

# Electronic Instruments



## Disadvantages of PMMC voltmeter

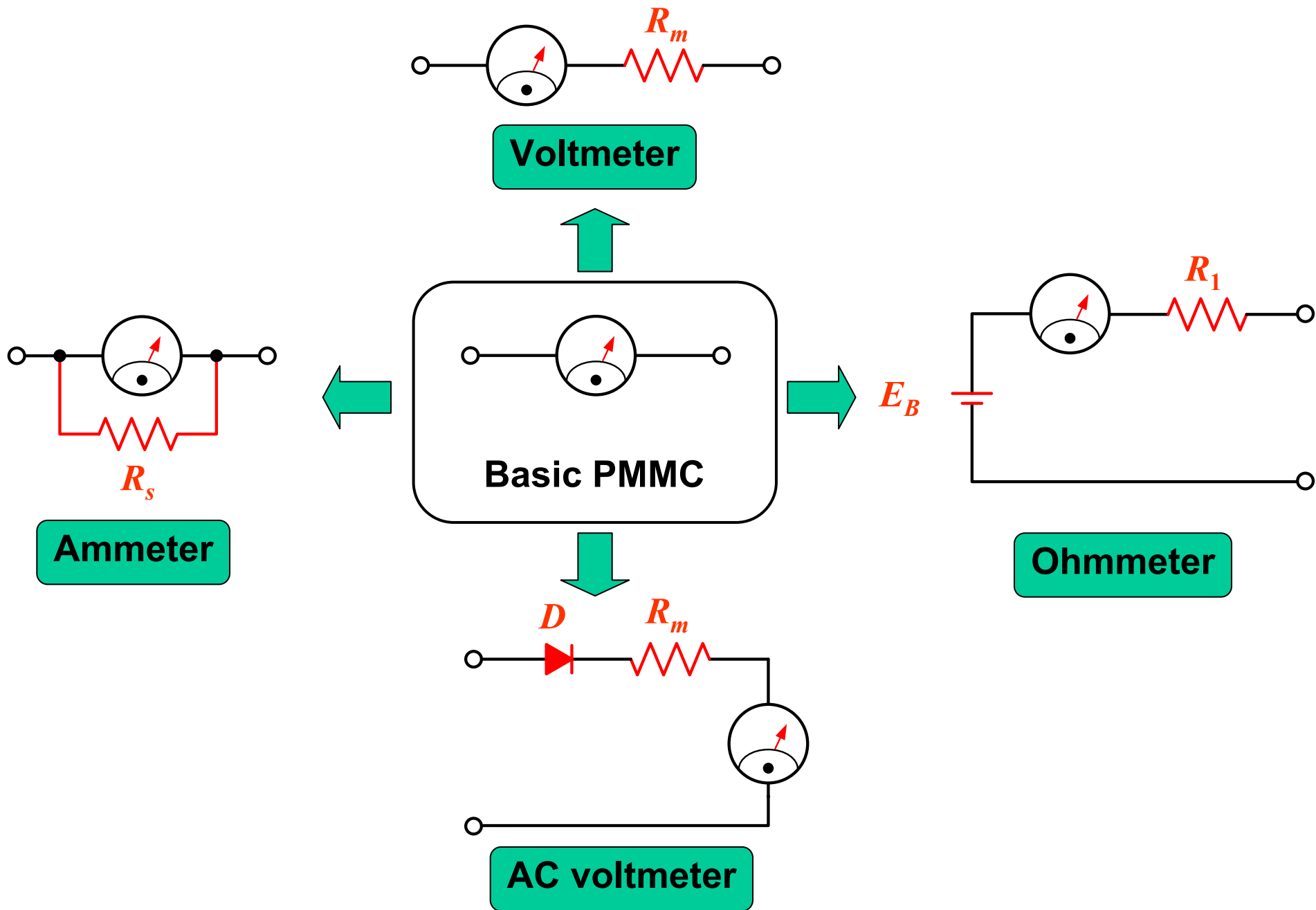
- Low input impedance: Loading effect
- Insufficient sensitivity to detect low level signal

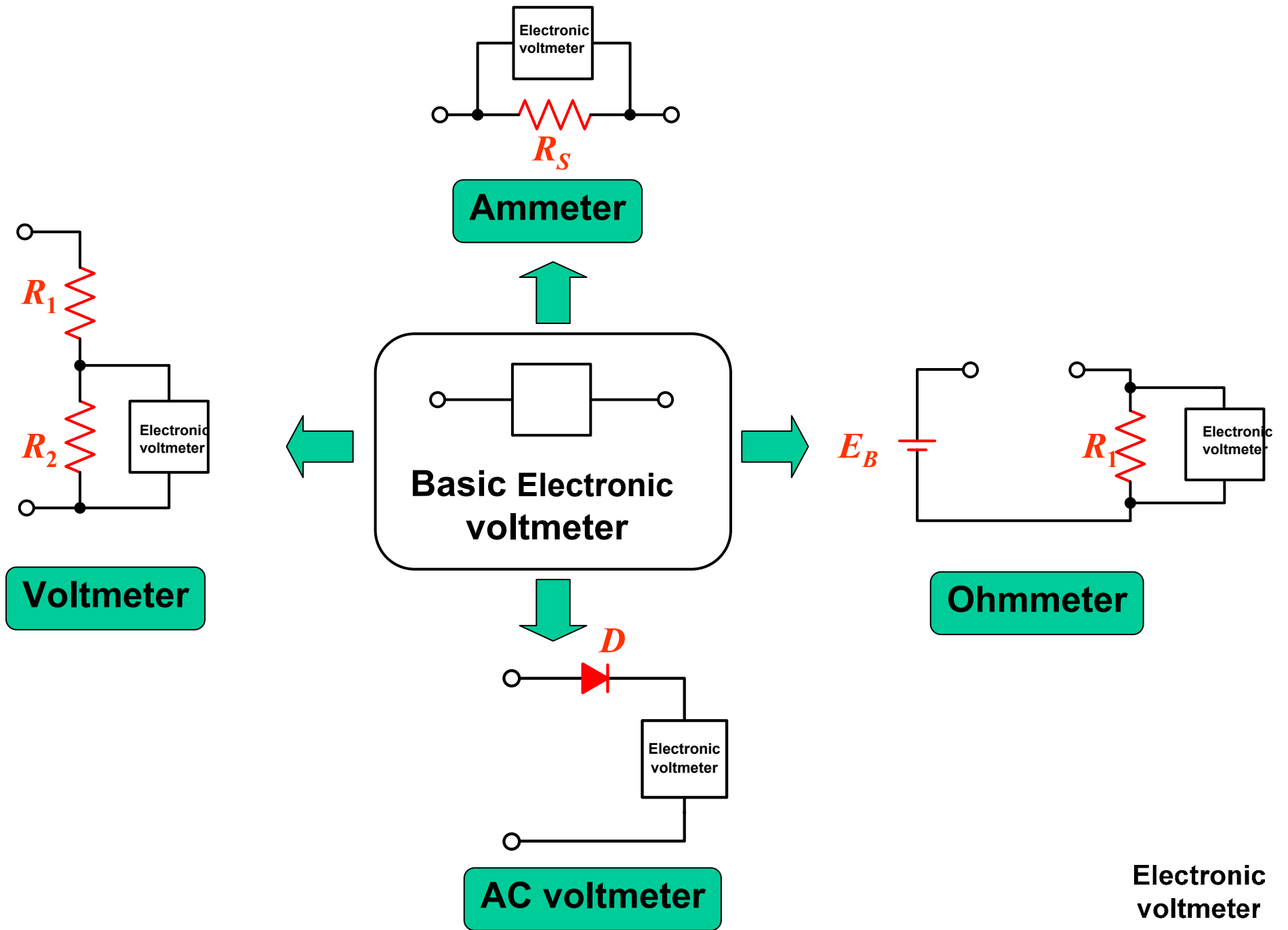
## Approach

- Utilized electronic devices such as BJT, FET or op amp to solve the above problems

## Electronic voltmeters

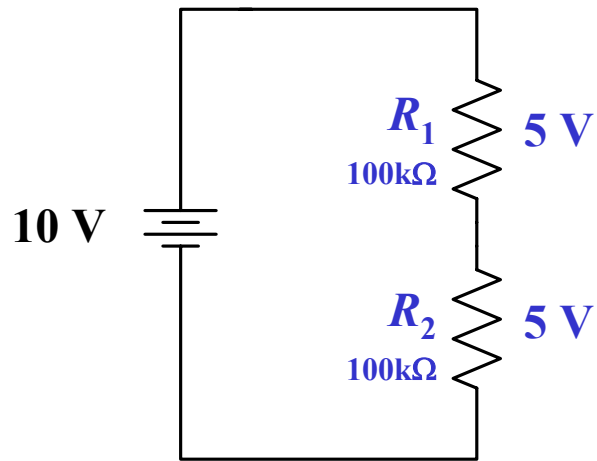
- Analog instrument
- Digital instrument



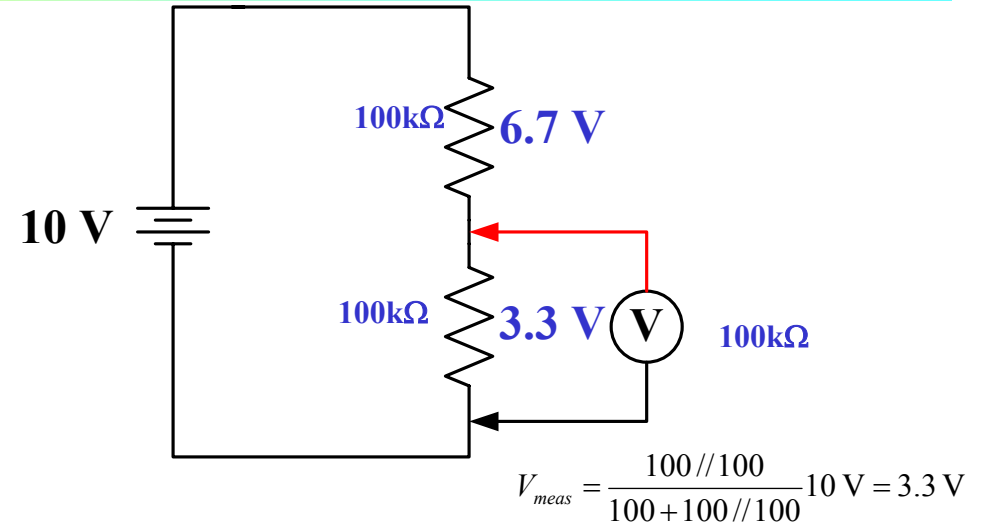


Electronic voltmeter

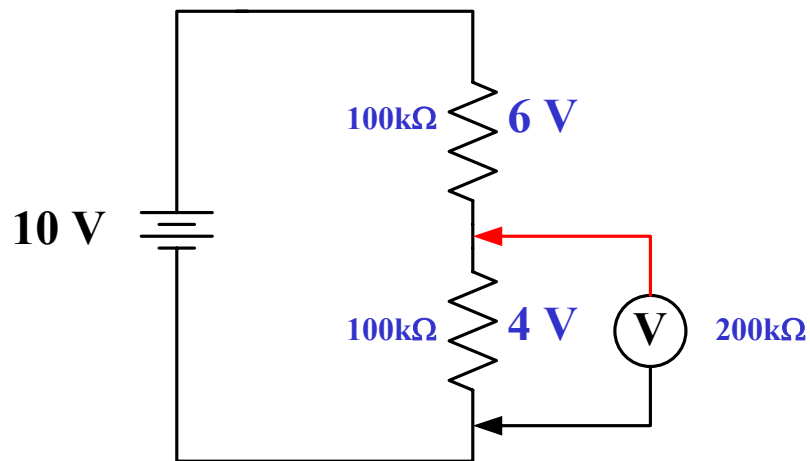
# Loading Effect



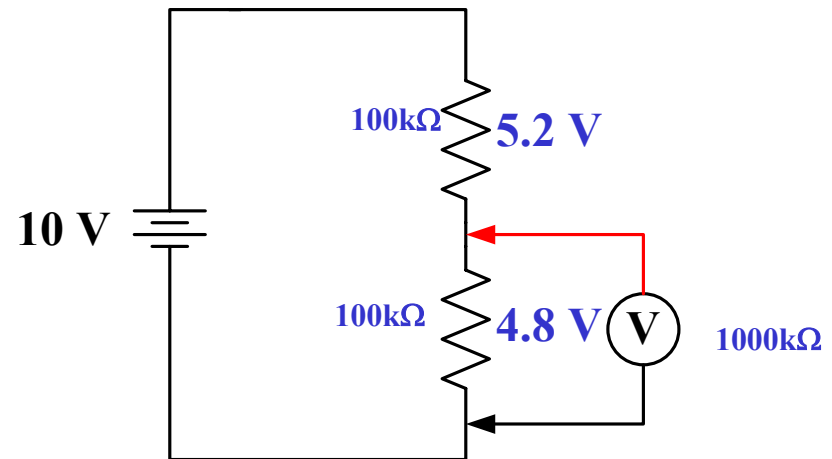
Circuit before measurement



Circuit under measurement



$$V_{meas} = \frac{200 // 100}{100 + 200 // 100} 10 \text{ V} = 4.0 \text{ V}$$

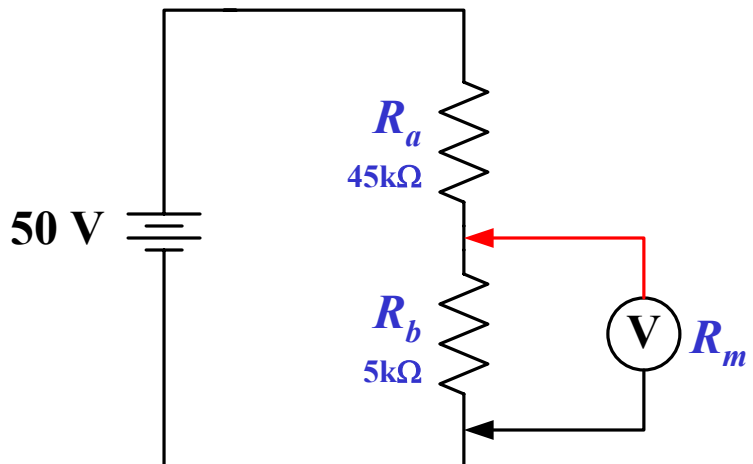


$$V_{meas} = \frac{1000 // 100}{100 + 1000 // 100} 10 \text{ V} = 4.8 \text{ V}$$

# Loading Effect

**Example** Find the voltage reading and % error of each reading obtained with a voltmeter on (i) 5 V range, (ii) 10 V range and (iii) 30 V range, if the instrument has a  $20 \text{ k}\Omega/\text{V}$  sensitivity, an accuracy 1% of full scale deflection and the meter is connected across  $R_b$

**SOLUTION** The voltage drop across  $R_b$  with output to the voltmeter connection



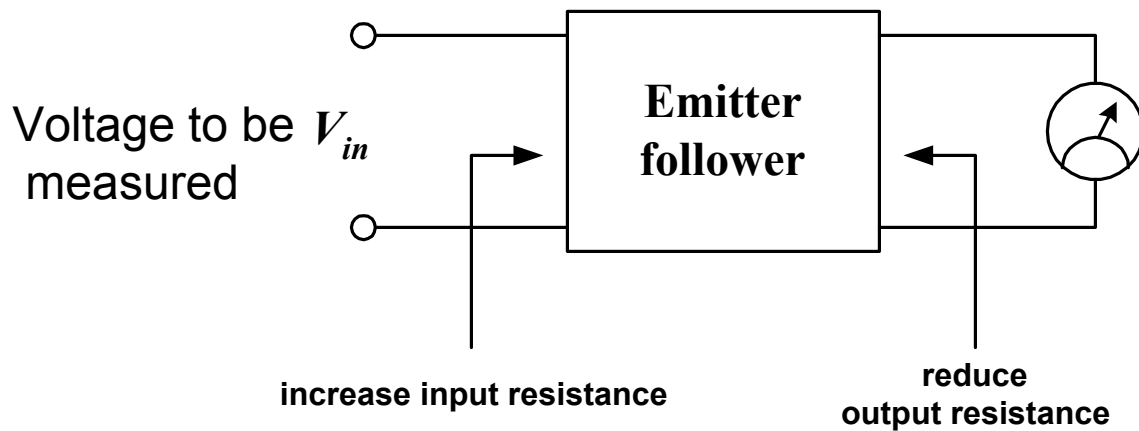
# Loading Effect

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Range (V)	$V_b$ (V)	Loading error (V)	Meter error (V)	Total error (V)	% error
5	4.78	-0.22	$\pm 0.05$	$\pm 0.27$	$\pm 5.36$
10	4.88	-0.12	$\pm 0.1$	$\pm 0.22$	$\pm 4.40$
30	4.95	-0.05	$\pm 0.3$	$\pm 0.35$	$\pm 6.10$

# Transistor Voltmeter: Emitter Follower

## Basic concept



Voltage drop across meter:  $V_m = V_{in} - V_{BE}$

where  $V_{BE}$  is base-emitter voltage  $\sim 0.7$  V for Si

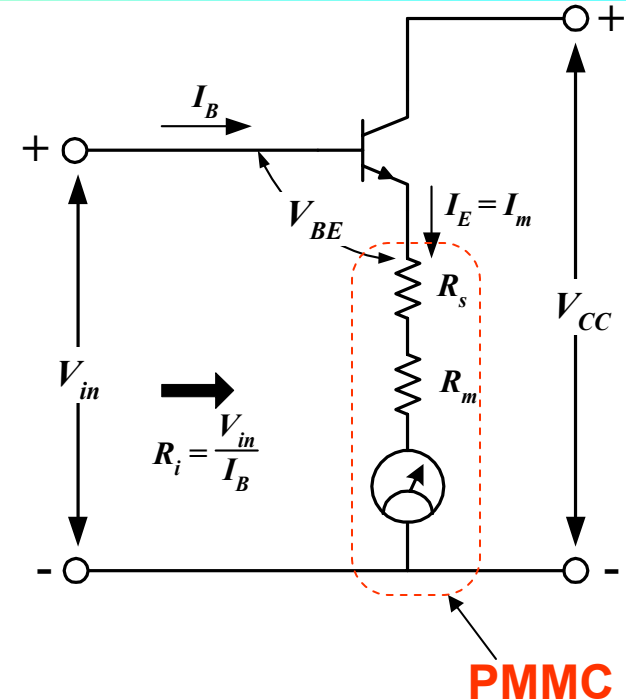
Meter current:

$$I_m = \frac{V_{in} - V_{BE}}{R_s + R_m}$$

Transistor base current:

$$I_B \approx \frac{I_E}{h_{FE}}$$

$h_{FE}$  = Transistor current gain (Typical values  $\sim 100$ - $200$ )



Schematic diagram of emitter follower

# Transistor Voltmeter: Emitter Follower

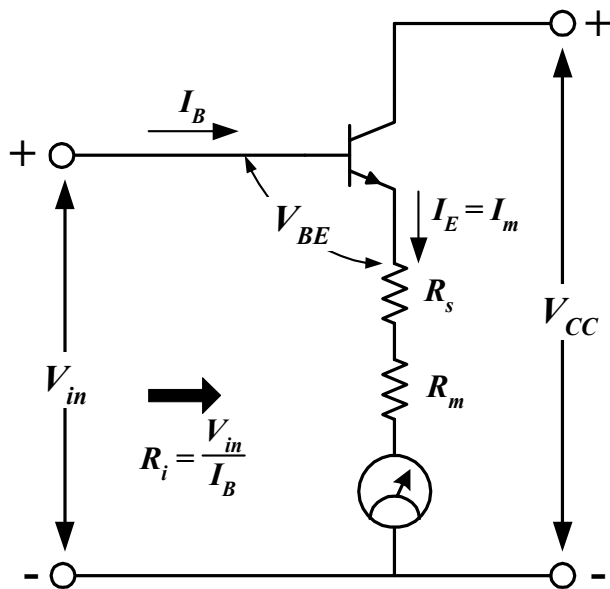
Circuit input resistance: 
$$R_i = \frac{V_{in}}{I_B} \approx h_{FE} \frac{V_{in}}{I_E} \approx h_{FE} (R_s + R_m)$$

**Example** The simple emitter-follower circuit has  $V_{CC} = 20 \text{ V}$ ,  $R_s + R_m = 9.3 \text{ k}\Omega$ ,  $I_m = 1 \text{ mA}$  at full scale, and transistor  $h_{FE} = 100$

(a) Calculate the meter current when  $V_{in} = 10 \text{ V}$

(b) Determine the voltmeter input resistance with and without the transistor.

## SOLUTION



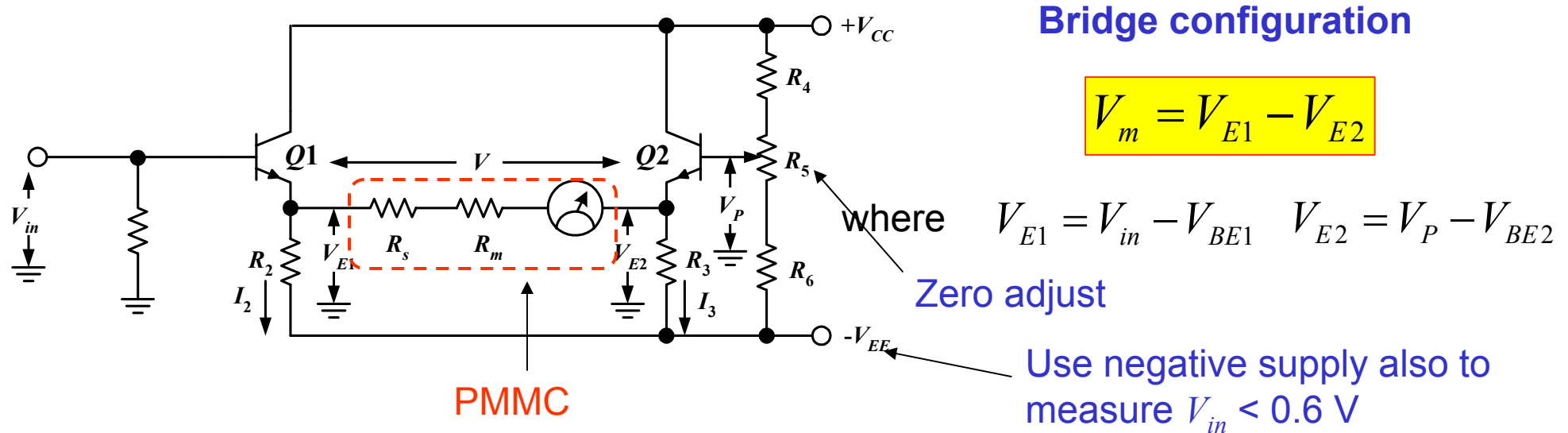


# Transistor Voltmeter: Emitter Follower

\*The base-emitter voltage drop ( $V_{BE}$ ) introduces some limitations in using emitter follower as a voltmeter:

- The circuit cannot measure the input voltage less than 0.6 V
- a non-proportional deflection: error

From the above experiment, if we apply  $V_{in}$  with 5 V, the meter should read half of full scale i.e.  $I_m = 0.5$  mA. But, the simple calculation shows that  $I_m = 0.46$  mA



Practical emitter-follower voltmeter using second transistor  $Q_2$  and voltage divider  $R_4$ ,  $R_5$  and  $R_6$  to eliminate  $V_{BE}$  error in  $Q_1$

# Transistor Voltmeter: Emitter Follower

At the condition of  $V_{in} = 0$ ,  $V_p$  should be set to give zero meter reading,  $V_m = 0$ .  
Therefore, the potentiometer  $R_5$  is for the zero adjust.

If transistors  $Q_1$  and  $Q_2$  are identical,  $V_{BE1} = V_{BE2}$

$$V_m = V_{E1} - V_{E2} = V_{in} - V_{BE1} - (V_p - V_{BE2}) = V_{in} - V_p$$

At  $V_{in} = 0 \rightarrow V_m = 0$ , give  $V_p = 0$

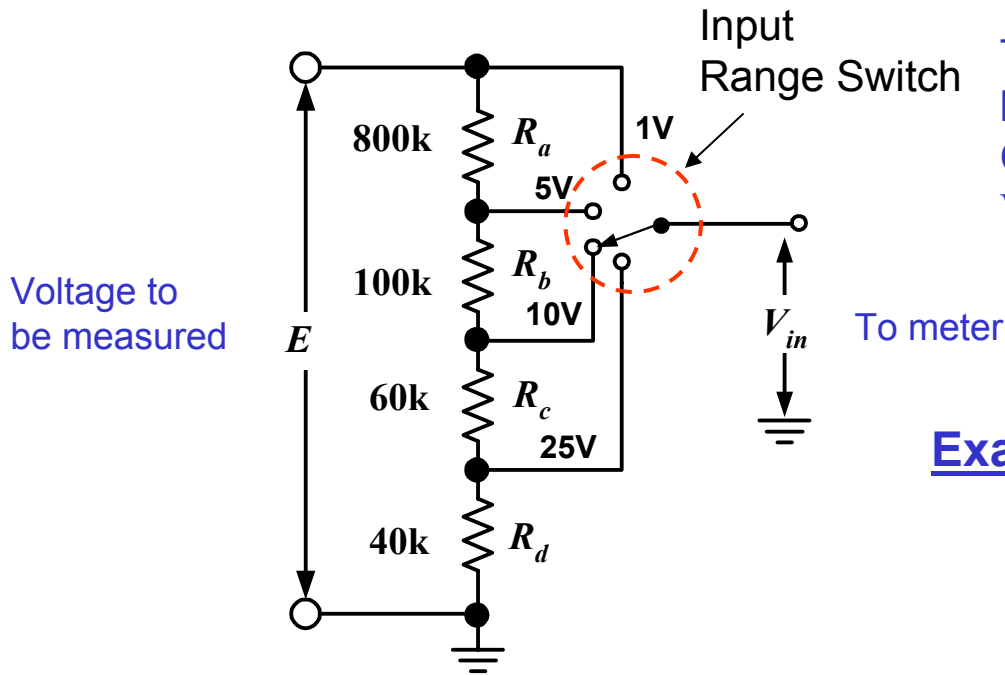
Consequently, if  $V_p$  is set properly,  $V_m$  will be the same as  $V_{in}$

**Example** An emitter-follower voltmeter circuit as shown in the previous picture has  $R_2 = R_3 = 3.9 \text{ k}\Omega$  and supply with  $\pm 12 \text{ V}$ . Calculate the meter circuit voltage when  $V_{in} = 1 \text{ V}$  and when  $V_{in} = 0.5 \text{ V}$ . Assume, both transistors have  $V_{BE} = 0.7 \text{ V}$

**SOLUTION** when  $V_{in} = 1 \text{ V}$

when  $V_{in} = 0.5 \text{ V}$

# Voltage Range Changing: Input Attenuator



The input attenuator accurately divides the voltage to be measured before it is applied to the input transistor. Calculation shows that the input voltage  $V_{in}$  is always 1 V when the maximum input is applied on any range

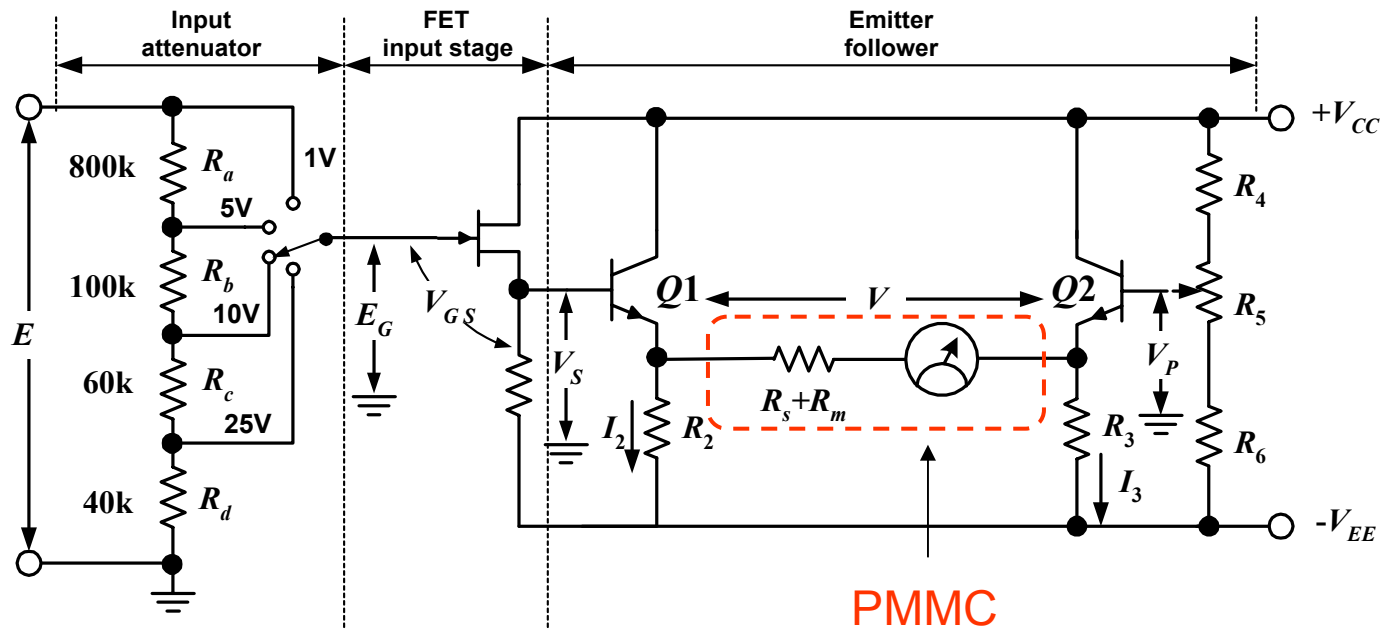
**Example** On the 5 V range:

$$\begin{aligned} V_{in} &= 5 \text{ V} \times \frac{R_b + R_c + R_d}{R_a + R_b + R_c + R_d} \\ &= 5 \text{ V} \times \frac{100 \text{ k}\Omega + 60 \text{ k}\Omega + 40 \text{ k}\Omega}{800 \text{ k}\Omega + 100 \text{ k}\Omega + 60 \text{ k}\Omega + 40 \text{ k}\Omega} \\ &= 1 \text{ V} \end{aligned}$$

The measurement point always sees a constant input resistance of 1 MΩ

# FET Input Voltmeter

The addition of FET at the input gives higher input resistance than can be achieved with a bipolar transistor



**A FET Input Voltmeter**

$$V_m = V_{E1} - V_{E2}$$

where  $V_{E1} = E_G - V_{GS} - V_{BE1}$

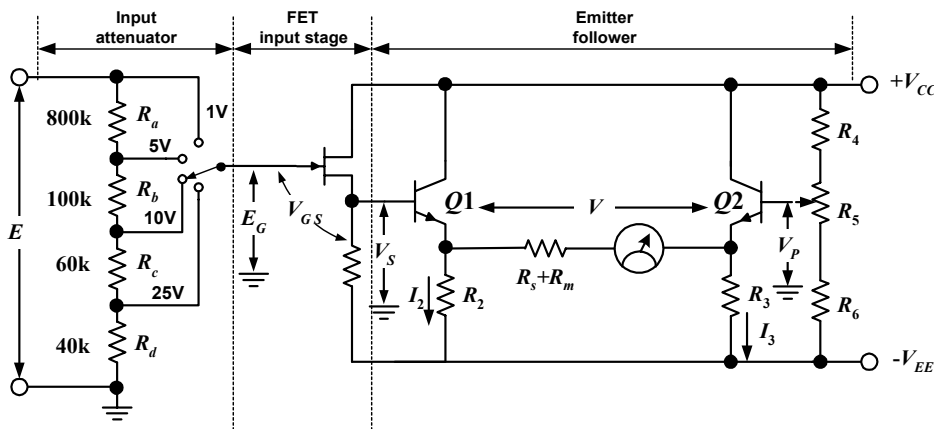
$$V_{E2} = V_P - V_{BE2}$$

In general, it is not simple to calculate  $V_{GS}$ , for simplicity, we assume that  $V_{GS}$  will be given.

# FET Input Voltmeter

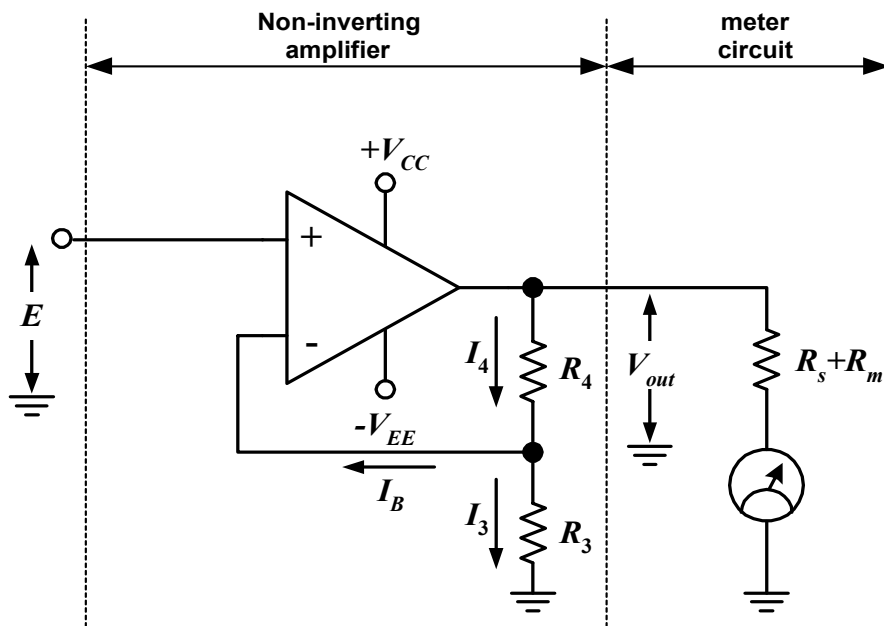
**Example** Determine the meter reading for the FET input voltmeter in the previous figure, when  $E = 7.5 \text{ V}$  and the meter is set to its 10 V range. The FET gate-source voltage is  $-5 \text{ V}$ ,  $V_P = 5 \text{ V}$ ,  $R_s + R_m = 1 \text{ k}\Omega$  and  $I_m = 1 \text{ mA}$  at full scale

**SOLUTION** On the 10 V range:



# Operational Amplifier Voltmeter

## Op-Amp Amplifier Voltmeter



$$V_{out} = \left(1 + \frac{R_4}{R_3}\right)E$$

The voltage gain

$$A_v = \left(1 + \frac{R_4}{R_3}\right)$$

Selection of  $R_3$  and  $R_4$

$$R_3 = \frac{E}{I_3}$$

and

$$R_4 = \frac{V_{out} - E}{I_3}$$

The non-inverting amplifier gives a very high input impedance and very low output impedance. Therefore, the loading effect can be neglected. Furthermore, it can provide gain with enabling to measure low level input voltage.

# Operational Amplifier Voltmeter

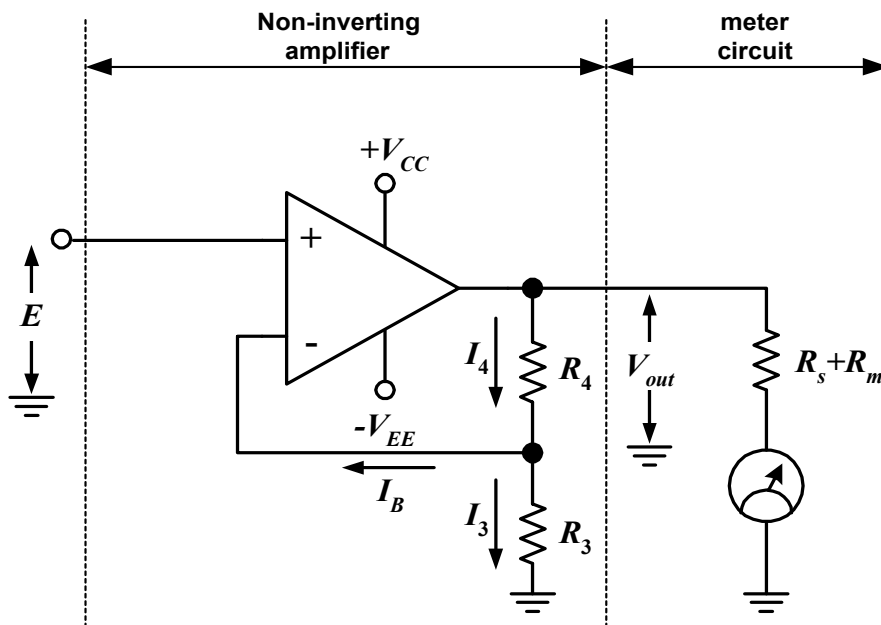
**Example** Design an op-amp Voltmeter circuit which can measure a maximum input of 20 mV. The op-amp input current is  $0.2 \mu\text{A}$ , and the meter circuit has  $I_m = 100 \mu\text{A}$  FSD and  $R_m = 10 \text{ k}\Omega$ . Determine suitable resistance values for  $R_3$  and  $R_4$

## SOLUTION

To neglect the effect of  $I_B$ , the condition of  $I_4 \gg I_B$  must be satisfied. The rule of thumb suggested  $I_4$  should be at least 100 times greater than  $I_B$

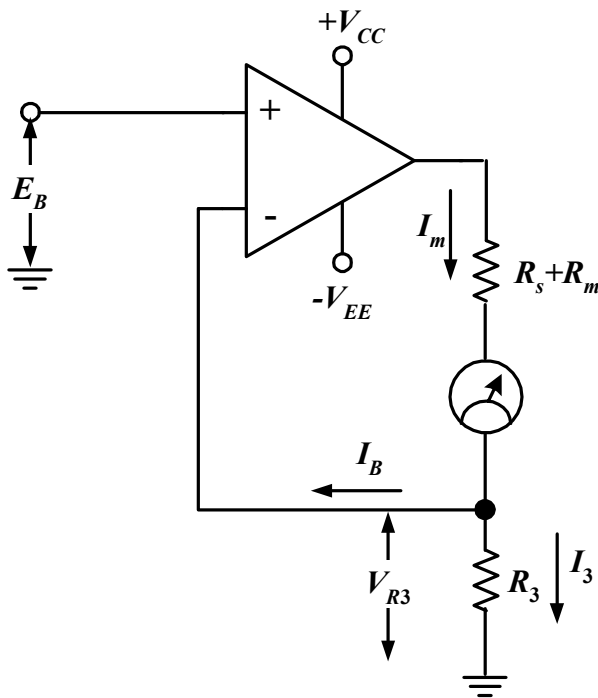
Select  $I_4 = 1000 \times I_B = 1000 \times 0.2 \mu\text{A} = 0.2 \text{ mA}$

At full scale:  $I_m = 100 \mu\text{A}$



# Operational Amplifier Voltmeter

## Op-Amp Amplifier Voltmeter: voltage to current converter



Since  $I_3 \gg I_B$ , therefore  $I_m = I_3$

Meter current

$$I_m = I_3 = \frac{E}{R_3}$$

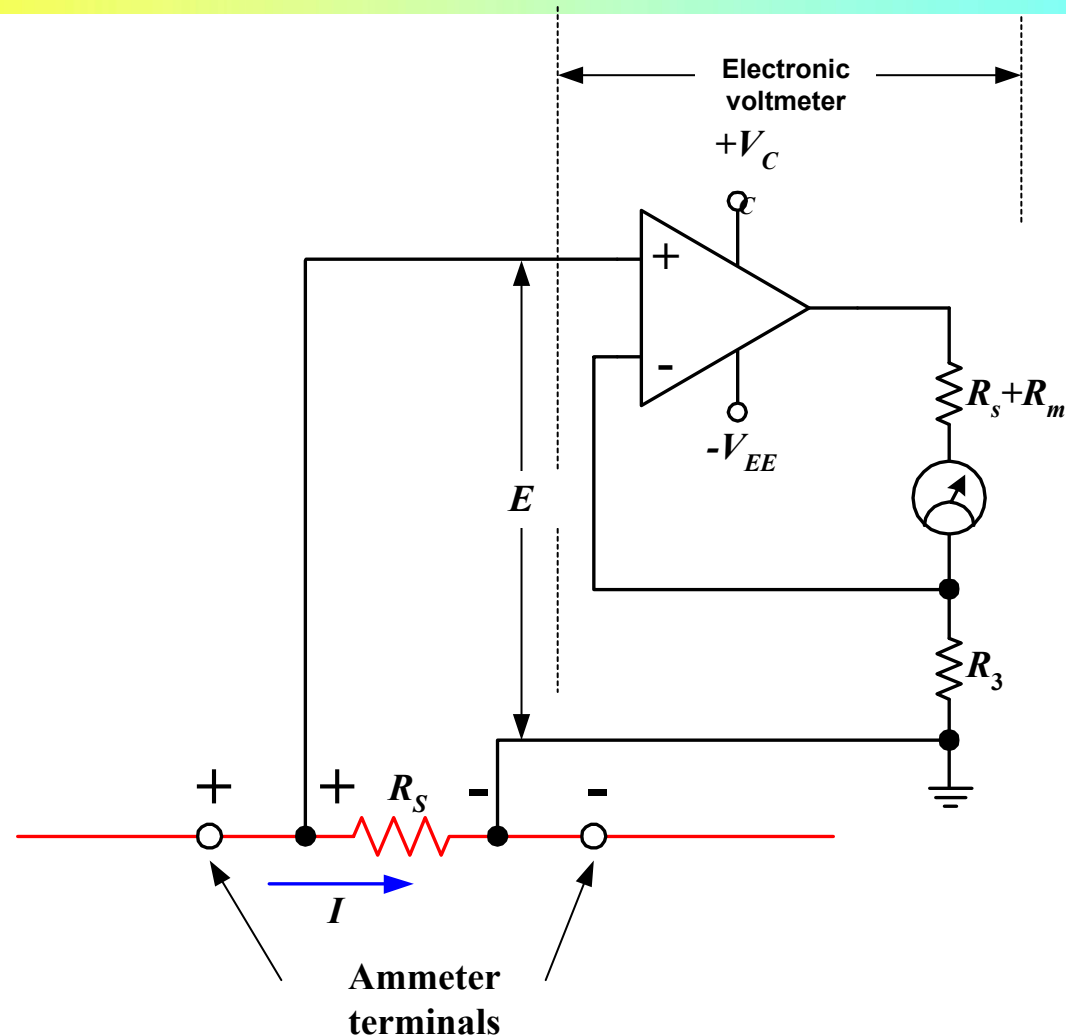
Meter voltage

$$V_m = \frac{R_m}{R_3} E$$

if  $R_m > R_3$ , voltage  $E$  is amplified by the ratio of  $R_m/R_3$

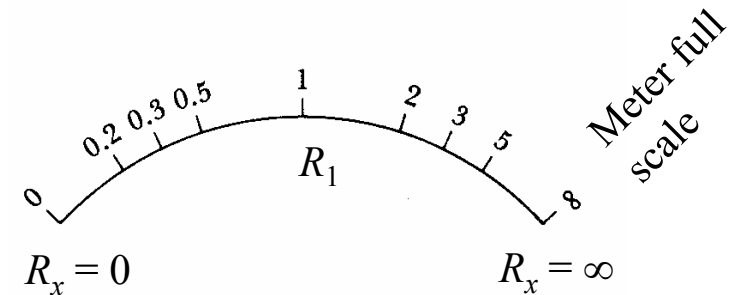
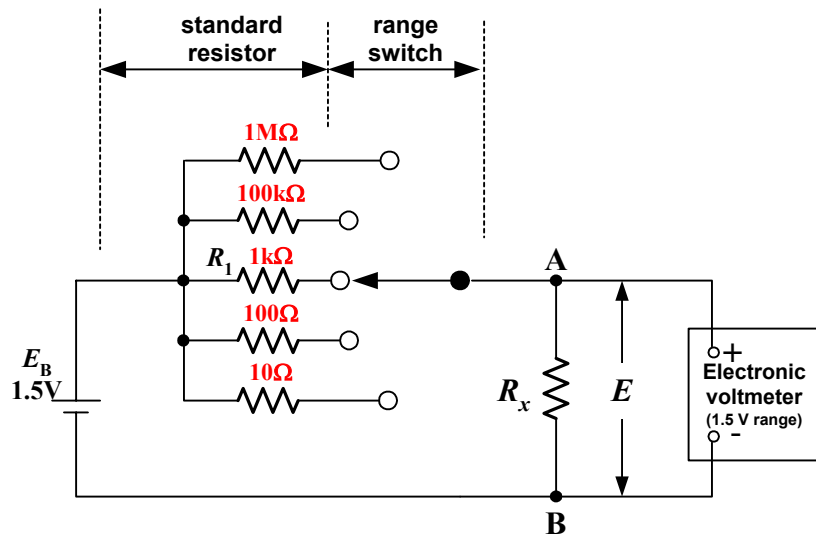


# Current Measurement with Electronic Voltmeter



An electronic voltmeter can be used for current measurement by measuring the voltage drop across a shunt ( $R_s$ ). The instrument scale is calibrated to indicate current.

# Electronic Ohmmeter: Series Connection



Ohmmeter scale for electronic instrument

## Series Ohmmeter for electronic instrument

At  $R_x = \infty$  or open circuit, the voltmeter indicate full scale deflection ( $E = 1.5 \text{ V}$ ) and  $R_x = 0$  or shorted circuit, since  $E = 0$ , no deflection is observed. At other values of resistance, the battery voltage  $E_B$  is potentially divided across  $R_1$  and  $R_x$ , given by

$$E = E_B \frac{R_x}{R_1 + R_x}$$

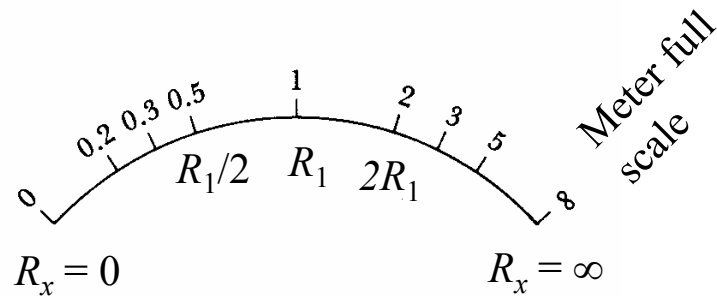
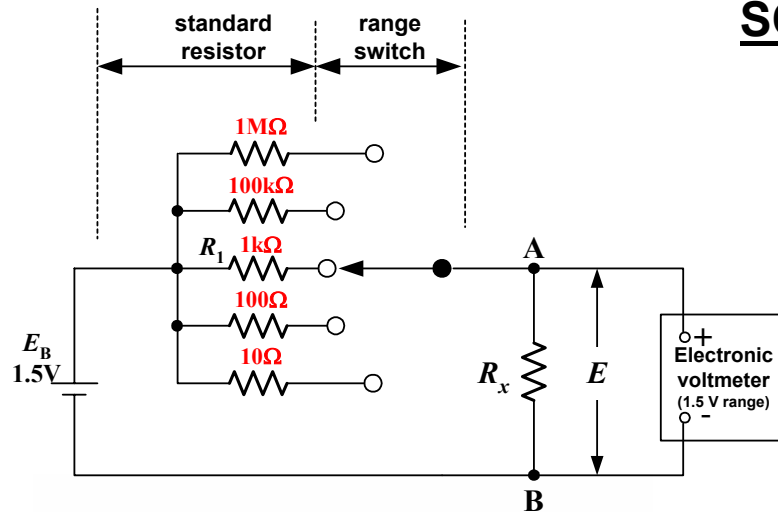
Suppose that  $R_1$  is set to  $1 \text{ k}\Omega$

$$E = 1.5 \text{ V} \times \frac{1 \text{ k}\Omega}{1 \text{ k}\Omega + 1 \text{ k}\Omega} = 0.75 \text{ V} \quad (50\% \text{ deflection})$$

Thus if  $R_x = R_1$ , half scale will be indicated

# Electronic Ohmmeter: Series Connection

**Example** For the electronic ohmmeter in the Figure, determine the resistance scale marking at 1/3 and 2/3 of full scale



**SOLUTION** From

$$E = E_B \frac{R_x}{R_1 + R_x}$$

Rearrange, give us

$$R_x = \frac{R_1}{\frac{E}{E_B} - 1}$$

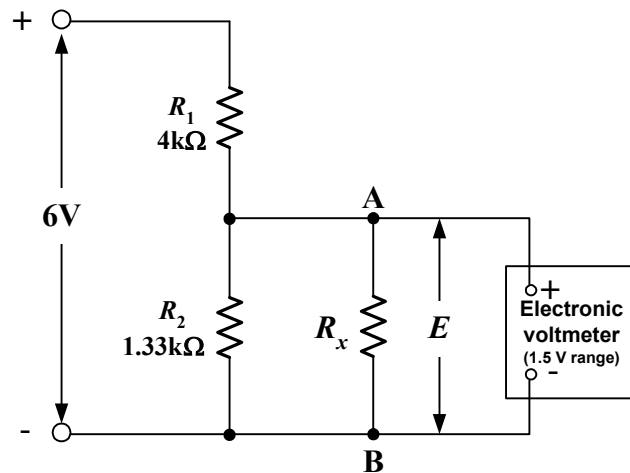
At 1/3 FSD;  $E = E_B/3$

$$R_x = \frac{R_1}{\frac{E_B/3}{E_B} - 1} = \frac{R_1}{\frac{1}{3} - 1} = \frac{R_1}{-2/3} = -\frac{3}{2}R_1$$

At 2/3 FSD;  $E = 2E_B/3$

$$R_x = \frac{R_1}{\frac{2E_B/3}{E_B} - 1} = \frac{R_1}{\frac{2}{3} - 1} = \frac{R_1}{-1/3} = -3R_1$$

# Electronic Ohmmeter: Parallel Connection



At  $R_x = \infty$  or open circuit,

$$E = E_B \frac{R_2}{R_1 + R_2}$$

$$= 6 \text{ V} \times \frac{1.33 \text{ k}\Omega}{4 \text{ k}\Omega + 1.33 \text{ k}\Omega} = 1.5 \text{ V}$$

Therefore, this circuit give FSD, when  $R_x = \infty$

When,  $R_x = 0 \Omega$ ,  $E = 0 \text{ V}$ , therefore, the meter gives no deflection.

## Shunt Ohmmeter for electronic instrument

At any value of  $R_x$

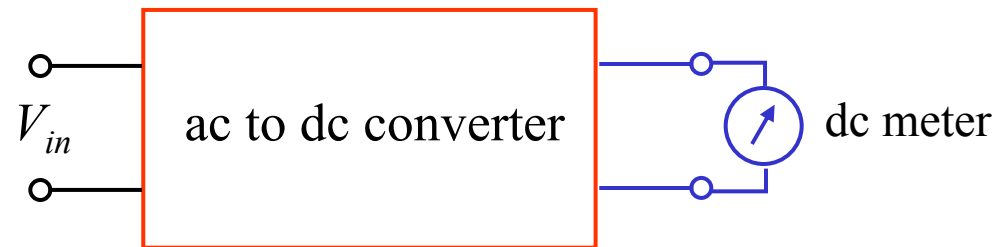
$$E = E_B \frac{R_2 \parallel R_x}{R_1 + R_2 \parallel R_x}$$

So, the meter indicates half-scale when  $R_x = R_1 \parallel R_2$

# AC Electronic Voltmeter

## Principle

Most ac measurements are made with ac-to-dc converter, which produce a dc current/voltage proportional to the ac input being measured



## Classification:

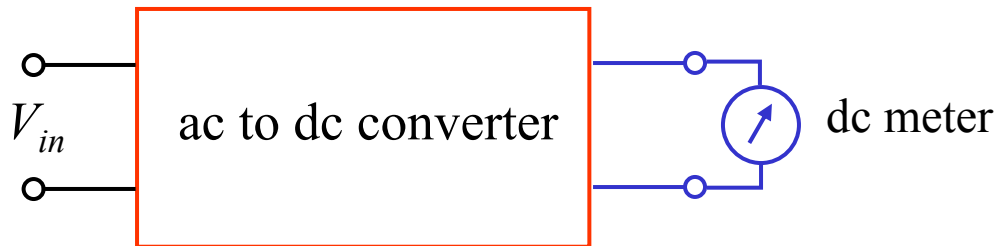
- Average responding
  - Peak responding
  - RMS responding (True rms meter)
- } periodic signal only
- any signal

# AC Electronic Voltmeter

The scale on ac voltmeters are ordinarily calibrated in rms volts

## Average responding meter

Form factor is the ratio of the rms value to the average value of the wave form



$$\text{Form Factor} = \frac{V_{rms}}{V_{average}}$$

It should be noted that the rms value is calculated from  $V_{in}$ , while the average value is calculated from the output of ac-dc converter.

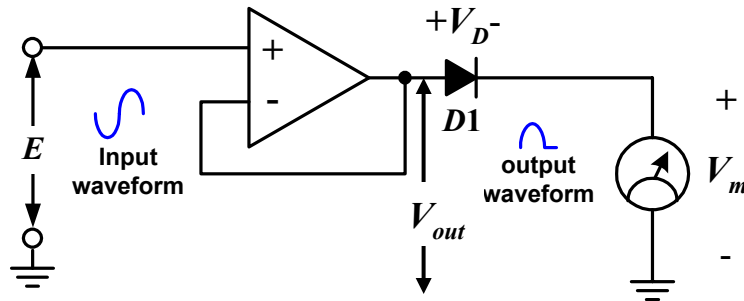
## Peak responding meter

Form factor is the ratio of the peak value to the rms value of the wave form

$$\text{Crest Factor} = \frac{V_{peak}}{V_{rms}}$$

# Average-Responding Meter

In this type of instrument, the ac signal is rectified and then fed to a dc millimeter. In the meter instrument, the rectified current is averaged either by a filter or by the ballistic characteristics of the meter to produce a steady deflection of the meter pointer.



**Conventional half-wave rectifier**

For the positive cycle,  $V_{out} = E$

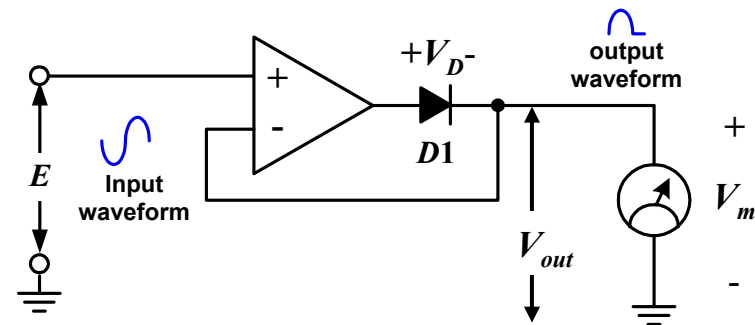
$$V_m = E - V_D$$

where  $V_D =$  cut-in voltage  $\sim 0.6-0.7$  for Si

For the negative cycle,  $V_{out} = 0$

$$V_m = 0$$

Since Diode  $D_1$  is reverse bias, no current flow through meter



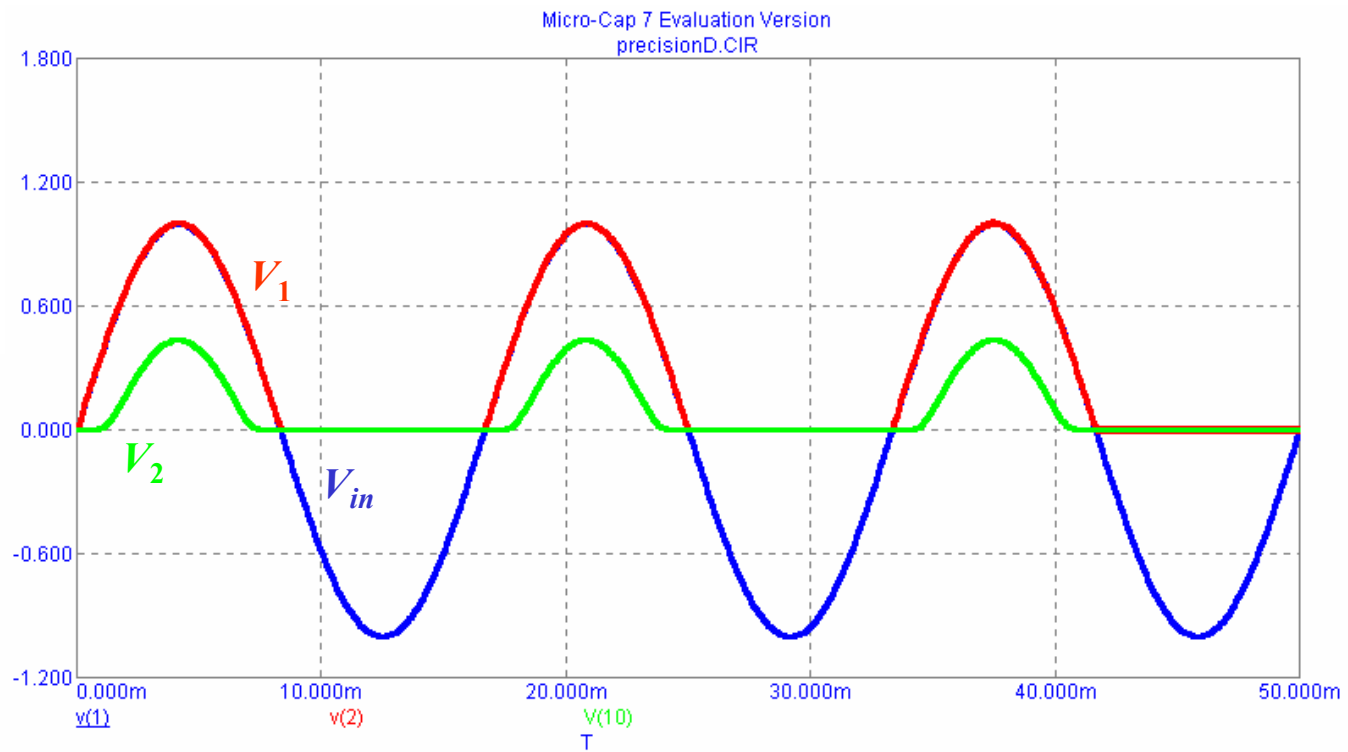
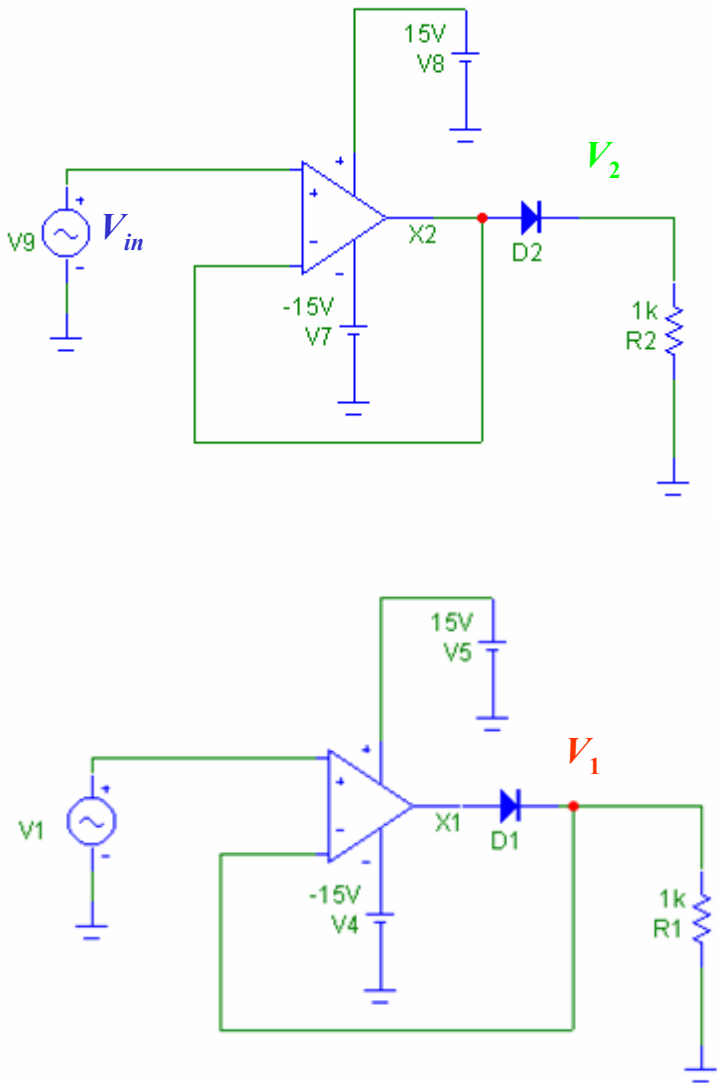
**precision rectifier**

For the positive cycle,  $V_{out} = V_m = E$

For the negative cycle,  $V_{out} = 0$

Therefore, the voltage drop in the forward bias can be compensated by this configuration

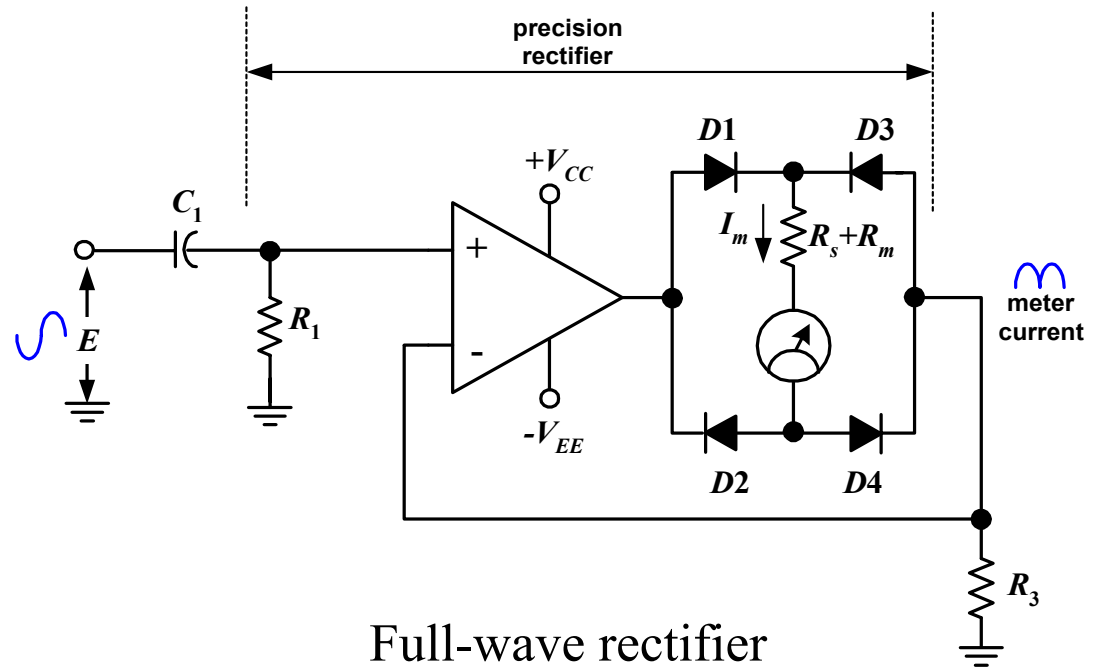
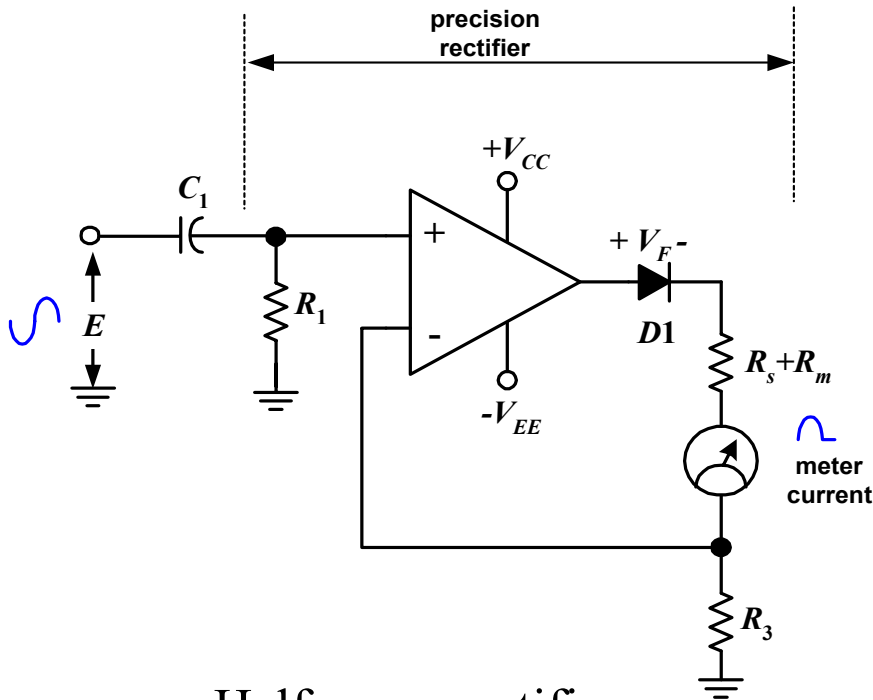
# Average-Responding Meter





# Average-Responding Voltmeter

## Voltage to current converter



Meter peak current

$$I_p = \frac{E_p}{R_3}$$

Average meter current

$$I_{av} = \frac{1}{\pi} I_p = 0.318 I_p$$

Meter peak current

$$I_p = \frac{E_p}{R_3}$$

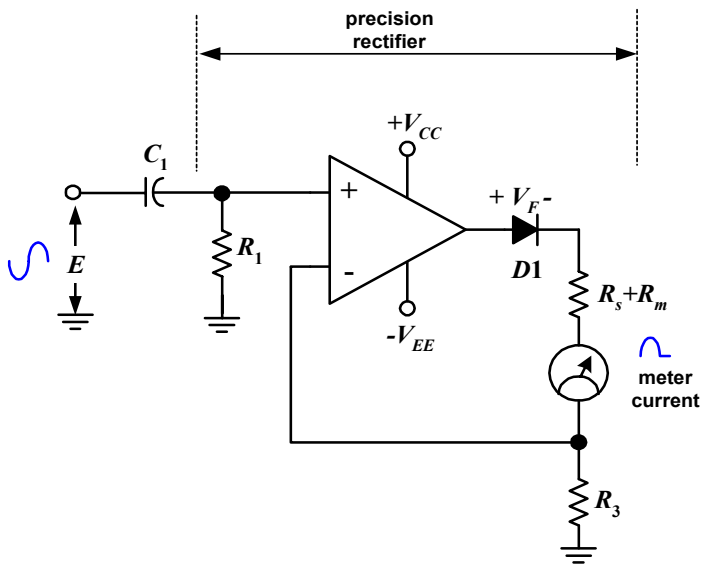
Average meter current

$$I_{av} = \frac{2}{\pi} I_p = 0.637 I_p$$

# Average-Responding Voltmeter

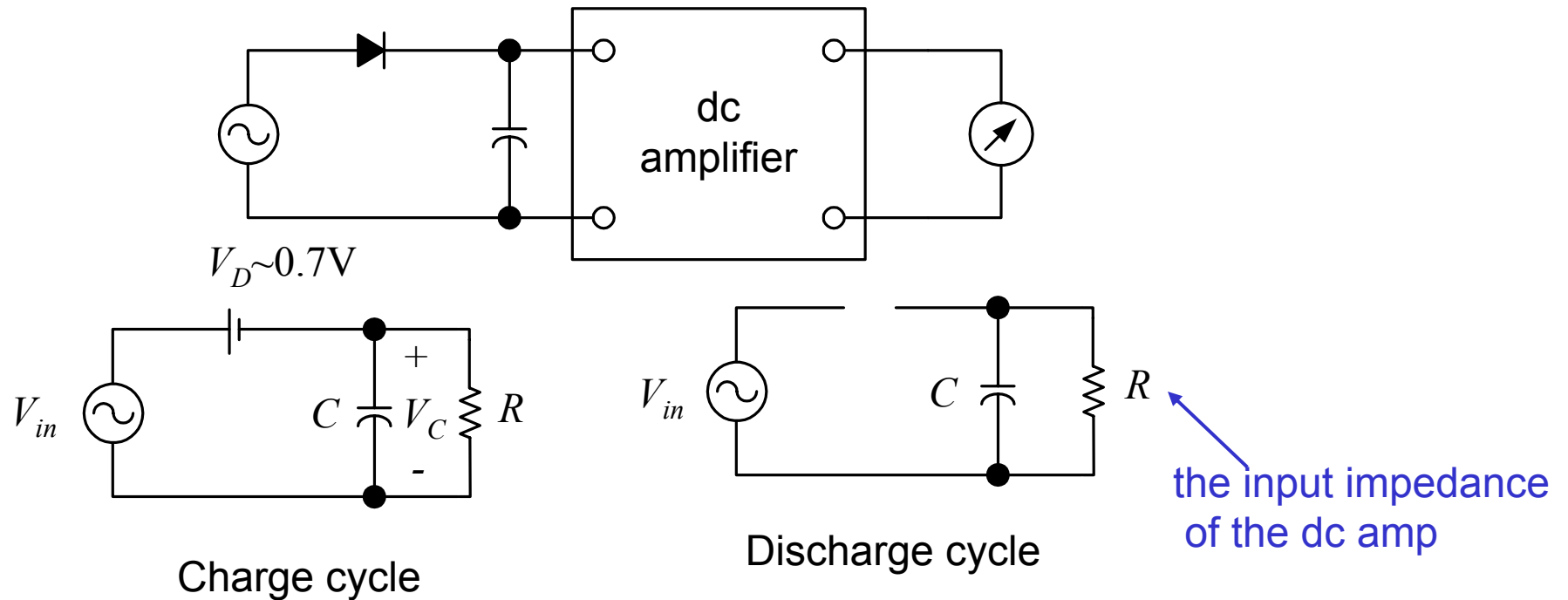
**Example** The half-wave rectifier electronic voltmeter circuit uses a meter with a FSD current of 1 mA. The meter a coil resistance is 1.2 k $\Omega$ . Calculate the value of  $R_3$  that will give meter full-scale pointer deflection when the ac input voltage is 100 mV (rms). Also determine the meter deflection when the input is 50 mV.

**SOLUTION** at FSD, the average meter current is 1 mA



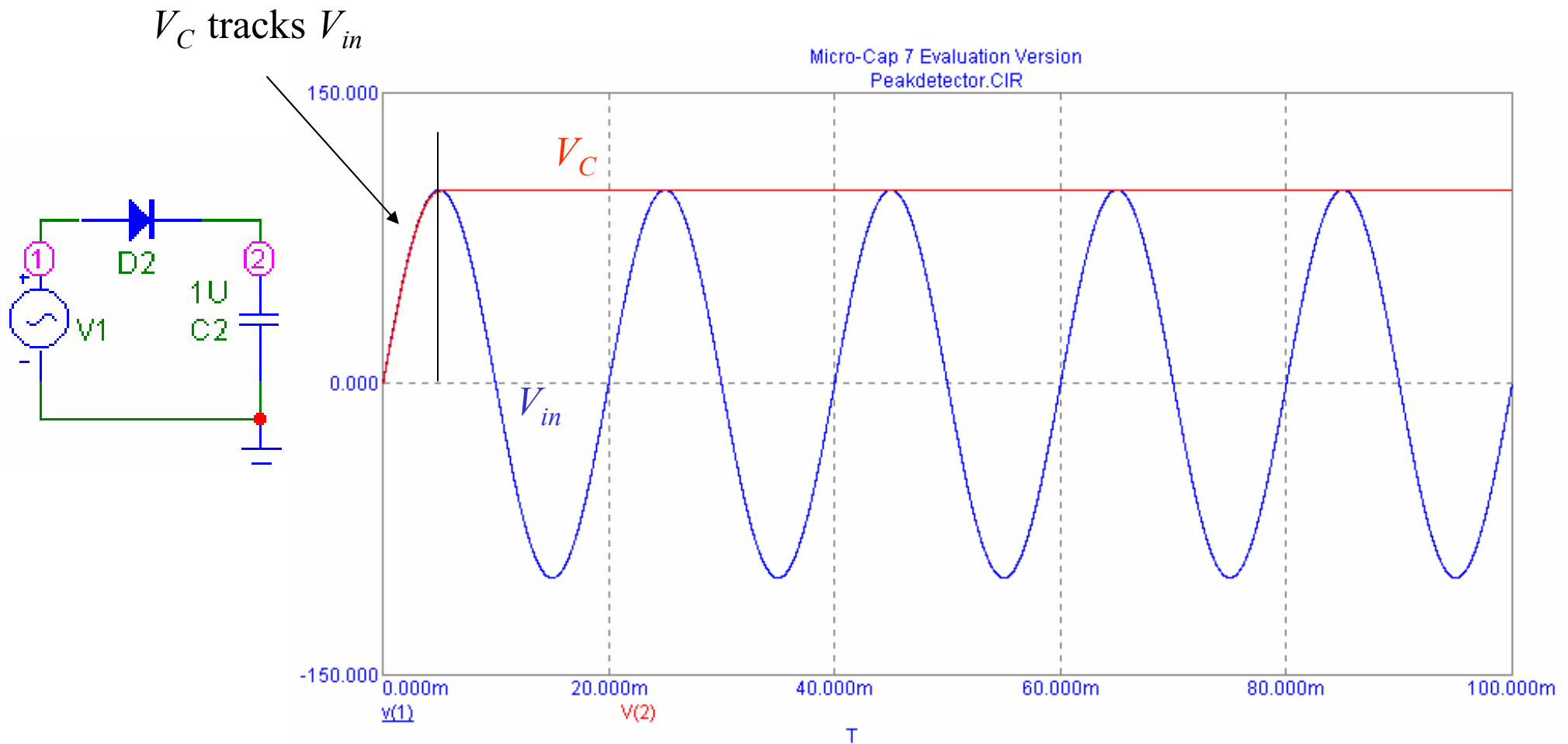
# Peak-Responding Voltmeter

The primary difference between the peak-responding voltmeter and the average-responding voltmeter is the use of a storage capacitor with the rectifying diode.



In the first positive cycle:  $V_C$  tracks  $V_{in}$  with the difference of  $V_D$ , until  $V_{in}$  reaches its peak value. After this point, diode is reversed bias and the circuit keeps  $V_C$  at  $V_p - V_D$ . The effect of discharging through R will be minimized if its value is large enough to yield that  $RC \gg T$ .

# Peak-Responding Voltmeter

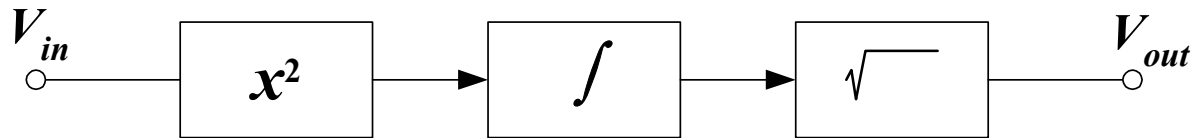


# RMS-Responding Voltmeter

Suitable for: low duty-cycle pulse trains  
voltages of undetermined waveform

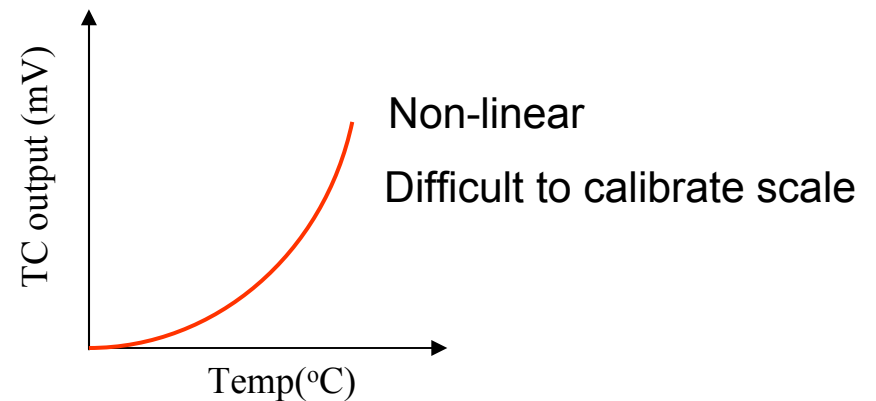
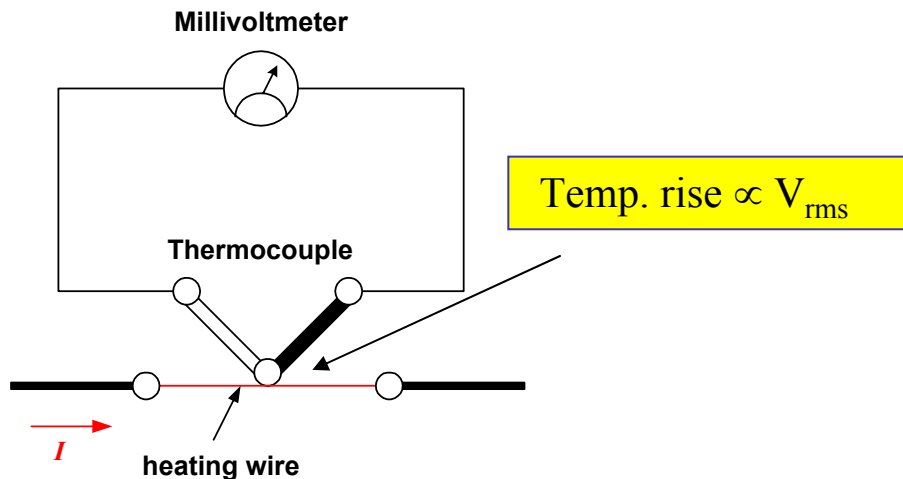
**RMS value definition: Mathematic**

$$V_{rms} = \sqrt{\frac{1}{T} \int_0^T v^2(t) dt}$$



**RMS value definition: Physical**

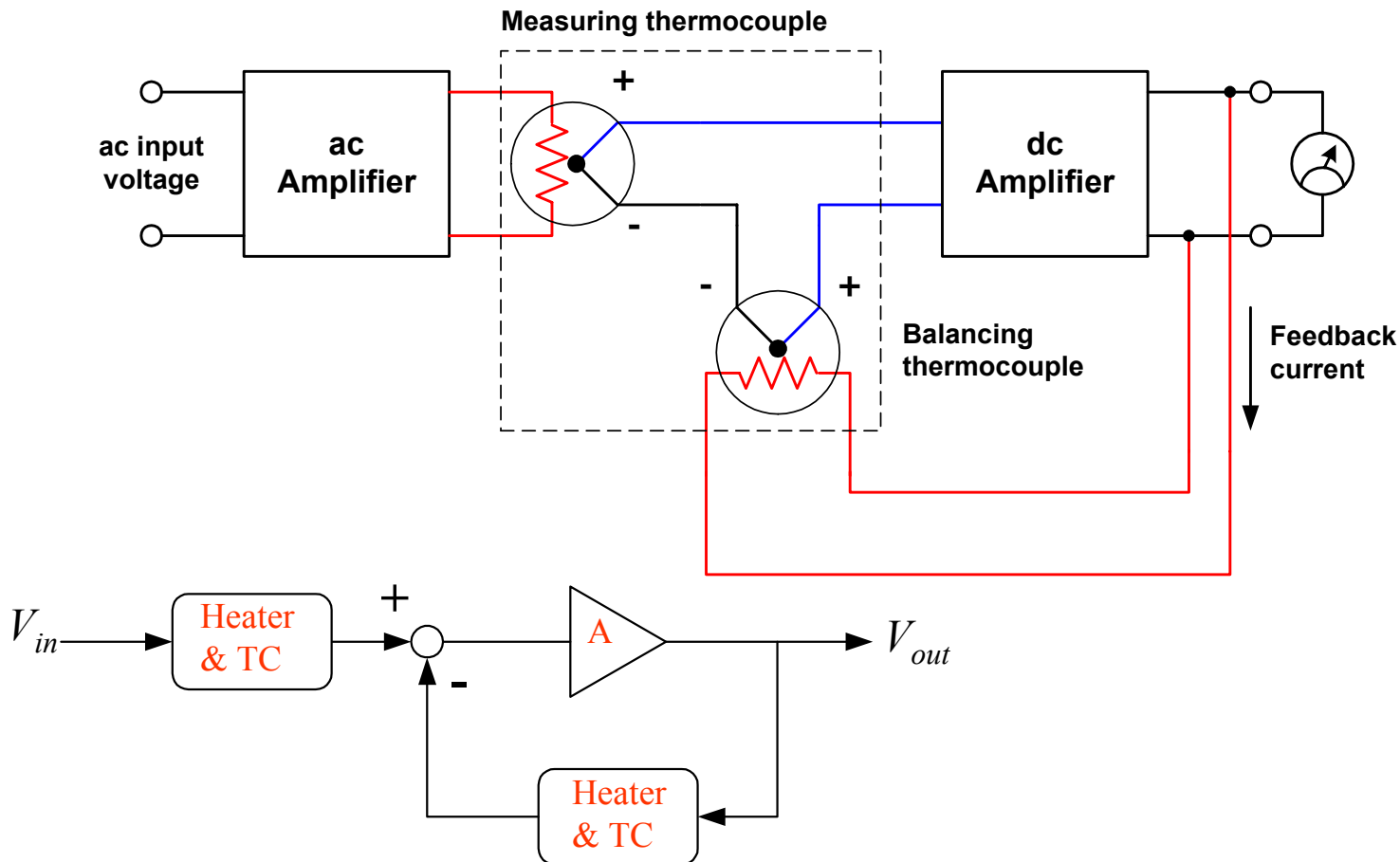
rms voltage is equivalent to a dc voltage which generates the same amount of heat power in a resistive load that the ac voltage does.



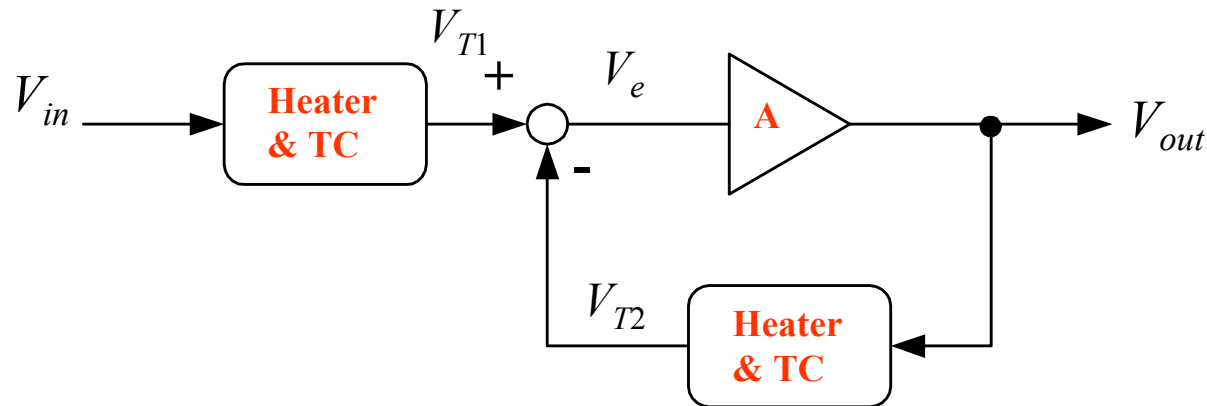
# RMS-Responding Voltmeter

## Null-balance technique: non-linear cancellation

Compare the heating power generated by input voltage to the heating power generated the dc amplifier



# Negative Feedback



$$V_{out} = V_e = A(V_{T1} - V_{T2})$$

Let,  $V_{T1} = k V_{in}$  and  $V_{T2} = k V_{out}$  where  $k$  is proportional constant of the heater and TC in the system. Note that  $k$  may depend on the level of the input signal

$$V_{out} = A(kV_{in} - kV_{out})$$

$$\frac{V_{out}}{V_{in}} = \frac{Ak}{1 + Ak}$$

If  $A$  is large  $\longrightarrow$

$$V_{out} \approx V_{in}$$

If the amplifier gain is very large,  $V_{out}$  is equal to  $V_{in}$ , this means that the dc voltage output is therefore equal to the effective, or rms value of the input voltage