## Digital Logic Gates

| Name | Algebraic equation | Truth table |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | X | Y | F |
| AND | $\mathrm{F}=\mathrm{XY}$ | 0 | 0 | 0 |
|  |  | 0 | 1 | 0 |
|  |  | 1 | 0 | 0 |
|  |  | 1 | 1 | 1 |
| OR | $\mathrm{F}=\mathrm{X}+\mathrm{Y}$ | 0 | 0 | 0 |
|  |  | 0 | 1 | 1 |
|  |  | 1 | 0 | 1 |
|  |  | 1 | 1 | 1 |
| NOT <br> (inverter) <br> Buffer | $\mathrm{F}=\overline{\mathrm{X}}$ | 0 |  | 1 |
|  |  | 1 |  | 0 |
|  | $\mathrm{F}=\mathrm{X}$ | 0 |  | 0 |
|  |  | 1 |  | 1 |
| NAND | $F=\overline{X \cdot Y}$ | 0 | 0 | 1 |
|  |  | 0 | 1 | 1 |
|  |  | 1 | 0 | 1 |
|  |  | 1 | 1 | 0 |
| NOR | $\mathrm{F}=\overline{\mathrm{X}+\mathrm{Y}}$ | 0 | 0 | 1 |
|  |  | 0 | 1 | 0 |
|  |  | 1 | 0 | 0 |
|  |  | 1 | 1 | 0 |
| XOR <br> (Exclusive-OR) | $\begin{aligned} F & =X \bar{Y}+\bar{X} Y \\ & =X \oplus Y \end{aligned}$ | 0 | 0 | 0 |
|  |  | 0 | 1 | 1 |
|  |  | 1 | 0 | 1 |
|  |  | 1 | 1 | 0 |
| XNOR <br> (Exclusive-NOR) | $\begin{aligned} \mathrm{F} & =\mathrm{XY}+\overline{\mathrm{XY}} \\ & =\overline{\mathrm{X} \oplus \mathrm{Y}} \end{aligned}$ | 0 | 0 | 1 |
|  |  | 0 | 1 | 0 |
|  |  | 1 | 0 | 0 |
|  |  | 1 | 1 | 1 |

## Additional identities

| $\mathrm{X} \oplus 0$ | $=\mathrm{X}$ | $\mathrm{X} \oplus 1$ | $=\bar{X}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{X} \oplus \mathrm{X}$ | $=0$ | $\mathrm{X} \oplus \overline{\mathrm{X}}$ | $=1$ |
| $\mathrm{X} \oplus \overline{\mathrm{Y}}$ | $=\overline{\mathrm{X} \oplus \mathrm{Y}}$ | $\overline{\mathrm{X}} \oplus \mathrm{Y}$ | $=\overline{\mathrm{X} \oplus \mathrm{Y}}$ |

$\mathrm{A} \oplus \mathrm{B}$
$=\mathrm{B} \oplus \mathrm{A}$
$(\mathrm{A} \oplus \mathrm{B}) \oplus \mathrm{C} \quad=\mathrm{A} \oplus(\mathrm{B} \oplus \mathrm{C})$
$=\mathrm{A} \oplus \mathrm{B} \oplus \mathrm{C}$

