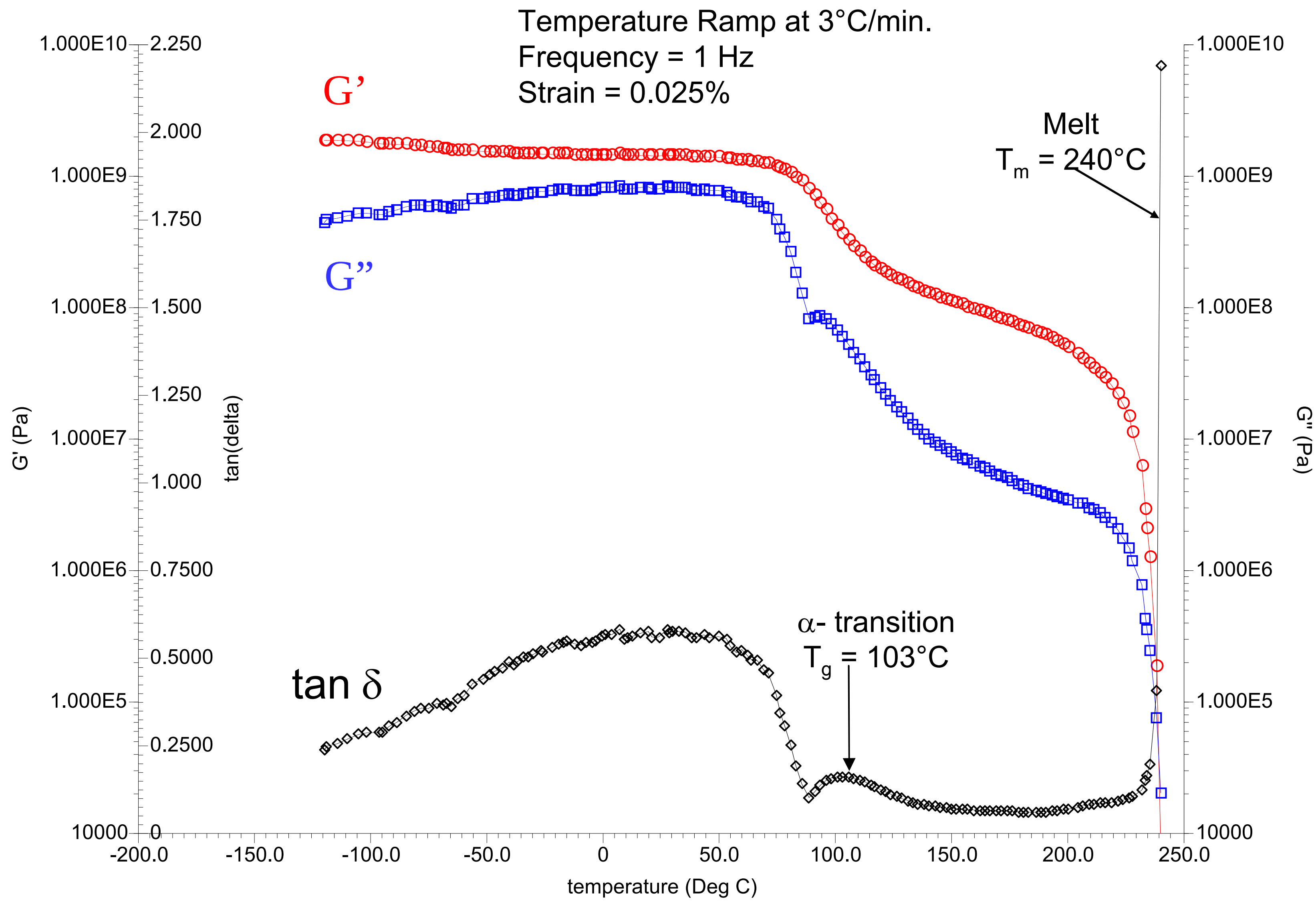
PET Bottle Resin – Before and After DMA Scan



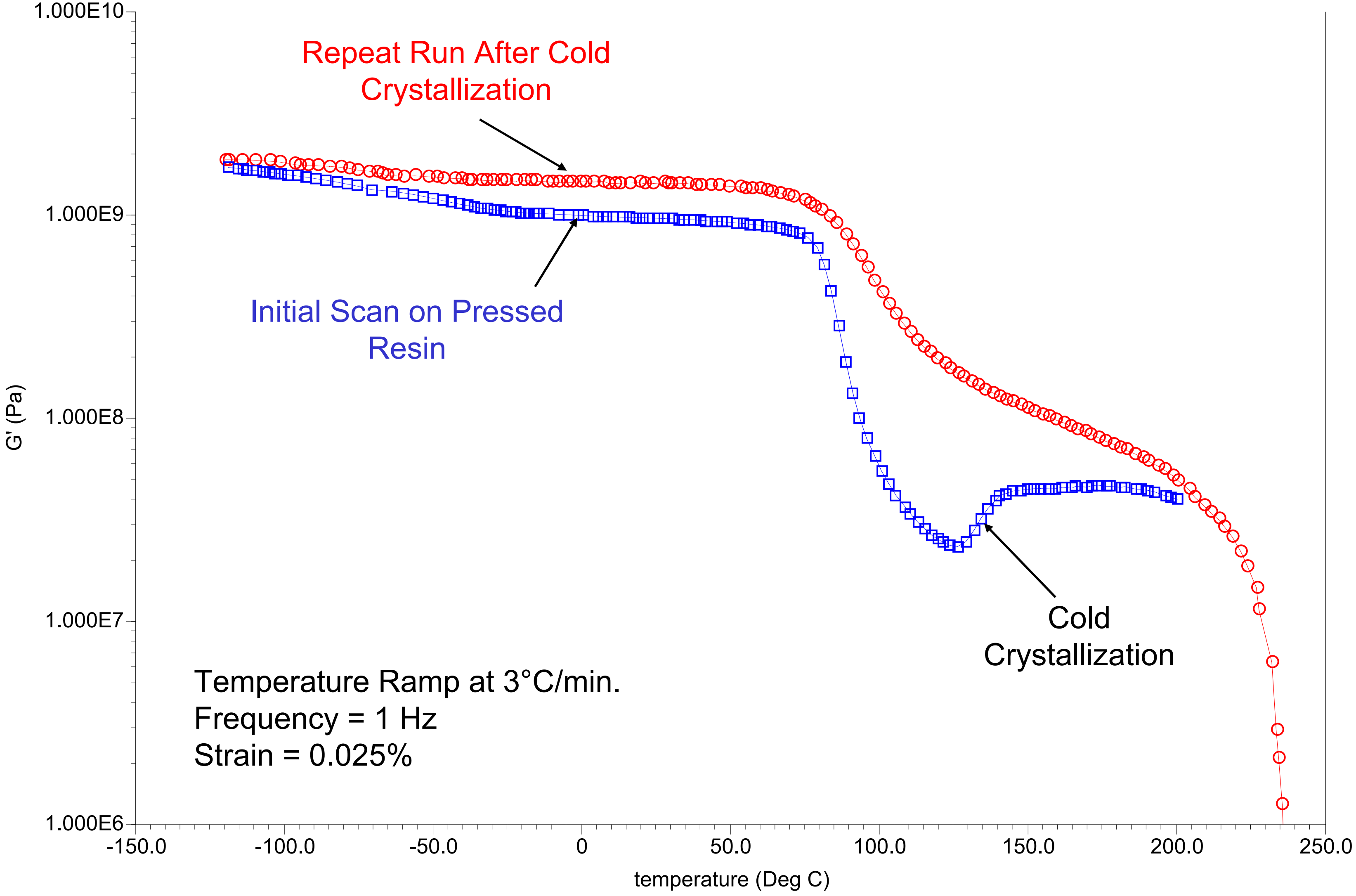
Pressed PET Bottle Resin

PET After Temperature Ramp Scan (Cold Crystallization)

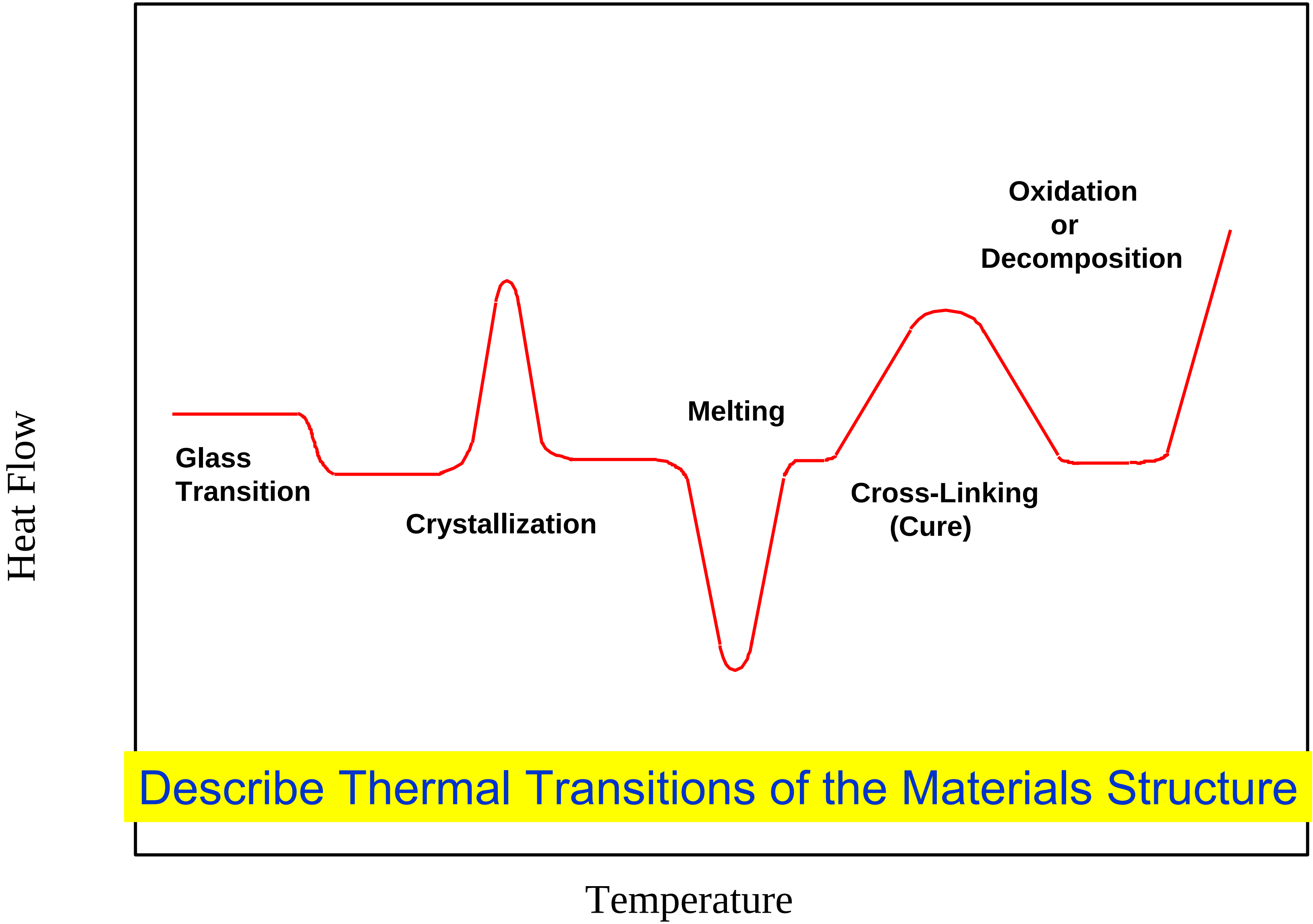
PET Bottle Resin - Repeat Run After Cold Crystallization



PET Bottle Resin - Comparison of G'



BECAUSE …Typical DSC Transitions



Describe Thermal Transitions of the Materials Structure

Quantitative Description of Consistency (structure) ?

BECAUSE …

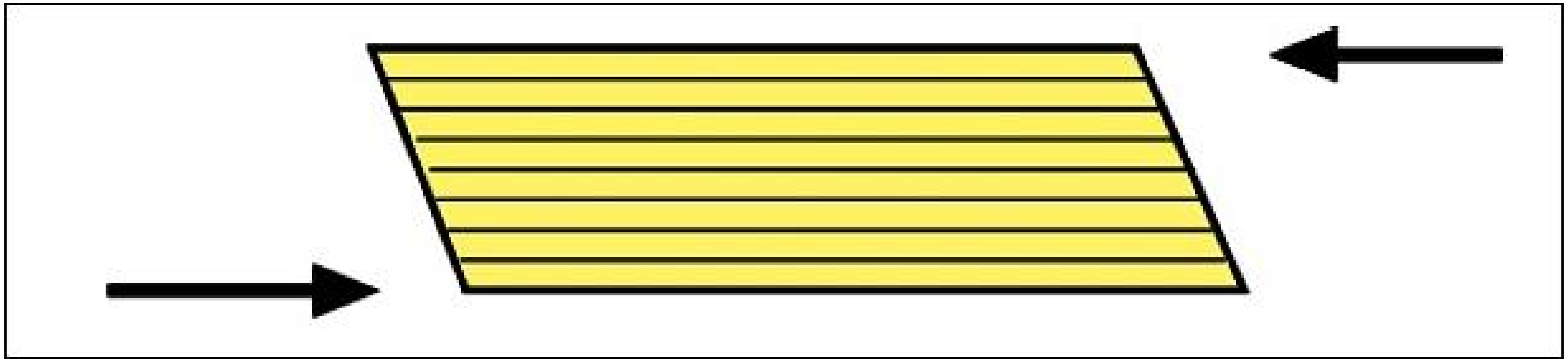
- Thermal Analysis describes thermal transitions

NEED to quantify ...

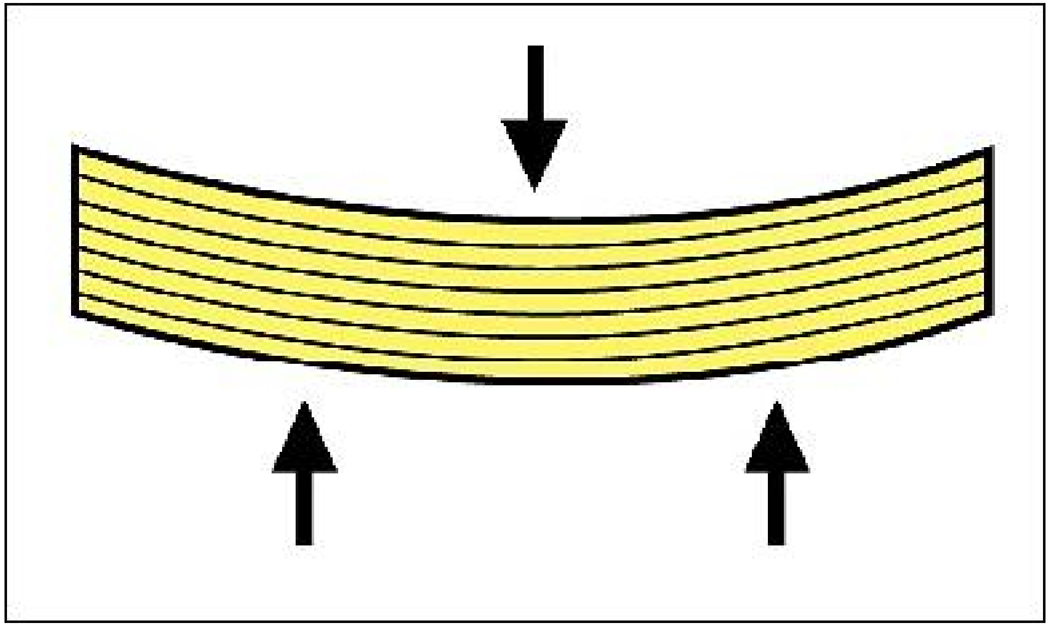
- Physical Properties of Structure
- Strength or weakness of the Structure

and because …

Rheology can do these; therefore, it is much more informative tool

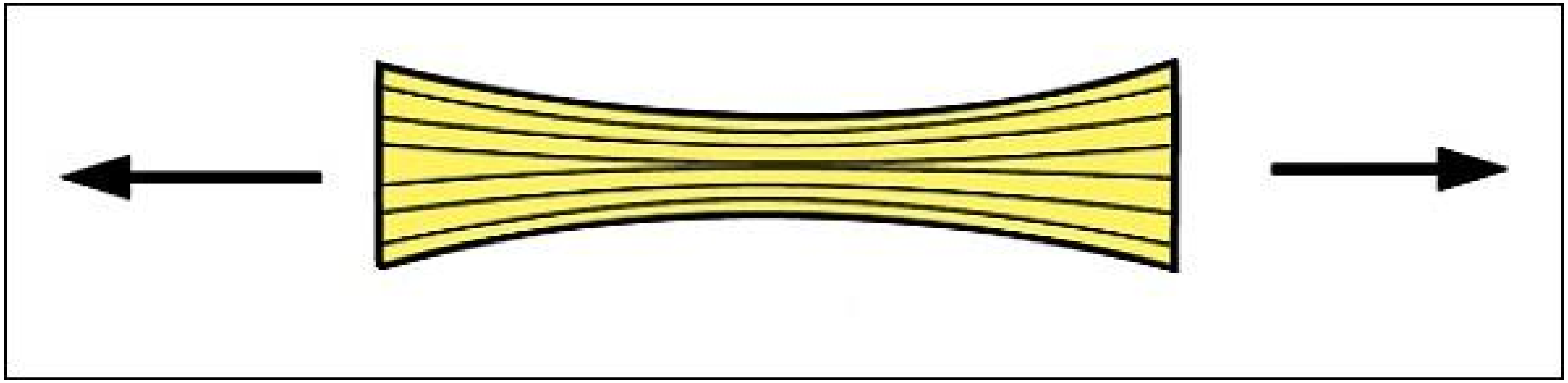


Shear

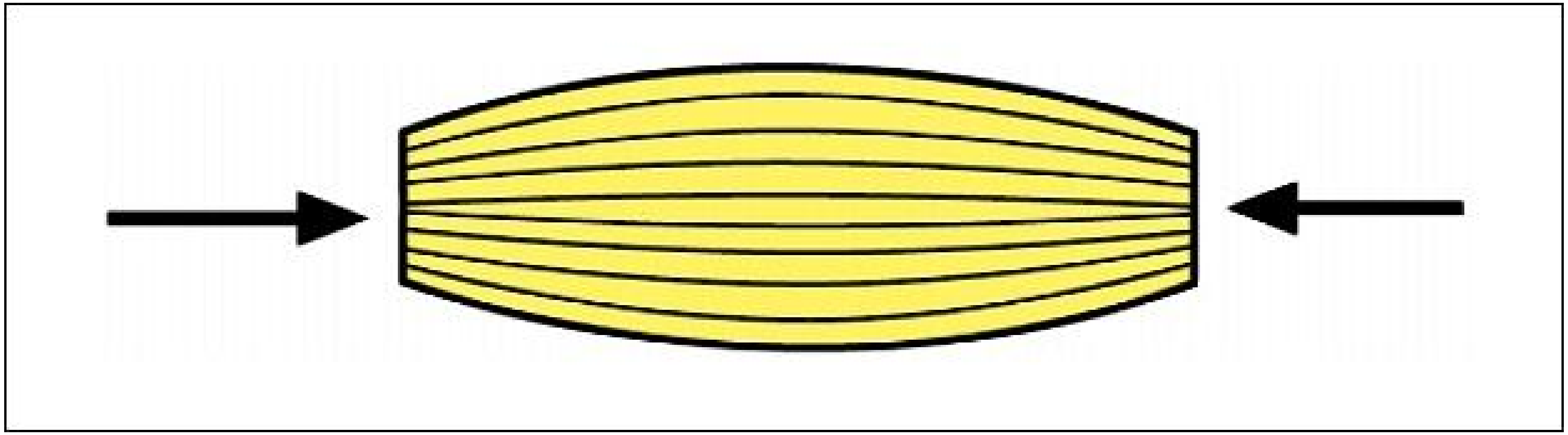


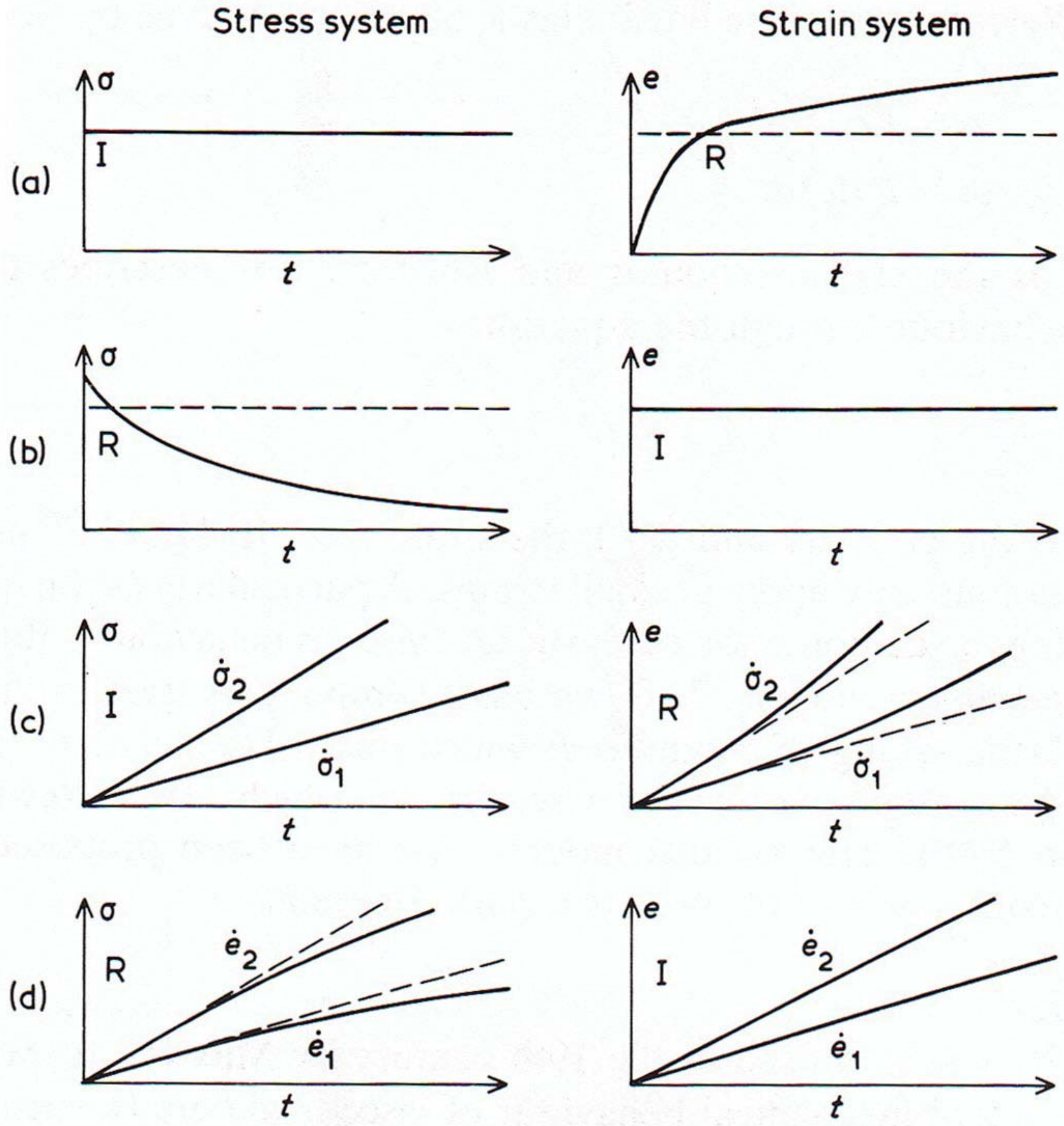
Flexure

Tension



Compression





Stress system
Strain system
(a)
σ
I
t
e
R
t
(b)
σ
R
t
e
I
t
(c)
σ
I
$\dot{\sigma}_2$
$\dot{\sigma}_1$
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e
R
$\dot{\sigma}_2$
$\dot{\sigma}_1$
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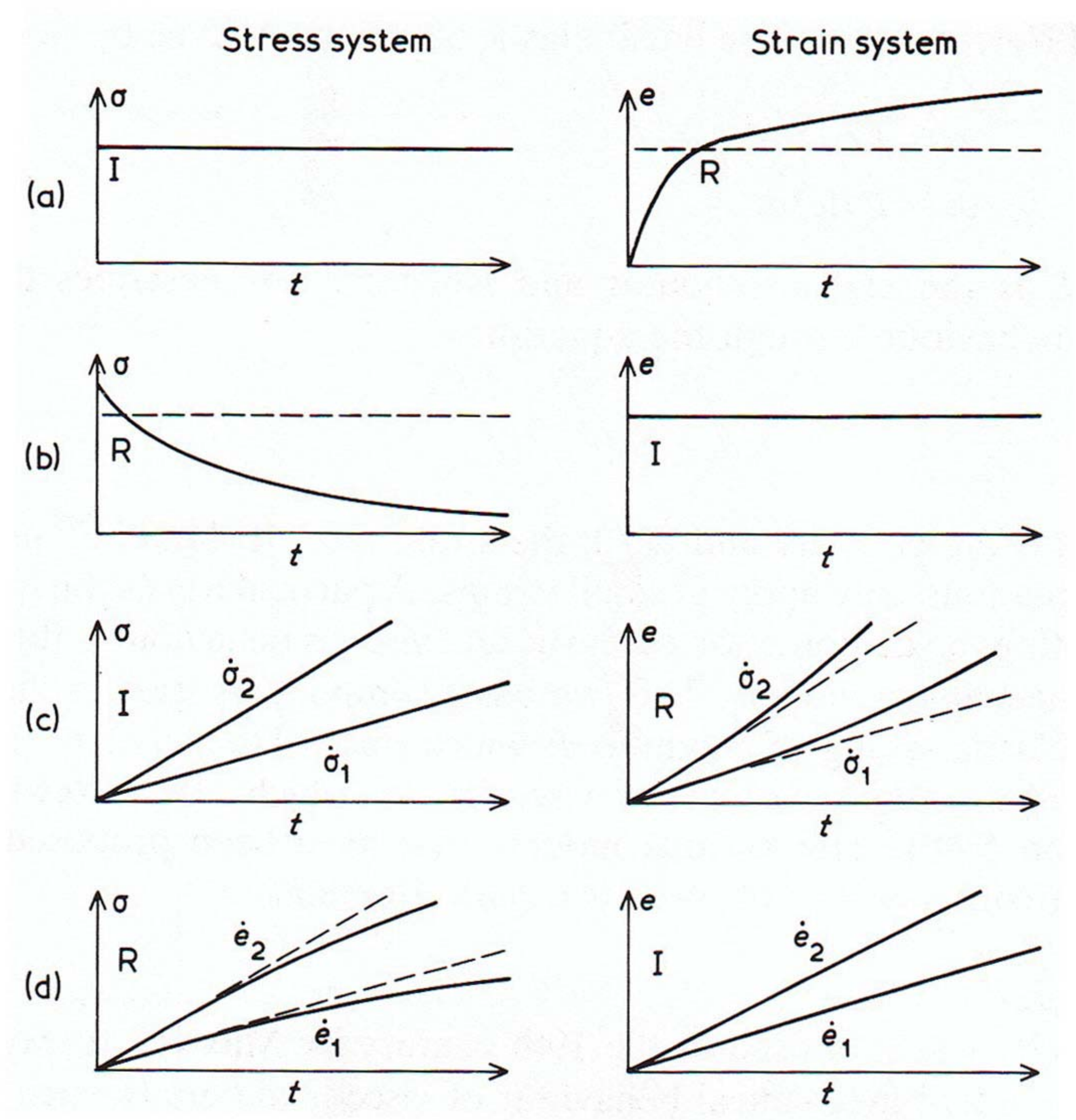

Stress system
Strain system
(a)
(b)
(c)
(d)
σ
e
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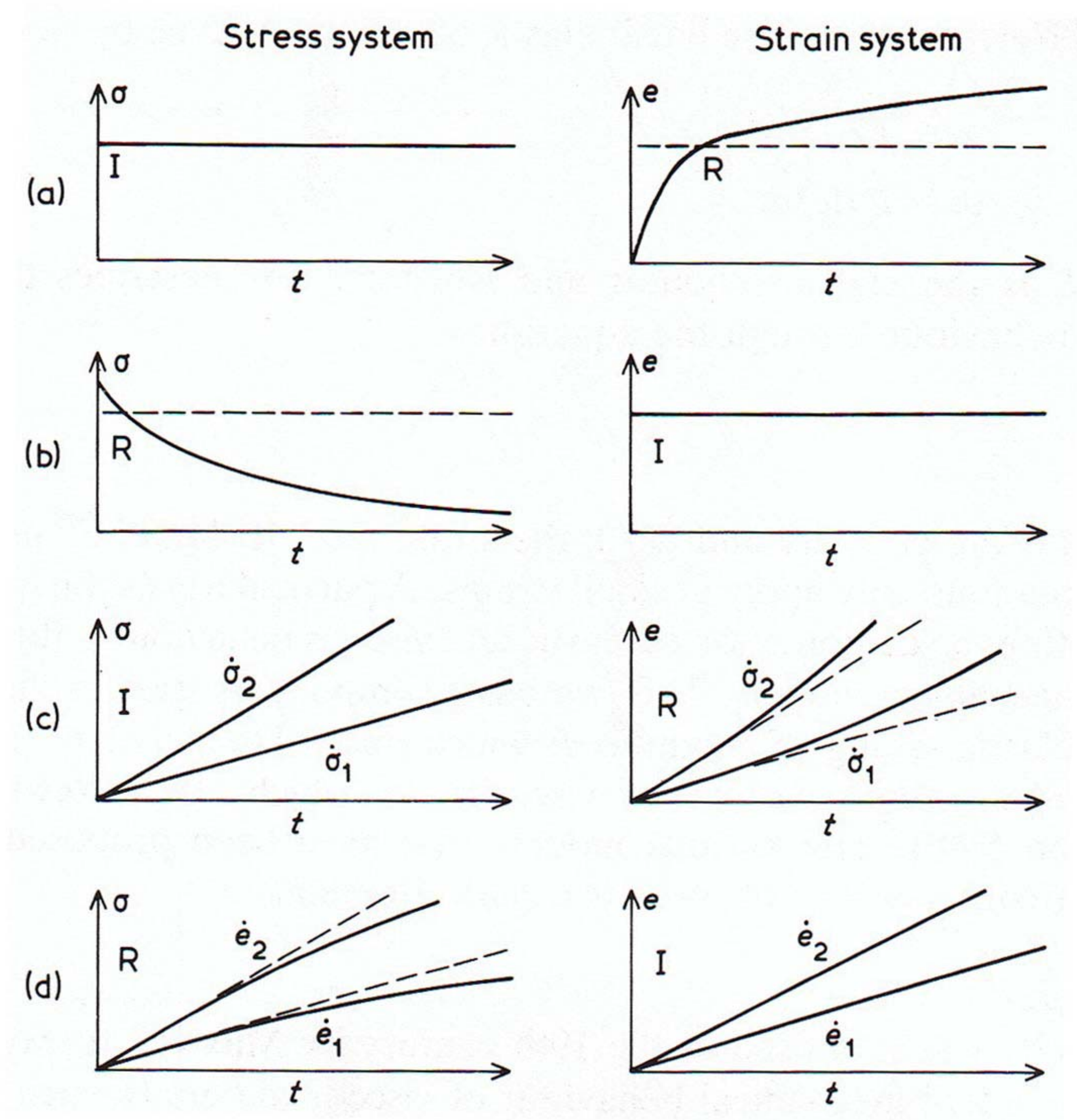
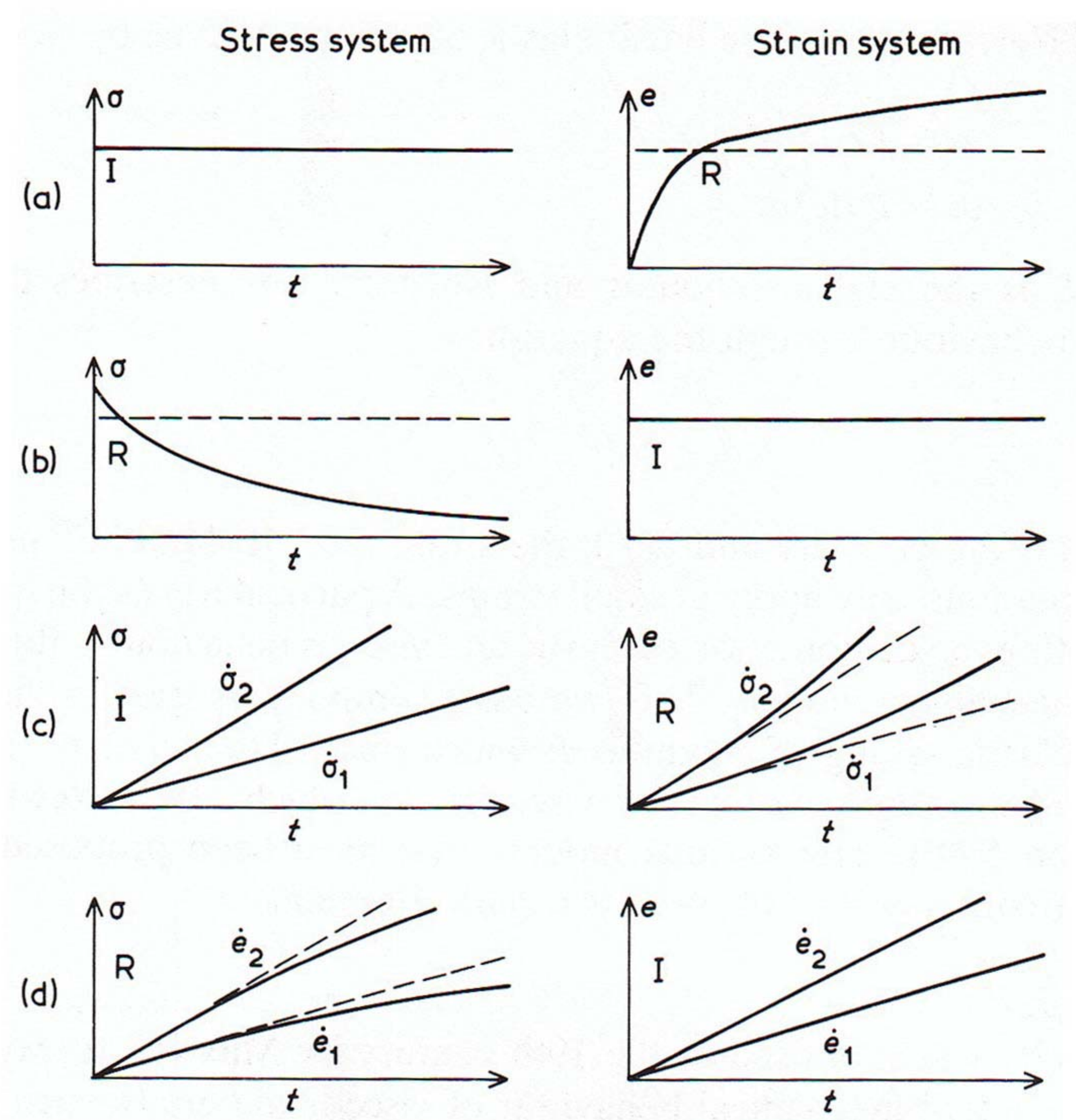
R
$\dot{\sigma}_2$
$\dot{\sigma}_1$
$\dot{e}_2$
$\dot{e}_1$

Creep



Creep

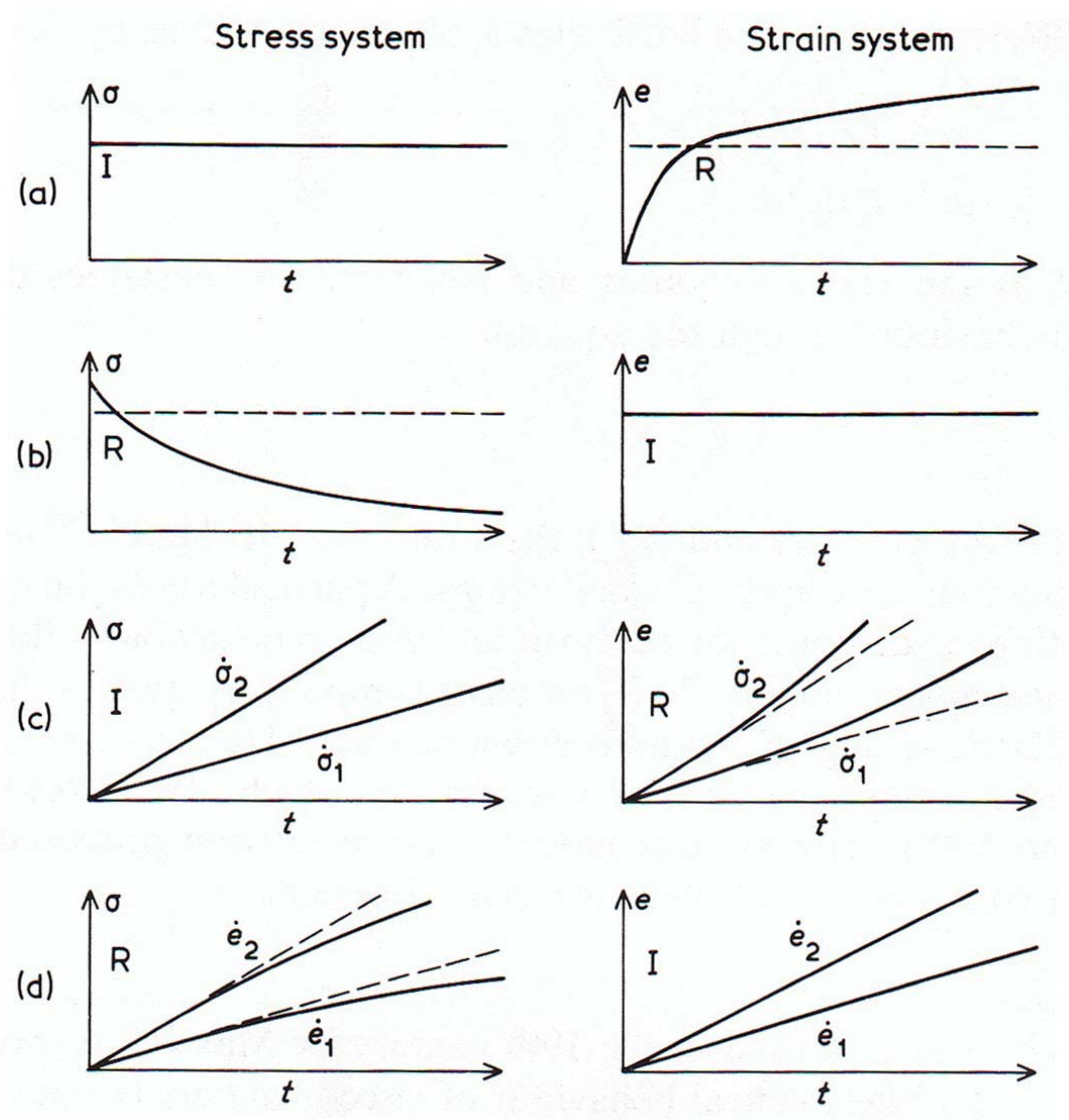
Stress relaxation



Creep

Stress relaxation

Constant stressing rate



Creep

Stress relaxation

Constant stressing rate

Constant straining rate

Acknowledgements

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TA Instruments – Waters, Inc

For graphs and figures