

## Symbolic computation

**float**      แสดงผลการคำนวณเป็นตัวเลข

$$\frac{\frac{25}{4} + \frac{12}{5}}{\frac{7}{9}} \text{ float, 10} \rightarrow 11.12142857$$

$$\frac{\frac{25}{4} + \frac{12}{5}}{\frac{7}{9}} = 11.121$$

$$\frac{\frac{25}{4} + \frac{12}{5}}{\frac{7}{9}} \rightarrow \frac{1557}{140}$$

**complex** แสดงผลการคำนวณเป็นจำนวนเชิงซ้อน

$$\frac{\frac{25}{4} + \frac{12 \cdot i}{5}}{\frac{7}{9}} = 8.036 + 3.086i$$

$$\frac{\frac{25}{4} + \frac{12 \cdot i}{5}}{\frac{7}{9}} \text{ complex} \rightarrow \frac{225}{28} + \frac{108}{35} \cdot i$$

$$\frac{\frac{25}{4} + \frac{12 \cdot i}{5}}{\frac{7}{9}} \rightarrow \frac{225}{28} + \frac{108}{35} \cdot i$$

$$(-1)^{\frac{1}{4}} = 0.707 + 0.707i$$

$$(-1)^{\frac{1}{4}} \rightarrow (-1)^{\frac{1}{4}}$$

$$(-1)^{\frac{1}{4}} \text{ complex} \rightarrow \frac{1}{2} \cdot 2^{\frac{1}{2}} + \frac{1}{2} \cdot i \cdot 2^{\frac{1}{2}}$$

$$e^{\frac{\pi}{3} \cdot i} = 0.5 + 0.866i$$

$$e^{\frac{\pi}{3} \cdot i} \rightarrow \frac{1}{2} + \frac{1}{2} \cdot i \cdot 3^{\frac{1}{2}}$$

$$\left( e^{\frac{\pi}{8} \cdot i} \right) \cdot \left( e^{\frac{\pi}{8} \cdot i} \right) \text{ complex} \rightarrow \frac{1}{2} \cdot 2^{\frac{1}{2}} + \frac{1}{2} \cdot i \cdot \left( 2 + 2^{\frac{1}{2}} \right)^{\frac{1}{2}} \cdot \left( 2 - 2^{\frac{1}{2}} \right)^{\frac{1}{2}}$$

$$\left( e^{\frac{\pi}{8} \cdot i} \right) \cdot \left( e^{\frac{\pi}{8} \cdot i} \right) = 0.707 + 0.707i \quad \left( e^{\frac{\pi}{8} \cdot i} \right) \cdot \left( e^{\frac{\pi}{8} \cdot i} \right) \rightarrow \exp\left(\frac{1}{8} \cdot i \cdot \pi\right)^2$$

$$\left( e^{\frac{\pi}{8} \cdot i} \right) \cdot \left( e^{\frac{\pi}{8} \cdot i} \right) \text{ float, 8} \rightarrow .70710677 + .70710679 \cdot i$$

**solve** แสดงผลเฉลยของสมการ

$$2 \cdot x + 5 \text{ solve, } x \rightarrow \frac{-5}{2}$$

$$x^2 - 2 \text{ solve, } x \rightarrow \begin{pmatrix} \frac{1}{2} \\ 2^{\frac{1}{2}} \\ -2^{\frac{1}{2}} \end{pmatrix}$$

$$a \cdot x^2 + b \cdot x + c \text{ solve, } x \rightarrow \begin{bmatrix} \frac{1}{2 \cdot a} \cdot \left[ -b + (b^2 - 4 \cdot a \cdot c)^{\frac{1}{2}} \right] \\ \frac{1}{2 \cdot a} \cdot \left[ -b - (b^2 - 4 \cdot a \cdot c)^{\frac{1}{2}} \right] \end{bmatrix}$$

$$\text{solve}(a \cdot x^2 + b \cdot x + c, x) \rightarrow \begin{bmatrix} \frac{1}{2 \cdot a} \cdot \left[ -b + (b^2 - 4 \cdot a \cdot c)^{\frac{1}{2}} \right] \\ \frac{1}{2 \cdot a} \cdot \left[ -b - (b^2 - 4 \cdot a \cdot c)^{\frac{1}{2}} \right] \end{bmatrix}$$

$$x^3 - 1 \text{ solve, } x \rightarrow \begin{pmatrix} 1 \\ \frac{-1}{2} + \frac{1}{2} \cdot i \cdot 3^{\frac{1}{2}} \\ \frac{-1}{2} - \frac{1}{2} \cdot i \cdot 3^{\frac{1}{2}} \end{pmatrix}$$

$$\text{solve}\left(\frac{x^2}{4} + \frac{y^2}{9} - 1, y\right) \rightarrow \begin{bmatrix} \frac{3}{2} \cdot (-x^2 + 4)^{\frac{1}{2}} \\ \frac{-3}{2} \cdot (-x^2 + 4)^{\frac{1}{2}} \end{bmatrix}$$

**simplify**    ทำการจัดรูปพีชคณิต

$$\left(\frac{4}{5} + \frac{3}{5}i\right)^4 \text{ simplify} \rightarrow \frac{-527}{625} + \frac{336}{625}i$$

$$(x+1) \cdot \left(x - \frac{1}{4}\right) \text{ simplify} \rightarrow \frac{1}{4} \cdot (x+1) \cdot (4x-1)$$

$$\left(e^{\frac{\pi}{8}i}\right) \cdot \left(e^{\frac{\pi}{8}i}\right) \text{ simplify} \rightarrow \frac{1}{2} \cdot 2^{\frac{1}{2}} + \frac{1}{2} \cdot i \cdot 2^{\frac{1}{2}}$$

$$\text{simplify} \left[ (x+1) \cdot \left(x - \frac{1}{4}\right) \right] \rightarrow \frac{1}{4} \cdot (x+1) \cdot (4x-1)$$

$$\frac{3}{19} + \frac{47}{93} \text{ simplify} \rightarrow \frac{1172}{1767}$$

$$\frac{3}{19.0} + \frac{47}{93} \text{ simplify} \rightarrow .66327108092812676854$$

**substitute** ทำแทนค่าตัวแปรในสูตรคณิตศาสตร์

$$x^2 + 2 \cdot x \cdot y + y^2 \text{ substitute } x = 4 \rightarrow 16 + 8 \cdot y + y^2$$

$$x^2 + 2 \cdot x \cdot y + y^2 \text{ substitute } y = 1 \rightarrow x^2 + 2 \cdot x + 1$$

$$x^2 + 2 \cdot x \cdot y + y^2 \text{ substitute } x = \sin(t) \rightarrow \sin(t)^2 + 2 \cdot \sin(t) \cdot y + y^2$$

$$\frac{\frac{25}{4} + \frac{12 \cdot x}{5}}{\frac{7}{9}} \text{ substitute } x = 1 \rightarrow \frac{1557}{140}$$

$$\frac{\frac{25}{4} + \frac{12 \cdot x}{5}}{\frac{7}{9}} \text{ substitute } x = \sin(t) \rightarrow \frac{225}{28} + \frac{108}{35} \cdot \sin(t)$$

**factor** แยกตัวประกอบ ตัวแปร และ ตัวเลข

$$x^3 + 3 \cdot x^2 \cdot y^2 + 3 \cdot x \cdot y^4 + y^6 \text{ factor} \rightarrow (x + y^2)^3$$

$$x^2 - 4 \cdot x - 12 \text{ factor} \rightarrow (x + 2) \cdot (x - 6)$$

$$(x + y^2)^2 \text{ expand} \rightarrow x^2 + 2 \cdot x \cdot y^2 + y^4$$

$$\text{expand}[(x + y^2)^2] \rightarrow x^2 + 2 \cdot x \cdot y^2 + y^4$$

$$(x + y^2 \cdot t)^2 \text{ expand} \rightarrow x^2 + 2 \cdot x \cdot y^2 \cdot t + y^4 \cdot t^2$$

$$\cos(5 \cdot x) \text{ expand} \rightarrow 16 \cdot \cos(x)^5 - 20 \cdot \cos(x)^3 + 5 \cdot \cos(x)$$

$$(x + y^2 \cdot t)^2 \text{ expand} \rightarrow x^2 + 2 \cdot x \cdot y^2 \cdot t + y^4 \cdot t^2 \left| \begin{array}{l} \text{substitute } x = 1 \\ \text{substitute } y = 1 \end{array} \right. \rightarrow 1 + 2 \cdot t + t^2$$

$$10! \text{ factor} \rightarrow 2^8 \cdot 3^4 \cdot 5^2 \cdot 7$$

**coeffs** ช่วยหาสัมประสิทธิ์ของตัวแปรในพหุนาม

$$2 + 3 \cdot x \text{ coeffs, } x \rightarrow \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$(2 + 3 \cdot x)^2 \text{ coeffs, } x \rightarrow \begin{pmatrix} 4 \\ 12 \\ 9 \end{pmatrix}$$

$$x^3 + 3 \cdot x^2 \cdot y^2 + 3 \cdot x \cdot y^4 + y^6 \text{ coeffs, } x \rightarrow \begin{pmatrix} y^6 \\ 3 \cdot y^4 \\ 3 \cdot y^2 \\ 1 \end{pmatrix}$$

$$(\sin(x) + 3 \cdot \cos(x))^2 \text{ expand} \rightarrow \sin(x)^2 + 6 \cdot \sin(x) \cdot \cos(x) + 9 \cdot \cos(x)^2$$

$$(\sin(x) + 3 \cdot \cos(x))^2 \text{ coeffs, } \sin(x) \rightarrow \begin{pmatrix} 9 \cdot \cos(x)^2 \\ 6 \cdot \cos(x) \\ 1 \end{pmatrix}$$

$$(\sin(x) + 3 \cdot \cos(x))^2 \text{ coeffs, } \cos(x) \rightarrow \begin{pmatrix} \sin(x)^2 \\ 6 \cdot \sin(x) \\ 9 \end{pmatrix}$$

**collect**    กระจายสูตรเป็นพหุนาม

$$(x + 2 \cdot y + 3 \cdot z)^2 \text{ collect, } x \rightarrow x^2 + (4 \cdot y + 6 \cdot z) \cdot x + (2 \cdot y + 3 \cdot z)^2$$

$$(x + 2 \cdot y + 3 \cdot z)^2 \text{ collect, } y \rightarrow 4 \cdot y^2 + (4 \cdot x + 12 \cdot z) \cdot y + (x + 3 \cdot z)^2$$

$$(x + 2 \cdot y + 3 \cdot z)^2 \text{ collect, } z \rightarrow 9 \cdot z^2 + (6 \cdot x + 12 \cdot y) \cdot z + (x + 2 \cdot y)^2$$

$$(x + 2 \cdot y + 3 \cdot z)^2 \text{ expand} \rightarrow x^2 + 4 \cdot x \cdot y + 6 \cdot x \cdot z + 4 \cdot y^2 + 12 \cdot y \cdot z + 9 \cdot z^2$$



**series**    หอนุกรมเทย์เลอร์ของฟังก์ชัน

$$e^x \text{ series, } x \rightarrow 1 + 1 \cdot x + \frac{1}{2} \cdot x^2 + \frac{1}{6} \cdot x^3 + \frac{1}{24} \cdot x^4 + \frac{1}{120} \cdot x^5$$

$$e^x \text{ series, } x, 2 \rightarrow 1 + 1 \cdot x$$

$$e^x \text{ series, } x, 3 \rightarrow 1 + 1 \cdot x + \frac{1}{2} \cdot x^2$$

$$e^x \text{ series, } x, 4 \rightarrow 1 + 1 \cdot x + \frac{1}{2} \cdot x^2 + \frac{1}{6} \cdot x^3$$

$$e^x \text{ series, } x, 6 \rightarrow 1 + 1 \cdot x + \frac{1}{2} \cdot x^2 + \frac{1}{6} \cdot x^3 + \frac{1}{24} \cdot x^4 + \frac{1}{120} \cdot x^5$$

$$\sin(t) \text{ series, } t \rightarrow 1 \cdot t - \frac{1}{6} \cdot t^3 + \frac{1}{120} \cdot t^5$$

$$\sin(t) \text{ series, } t, 1 \rightarrow 0$$

$$\sin(t) \text{ series, } t, 2 \rightarrow 1 \cdot t$$

$$\sin(t) \text{ series, } t, 3 \rightarrow 1 \cdot t$$

$$\sin(t) \text{ series, } t, 4 \rightarrow 1 \cdot t - \frac{1}{6} \cdot t^3$$

$$\sin(t) \text{ series, } t, 5 \rightarrow 1 \cdot t - \frac{1}{6} \cdot t^3$$

$$\sin(t) \text{ series, } t, 6 \rightarrow 1 \cdot t - \frac{1}{6} \cdot t^3 + \frac{1}{120} \cdot t^5$$

**convert, parfrac**      กระจายพหุนามเป็นผลบวกของเศษส่วนย่อย

$$\frac{x+1}{(x+2)\cdot(x+3)} \text{ convert, parfrac, x} \rightarrow \frac{-1}{(x+2)} + \frac{2}{(x+3)}$$

$$\frac{x^3+1}{(x+2)\cdot(x+3)} \text{ convert, parfrac, x} \rightarrow x-5 - \frac{7}{(x+2)} + \frac{26}{(x+3)}$$

$$\frac{x^3+1}{x^2+5\cdot x+6} \text{ convert, parfrac, x} \rightarrow x-5 - \frac{7}{(x+2)} + \frac{26}{(x+3)}$$

**laplace, invlaplace**      หาผลการแปลงลาปลาซ และ ผลการแปลงลาปลาซผกผัน

## Definition

$$F(s) = \int_0^{\infty} e^{-s \cdot t} \cdot f(t) dt$$

$$\int_0^{\infty} e^{-s \cdot t} \cdot t^2 dt \rightarrow \lim_{t \rightarrow \infty} \frac{-(\exp(-s \cdot t) \cdot s^2 \cdot t^2 + 2 \cdot s \cdot t \cdot \exp(-s \cdot t) + 2 \cdot \exp(-s \cdot t))}{s^3} + \frac{2}{s^3}$$

$$t^2 \text{ laplace, } t \rightarrow \frac{2}{s^3}$$

$$\frac{2}{s^3} \text{ invlaplace } s \rightarrow t^2$$